# Optimising the Structure of a Cascaded Modular Battery System for Enhancing the Performance of Battery Packs

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### Abstract

The overall performance of battery packs may be affected by imbalances between the series connected cells which is more likely in packs with high number of cells needed to provide a high voltage as needed for example in electric vehicles. In this case, the overall capacity and power capability of the pack is limited by the weakest cell in the stack which results in incomplete utilization of the pack's capabilities. In traditional centralized battery systems (TCBS), this is addressed by implementing cell active/passive balancing circuitry/techniques which restore some of the pack's energy capability. This paper proposes the use of cascaded modular battery systems (CMBS) to remove the need for extra balancing circuitry and maximises the performance and reliability of a battery system containing unequal matched/aged cells. The analysis is assessing the CMBS overall system efficiency, reliability and weight compared to the TCBS for a design of a 300V/3.6kW battery system as a case study.

## **1** Introduction

The degradation of performance of battery packs in battery based power systems as result of mismatch of cell performance or aging can affect the overall system performance so battery management systems (BMS) have an important role to minimise these effects in order to improve the performance and energy utilization of the battery pack and by reducing the stress on weaker cells, prolong its life time. The high voltage bus required by the traction system of electric vehicles requires the use of a large number of series connected cells. Therefore, the capacity of battery packs with series connected cells may be limited by the weakest cell in the string, i.e. if one of the cells lost 10% of its capacity compared to the majority of cells, the overall capacity of the pack will lose 10% as a result as the week cell will reach first the fully charged/discharged condition, and in order to prevent further degradation of this cell, the operation of the whole pack needs to be stopped. Although the mismatching

between pack's cells can be mitigated when the pack is manufactured by selecting cells with similar performance (matched capacity), after significant utilisation of the pack, the degree of capacity mismatch between pack's cells may increase and cannot be mitigated without a corrective actions. TCBS are implementing one of the traditional cells balancing techniques in order to achieve charge balancing to maximize the utilization of the pack capacity. Traditional cells charge balancing techniques are classified into two categories: i) dissipative balancing techniques that connect shunt resistors to dissipate the excess energy from cells with a too high state of charge (SoC) [1, 2] and ii) regenerative balancing techniques that circulate the extra energy from the cells that have a higher SoC to cells with lower SoC by using an efficient converter [3-6].



Fig. 1. System architecture of (a) TCBS (b)CMBS

The regenerative balancing techniques may have the advantages of being more efficient as there is little energy dissipation compared to the dissipative balancing techniques but this depends on how smart the energy circulation algorithm is. This is because the dissipative technique are typically activated only when the battery pack gets closer to the fully charged conditions whilst the regenerative technique may require significantly longer or continuous operation[7]. However, these cannot solve the problem of internal resistance mismatch between series connected cells that results in higher losses continuing to affect weaker cells that further accelerate degradation of their performance. The mismatching of internal resistance between battery cells with very similar matched capacity may be significant and it was shown that it could reach 20% at the beginning of life (BoL)[8], therefore it may reach an even larger value during the lifetime of the battery.

Loading all cells with the same load current share under this mismatching condition of the internal resistances can contribute to significant differences in the cell's temperature affecting more the life time of the hotter cells. Based on this, it is important for the BMS to be able to perform a power losses balancing (PLB) strategy in addition to the charge balancing strategy in order preserve battery life time and achieve safe operation. The PLB strategy cannot be achieved in the TCBS due to the need to have the possibility to change significantly the individual currents of some cells which is impossible in a series connected stack. To implement this, it is required to have a modular battery system having distributed power converters to enable independent control of the current sharing of individual battery cells/modules, according to each cell/module capabilities in terms of power and energy.

Recently, new research has been conducted on the modular battery system concept especially to be used with second life batteries [9]. Such configurations can implement the suggested PLB strategy, but the problem of charge imbalances between the cells of each module still exist that may require additional balancing circuits. The modular battery system concept can be implemented at cell level [10], i.e each converter interfaces a battery cell instead of a battery module which can ensure charge balancing and also can implement the PLB at cell level, but the system will become very complex and expensive for applications where large number of series connected cells are needed as each cell requires a separate converter and control loop.

This paper proposes the use of the modular battery system and identify a design of optimized number of cells per module to maximize the utilization of battery capabilities and overall System efficiency and reliability whilst at minimising the size, cost and complexity.

## 2 Usable capacity

The usable capacity of a battery pack of an n-series connected battery cells can be estimated:

$$U_{Cap} = \sum_{i=1}^{n} Cap(cell_i)$$
(1)

Considering capacity mismatching between pack's cells illustrated in Fig. 2; therefore Equation (1) can be reconstructed as:



Where  $Cap(cell_{weak})$  is the capacity of the weakest cell in the pack.



Fig. 2. Illustrating the usable capacity of a battery pack

Based on Equation (2), the total usable capacity of the pack consists of two terms: the first term is the direct usable capacity (DUC) that can be utilized directly without any additional balancing circuitry which can facilitate fast charging/discharging. The second term is the processing needed capacity (PNC) that cannot be utilized unless a processing technique like the cell charge balancing system (CBS) is activated in the TCBS. Assuming a 10% capacity fade of the weakest cell (Cell<sub>weak</sub>) compared to the average capacity fade of the other cells, this will make the PNC of the pack to become 10 % of the overall usable capacity. In order to remove the need for the CBS, the PNC should be kept as minimum as possible as it will not be utilized in the absence of balancing system.

By using a CMBS topology (Fig. 3) in which the battery pack is split into M-modules each with its own converter, the weakest cell will limit only the capability of its specific module, allowing maximum utilization of the stronger cells in the other modules.



Fig. 3. CMBS architecture

In order to determine the optimum split of battery cells in M modules, let's consider the need to implement a 100-series cells pack having a single cell with a capacity fade of 10%.

As shown in Fig. 4, for a TCBS (M=1) the DUC of the pack is 90% and the PNC is 10% of the available usable capacity (Ucap). This means that 10% of its capacity is lost in absence of a CBS. As the number of modules increases, the PNC decreases until it reaches 0.1% when M=50 (2 cells each module).



Fig. 4. Illustrating the effect of increasing the number of modules on the DUC and PNC of a battery pack.

It can be clearly seen that the PNC reduces significantly as the number of modules increases and this reduces the penalty of not having a CBS. However, increasing the number of modules is adding other penalties on system complexity, energy efficiency and weight which will be analysed in the following section in order to identify the optimal system configuration.

# 3 System design

The analysis will be performed on the CMBS based on a stepdown converter topology (Fig. 5) as it is inherently fault tolerant as any module can be bypassed by just switching-off the converter switches with no need for extra switches [11].



Fig. 5: Step-down topology based CMBS

It is also possible to implement a PLB based on cells internal resistances to ensure equal cell losses and therefore thermal balancing between cells based on an accurate losses observer developed in [12].

#### 3.1 Converter design

Considering that a Li-ion cell voltage varies between 3V to 3.6V based on its SoC and discharging current, so the minimum converter duty-cycle D has been selected to be 80% to maintain bus voltage at 300V when cells are fully charged and increase to 0.99 when discharged. The values of other design parameters are included in Table 1.

| Parameter         | description                   | Value    |
|-------------------|-------------------------------|----------|
| V <sub>cell</sub> | Battery cell voltage          | 3 - 3.6V |
| Ν                 | Total number of battery cells | 100      |
| $\Delta I$        | Inductor current ripple(p-p)  | 4A       |
| Fs                | Switching frequency           | 100kHz   |
| D                 | Converter duty ratio          | 80-100 % |
| Ibus              | Load current                  | 12A      |
| М                 | Number of modules             | 1-50     |

Table 1: converter design parameters

Based on the selected buck-topology, the inductance of each converter's inductor can be calculated:

$$L = \frac{N * V_{cell} * (1 - D) * D}{M * \Lambda I * F}$$
(3)

Based on inductor design rules considering the core geometrical constant  $K_g$  for core sizing [13], the inductor core size can be estimated as:

$$K_{g} = C_{1} \frac{L^{2}}{M^{2} * \frac{R_{DC}}{f_{1}(M)}}$$
(4)

Where  $R_{DC}$  is the winding resistance,  $f_1(M)$  is a function selected based on the required reduction in  $R_{DC}$  with increasing M in order to maintain the overall winding resistance of the system within a required value. As it can be observed in Equation (4) the reduction of the core size with increasing M is affected by  $f_1(M)$ , so a trade-off is required between the level of reduction in the core size with the increa-



Fig. 6. Required CMBS inductance and their corresponding core size

-sing of M to maintain the overall size at minimum and the reduction in the  $R_{DC}$  with increasing M to maintain the overall losses at minimum. Fig. 6 shows the required inductance and core size and its part numbers based on Kool Mµ® materials for each configuration.

The overall mass of the converters inductor can be approximated by excluding the mas of the former as:

$$Mass_{overall} = M^*(m_{core} + m_{copper}), \quad m_{copper} = d^*A_i^*MLT^*n \quad (5)$$

Where  $m_{core}$  is the core mass, d is the density of conductor material,  $A_i$  is the conductor cross section area and *n* the number of inductor turns. As it can be observed in Equation (5), the overall mass of the required inductors increases as M increases but the core size reduces with the increase of M as predicted by (4) and the reduction of the copper mass ( $m_{copper}$ ) as a result, ramping down the increase in overall mass at high values of M. Similarly, the overall  $R_{DC}$  can be estimated based on (6):

$$R_{DC \ overall} = M * \frac{R_{DC}}{f_1(M)} \tag{6}$$

The effect of increasing the number of modules on the CMBS overall inductors mass and overall windings DC resistance is shown in Fig. 7. It can be seen that if the increase in overall mass is somehow limited at high number of modules (M>20), the increase in overall resistance is in fact increasing which means that CMBSs with too high number of modules (M>10) will have significantly higher winding losses in their inductors.



Fig. 7. Overall inductors mass and R<sub>DC</sub> in CMBS3.2 System efficiency

The overall system losses are mainly determined by the inductor and switches losses. Inductor power losses can be approximated as:

$$P_{inductor} = M * P_{core} + I^2_{bus} * R_{DCoverall} + I^2_{AC-RMS} * R_{ACoverall}$$
(7)

Where  $P_{core}$  is the inductor core losses,  $I_{AC-RMS}$  is the RMS value of the inductor current ripple,  $R_{AC}$  are the winding's AC resistances and can be determined as:

$$R_{ACoverall} = C_2 R_{DCoverall} \tag{8}$$

Where:

$$C_{2} \frac{\pi^{*} r^{2}}{\pi^{*} r^{2} - \pi (r - D_{Pent})^{2}} \quad \text{and} \qquad D_{Pent} = \sqrt{\frac{\rho}{\pi^{*} \mu^{*} F_{s}}} \tag{9}$$

Where  $D_{Pent}$  is the penetration depth, to which the current flows at a particular frequency (due to skin effect), r is the conductor radius and  $\mu$  is the conductor's permeability.

The second part of the losses is the switches (MOSFETs) losses which is divided into the conduction and switching losses that can be estimated according to [14] as follows:

$$P_{MOSFETs} = P_{Cond} + P_{SW} \tag{10}$$

Where  $P_{Cond}$  and  $P_{SW}$  are the conduction and switching losses of the MOSFETs for all modules in the CMBS and can be estimated as Equations (11) and (13):

$$P_{Cond} = M * (I^2_{rms}(R_{DSon_{hs}}D + R_{DSon_{hs}}(1-D)))$$
(11)

Where  $R_{DSon_{hs}}$  and  $R_{DSon_{hs}}$  is the on-resistance of the high-side and low-side MOSFETs respectively, D is the duty-ratio and I<sub>rms</sub> is the RMS value of the switches current and estimated as:

$$I_{rms} = \sqrt{I_{bus}^2 + \frac{\Delta I^2}{12}}$$
(12)

The switching losses  $P_{SW}$  is dominated by the power losses during overlap of current and voltage during the transition period that can be estimated as:

$$P_{SW} = M * \left(\frac{N * V_{cell} * I_{bus}}{M} (t_r + t_f) f_{sw}\right)$$
(13)

Where  $t_r$  and  $t_f$  is the rising and fall time of the switching transition which depends on the gate capacitances and gate current.

As can be observed from Equation (11), the conduction losses assumed to be increased linearly with M, however increasing M reduces the required voltage rating of the MOSFETs and it's  $R_{DSon}$  as a result which ramp down the increase in the overall conduction losses. Similarly, based on Equation (13) the overall switching losses decreases as M increases due to the reduction of the MOSFTEs voltage rating and the reduction of gate capacitances as a result.

MOSFETs losses (conduction and switching) as well as inductors losses are shown in Fig. 8. The switching losses are estimated based on VISHAY® MOSFETs with part numbers indicated for each design point on the graph. As it can be noticed, the losses of the TCBS (M=1) is dominated by the MOSFETs losses. For the CMBS topologies as M increases, the overall power losses are increasing due increased inductors losses and MOSFETs conduction losses. The discontinuities in the increasing of the MOSFETs conduction losses at M=4 and M=20 is due to breaks in the  $R_{DSon}$ increasing that seems to be due to changing of the manufacturing technology in order to keep  $R_{DSon}$  at minimum similar to the semiconductor case when changing from planar to trench technology for higher voltage. Overall, it can be noticed that the switching losses mirrors in opposition and level the inductor losses which means their sum remains roughly constant. This means that the lowest losses will be determined by the semiconductor conduction losses which seem to reach a minimum at M=4.



Fig. 8. CMBS different power loss components

#### 3.3 Fault tolerance

The performance of the battery system under fault is very important as it affects the overall performance of the application. In order to analyse the performance of the CMBS under a different faults scenarios, it is important to consider how the faults affects the bus voltage as well as the available usable capacity. The minimum bus voltage under faults can be estimated as:

$$V_{busmin} = (M - x)\frac{N}{M}V_{Cell_{min}} \text{ where } x \le M$$
(14)

Where x is the number of faulty modules and  $V_{\text{Cellmin}}$  is the minimum voltage of the battery cell at highest depth of discharge (DOD). The available usable capacity can be estimated as:

$$U_{Cap_{\min}} = (M - x) \frac{U_{Cap}}{M} - U_{unlz}(V_{Cell_{\min}})$$
(15)

Where  $U_{\text{Cap}}$  is the overall capacity of the pack which is estimated based on Equation (2) and  $U_{\text{untlz}}$  is the unutilized capacity of the battery under limiting  $V_{\text{Cellmin}}$  to a specific value to maintain the bus voltage.



Fig. 9. Available capacity and bus voltage under faults

As it can be observed from Equations (14) and (15), the minimum cell voltage  $V_{\text{Cellmin}}$  at which discharging of the battery has to be stopped, is affecting both the bus voltage and the available capacity  $U_{\text{Cap}}$  but in opposite direction i.e increasing  $V_{\text{Cellmin}}$  will increase the minimum bus voltage but will increase  $U_{\text{untlz}}$  and decrease the  $U_{\text{Capmin}}$  as a result and vice versa. Analysis for minimum bus voltage and available capacity under different fault condition are shown in Fig. 9, the analysis has been done under ( $V_{\text{Cellmin}} = 3.2\text{V}$ ) which is corresponding to 90% DoD that will cause additional loss of the available capacity ( $U_{\text{untlz}} = 10\%$ ).

At M=50, the bus voltage exceeded the designed value (300V), this is due to the selected DoD that can be increased for this specific configuration allowing more usable capacity. As the minimum available bus voltage and available usable capacity are strongly defining the usability of the pack under faults, a combination between  $V_{\text{busmin}}$  and  $U_{\text{Capmin}}$  will be used as an indication for battery system usability under fault (UUF) in the further analysis.

#### 4 CMBS system multi-objective analysis

The different parameters of the system are affected differently with the increase of the number of modules (M), so a multiobjective analysis is required in order to define the optimum configuration based on the different parameters.



Fig. 10. System multi-objective analysis

The system analysis has been done based on the following parameters: i) battery system's DUC (in percentage of pack's capacity), ii) efficiency at full power (3.6kW), iii) UUF (in percentage of pack's usable capacity and designed voltage) under fault in two modules of the system, iv) system simplicity (in percentage of simplicity at M=1) which is inversely proportional to M as the increased number of modules means increased number of control loops and sensors and v) reduction in mass (in percentage of mass at M=50). As it can be seen in Fig. 10, although the TCBS

(M=1) shows a reasonable efficiency, mass reduction and simplicity, the pack's DUC and UUF are poor. On the other hand the CMBS (M>1) shows a good range of DUC, UUF, efficiency and simplicity based on the different values of M. As it can be observed in Fig. 10, it is not easy to identify an optimum solution as each configuration has positives and negatives. Therefore, evaluating a multi-objective cost function is required in order to determine the optimum value for M as:

$$C(M) = W_{DUC}(100 - DUC(M)) + W_{MR}(100 - m(M)) + W_{UUF}(100 - UUF(M) + W_{eff}(100 - eff(M)))$$
(16)

Where  $W_{DUC}$  is the penalty applied to the decrease in DUC,  $W_{MR}$  is the penalty applied to the increase in system mass,  $W_{UUF}$  is the penalty applied to decrease in pack's UUF and  $W_{eff}$  is the penalty applied to decrease in system efficiency. The value of the multi-objective cost function at different M under all penalties=1 are shown in Fig. 11, the minimum cost function is reached at (M=10); at (M<10) the cost function is influenced mainly by the system's UUF and DUC, however at (M>10) the cost function is defined mainly by the system simplicity, reduced mass and losses. Therefore a range of M=5-10 modules may be used for more detailed investigations whereby the penalty coefficients can be more accurately defined.



Fig. 11. Multi-objective system cost function at different M

# Conclusions

The CMBS has been proposed as a smart way to implement battery management functionality and to achieve maximum utilization of battery capacity without the need for cell balancing techniques as used with TCBS. A system analysis have been conducted based on a battery pack of 100 series connected cells to provide a designed bus voltage of 300V for a 3.6kW power system. The analysis showed that a combination of better efficiency, capacity utilization and fault tolerance of the CMBS can be achieved over the TCBS. The methodology to determine the optimum number of modules in cascade has been detailed by means of using a multi-objective cost function evaluation based on relevant system parameters.

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#### References

- S. W. Moore and P. J. Schneider, "A Review of Cell Equalization Methods for Lithium Ion and Lithium Polymer Battery Systems," 2001.
- [2] S. Wen, "Cell balancing buys extra run time and battery life," *Analog Applications Journal*, vol. 1Q, 2009 2009.
- [3] C. Pascual and P. T. Krein, "Switched capacitor system for automatic series battery equalization," in *Proceedings of APEC 97 - Applied Power Electronics Conference*, 1997, pp. 848-854 vol.2.
- [4] M. J. Isaacson, R. P. Hollandsworth, P. J. Giampaoli, F. A. Linkowsky, A. Salim, and V. L. Teofilo, "Advanced lithium ion battery charger," in *Fifteenth Annual Battery Conference on Applications and Advances (Cat. No.00TH8490)*, 2000, pp. 193-198.
- [5] J. Cao, N. Schofield, and A. Emadi, "Battery balancing methods: A comprehensive review," in 2008 IEEE Vehicle Power and Propulsion Conference, 2008, pp. 1-6.
- [6] M. Daowd, N. Omar, P. V. D. Bossche, and J. V. Mierlo, "Passive and active battery balancing comparison based on MATLAB simulation," in 2011 IEEE Vehicle Power and Propulsion Conference, 2011, pp. 1-7.
  - P. Kulsangcharoen, C. Klumpner, M. Rashed, and G. Asher, "Evaluation of a flyback regenerative voltage equalisation circuit for series-connected supercapacitor stacks," in *Proceedings of the 2011 14th European Conference on Power Electronics and Applications*, 2011, pp. 1-12.
- [8] R. Gogoana, M. B. Pinson, M. Z. Bazant, and S. E. Sarma, "Internal resistance matching for parallel-connected lithium-ion cells and impacts on battery pack cycle life," *Journal of Power Sources*, vol. 252, pp. 8-13, 4/15/ 2014.
  - ] N. Mukherjee and D. Strickland, "Analysis and Comparative Study of Different Converter Modes in Modular Second-Life Hybrid Battery Energy Storage Systems," *IEEE Journal of Emerging and Selected Topics in Power Electronics*, vol. 4, pp. 547-563, 2016.
- [10] Y. Li and Y. Han, "A Module-Integrated Distributed Battery Energy Storage and Management System," *IEEE Transactions on Power Electronics*, vol. 31, pp. 8260-8270, 2016.
- [11] A. Fares, C. Klumpner, and M. Sumner, "Investigating the benefits and limitations of cascaded converter topologies used in modular battery systems," in 2017 IEEE 26th International Symposium on Industrial Electronics (ISIE), 2017, pp. 2123-2130.
- [12] A. M. Fares, C. Klumpner, and M. Sumner, "Development of a battery energy loss observer based on improved equivalent circuit modelling," in 2016 18th European Conference on Power Electronics and Applications (EPE'16 ECCE Europe), 2016, pp. 1-10.
- [13] D. M. Robert W. Erickson, Fundamentals of Power Electronics, 2nd edition: KLUWER ACADEMIC PUBLISHERS, 2001.
- [14] J. Klein, "AN-6005 Synchronous buck MOSFET loss calculations with Excel model " *Fairchild applications Bulletin*, 2014.