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# Influence of stabilisers on the unconfined compressive strength of a fine soil

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In foundation engineering, weak subgrade soils are usually improved by adding several stabilisers to satisfy construction requirements, but the influence degree of each stabiliser on the strength of the stabilised soils is rarely studied. In this study, a series of unconfined compressive strength tests was conducted on a fine soil stabilised with various proportions of cement, lime, fly ash and gypsum. The influences of the four stabilisers were investigated through quantitative analysis and grey correlation analysis. The quantitative analysis examined the trends of the unconfined compressive strength with increasing contents of different stabilisers. It was found that there existed optimum fly ash and gypsum contents in this study. Also, the cement had the highest positive impact on the unconfined compressive strength. In the grey relational analysis, different normalisation methods were utilised, and it was found that the normalisation method and the trend of the strength with rising stabiliser content affected the order of the impact of various stabilisers. The grey relational analysis with a range-normalisation method provided a reasonable order of impact in this study.

## Notation

$i$	reference number of each stabiliser
$j$	element number in a sequence
$m$	group test number
$n$	total number of stabilisers
$r_i$	relevancy
$x_0(j)$	reference sequence after normalisation
$x_i(j)$	sequence after normalisation
$y_0(j)$	reference sequence
$y_0^m$	element in a reference sequence
$\bar{y}_i$	average value of comparison sequence
$y_i(1)$	initial value of a comparison sequence
$y_i(j)$	comparison sequence
$y_i^m$	element in a comparison sequence
$\Delta_i(j)$	absolute difference between the normalised reference and normalised comparison sequences
$\Delta_{\max}$	maximum value of $\Delta_i(j)$
$\Delta_{\min}$	minimum value of $\Delta_i(j)$
$\xi_i(k)$	relational coefficient

## Introduction

Weak subgrade soils are often mixed with stabilisers to satisfy construction requirements. The most commonly used stabilisers are cement and lime. As noted by many researchers (e.g. Bell, 1995; Prusinski and Bhattacharja, 1999), cement-treated soils gain their early strength mainly due to hydrolysis and hydration reactions, while their long-term strength is attributed to pozzolanic reactions. As for lime, ion-exchange reactions can take place immediately (Bell, 1996; Sherwood, 1993). Meanwhile, pozzolanic reactions between the remanent calcium hydroxide and active clay minerals can also

improve strength, but their reaction rate is relatively slow (Petry and Little, 2002). In light of geotechnical sustainability, alternative materials such as fly ash and gypsum are also applied in many studies (Purwanto *et al.*, 2020). It was found that an alkaline environment can remarkably improve the degree of activity of fly ash and accelerate the hydration process, and therefore, more cementitious gels and thus a higher strength (Taştan, 2005) can be obtained. Considering that the hydroxide ion content in fly ash is limited, lime or other alkaline excitation agents are always used as supplements (e.g. Chen *et al.*, 2013; Kumar, *et al.* 2007; Sivapullaiah and Jha, 2014). Other combinations of stabilisers are also used by many researchers. For example, cement or fly ash is always applied along with lime to facilitate its pozzolanic reaction (e.g. Åhnberg and Holm, 2009; Indraratna *et al.*, 1995; Jauberthie *et al.*, 2010; Ouhadi *et al.*, 2014). For the combination of cement and fly ash, cement works as a stabiliser as well as an alkali activator for fly ash (Kogbara *et al.*, 2013; Wang and Xu, 2013). Also, adding a proper portion of gypsum as the supplement can help fill the voids in the stabilised soil and thus, improve its strength (Huang and Hu, 1998; Jin *et al.*, 2014). In addition, peat ash, silica sand, sludge ash and other emerging materials can also be used as a stabiliser or supplement for soil stabilisation (e.g. Lin *et al.*, 2007; Mousavi and Wong, 2015).

Nowadays, there are various stabilisers available in the market, and many studies have been conducted to examine the relationship between the stabiliser content and the strength of the stabilised soil considering one or more stabilisers or to select optimum combinations for construction projects. For instance, unconfined compressive strength (UCS), one of the key indicators of the strength of stabilised soils, was studied by Tsuchida and

Tang (2015) for a cement-treated marine clay to obtain the required cement content. Kolay and Pui (2010) investigated the impacts of gypsum and fly ash contents on the UCSs of stabilised muddy soils, and the best combination was recommended based on quantitative analyses. Nevertheless, few scholars have studied the impact degree of each component in a combination of various stabilisers on the strength of stabilised soils. The impact order can help engineers quickly select stabilisers for similar cases.

Grey relational analysis has been widely used to analyse the relationship between several sequences, and the grade of correlation can be determined, known as the grey relational coefficient (Deng, 1989; Gau *et al.*, 2006). In the field of civil engineering, this method has been applied by researchers to study the impact degrees of different factors on a target objective, thus, providing guidance for engineering applications. For instance, Wang *et al.* (2004) studied the correlations between the stability of slide slopes and some sensitive factors. They found that the effects of cohesion and friction angle of the materials are more significant than those of earthquake acceleration and water level in reservoirs. For a cut-and-fill pavement foundation, Su *et al.* (2012) ranked the relations between the slope stability and possible influencing factors, including the properties of fills and the geometry of the embankment slope. He *et al.* (2014) investigated the effect of particle characteristics on the compressive strength for lightweight aggregate concretes and provided suggestions on the optimisation strategy based on grey relational analyses. Zhang and Zhang (2007) considered the effect of different particle fractions of slag powders on the strength of slag cements, and suggestions were proposed to help slag cement gain more strength. It is worth mentioning that one important process in grey relational analysis is the normalisation of source data, since the comparative sequences usually have different dimensions and their numerical values may vary greatly. Several different normalisation methods have been used in previous research studies, such as the range method (e.g. Su *et al.*, 2012), average range method (e.g. He *et al.*, 2014; Zhang and Zhang, 2007), maximisation or minimisation methods (e.g. Mishra *et al.*, 2015) and initialisation method (e.g. Feng *et al.*, 2014). Despite those applications, none of the research studies have examined the effects of different normalisation methods on grey relational analysis results. Also, the applicability of grey relational analysis in identifying the impact degree of various stabilisers on soil strength is yet to be investigated.

In this study, cement, fly ash, lime and gypsum were used as the stabilisers for a fine soil. Their effects on the UCS of the stabilised soil were researched through both quantitative analysis and grey relational analysis. The influence of various normalisation methods was also studied.

## Experimental procedure

### Materials

The fine soil used in this study was taken from an expressway construction site in Ningbo, China, the location of which is shown in Figure 1. Figure 2 shows the gradation curve of the soil



Figure 1. Location of the construction site

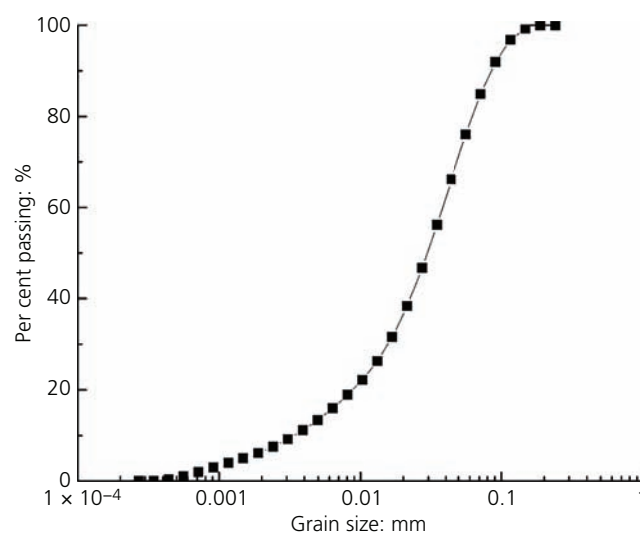


Figure 2. Soil gradation

obtained by using a Battersize 2000 laser particle size analyser. The liquid limit, plastic limit and plastic index of the soil are 24.0%, 14.3% and 9.7, respectively. It can be classified as CL according to the British standard BS 5930:2015 (BSI, 2015). Light compaction tests were carried out on the fine soil according to the standard Proctor compaction test procedure in the British standard BS 1377-2:1990 (BSI, 1990a). It was found that the maximum dry density and the optimum moisture content of the fine soil were  $1.81 \times 10^3 \text{ kg/m}^3$  and 9.4%, respectively.

Four stabilisers, cement, fly ash, quick lime and gypsum, were used in this project. The Portland cement CEM I 42.5 N was

Table 1. Chemical composition of the class II fly ash

Component	Loss on ignition	Silicon dioxide (SiO <sub>2</sub> )	Iron (III) oxide (Fe <sub>2</sub> O <sub>3</sub> )	Calcium oxide (CaO)	Magnesium oxide (MgO)	Aluminium oxide (Al <sub>2</sub> O <sub>3</sub> )
Mass percentage: %	7.50	56.96	4.63	1.50	1.50	23.67

provided by Hailuo Cement Company, China. The fly ash was classified as class II, the chemical composition and the gradation

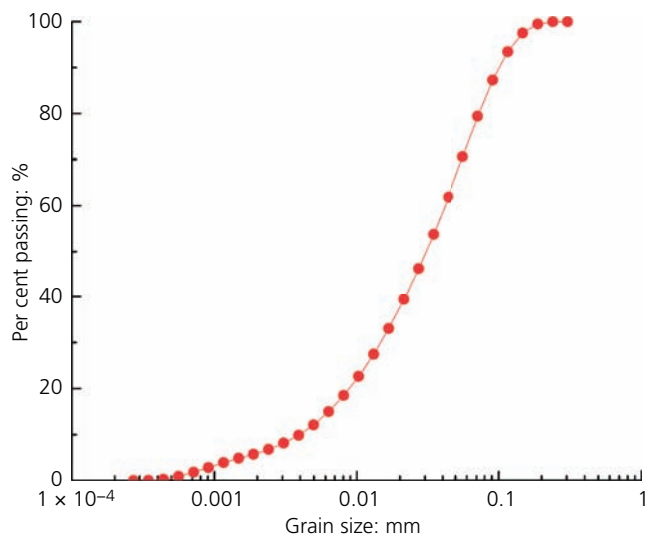


Figure 3. Fly ash gradation

of which are given in Table 1 and Figure 3, respectively. The quick lime had a purity higher than 98%, and the gypsum was mainly composed of calcium sulfate dihydrate ( $\geq 99\%$ ).

### Test plan and test procedure

In this study, UCS tests were conducted to investigate the effects of different stabilisers and their contents. The moisture content of the fine soil was kept at 20%, and its UCS was found to be 0.033 MPa. The test plan is shown in Table 2. The group name reflects the contents of the stabilisers, in which CE, CA, FA and CAS represent cement, lime, fly ash and gypsum, respectively. The stabiliser contents are by the weight of the dry soil. For example, CA4-FA8-CE2-CAS1 represents 4% lime, 8% fly ash, 2% cement and 1% gypsum.

The samples were prepared following the steps below.

- Soils from the construction site were ground into smaller assemblies after drying by oven in the laboratory and then screened through a 0.2 mm sieve.
- The prepared soils were first well mixed with different stabilisers and then mixed with water by an electronic mixer.

Table 2. Test plan and UCSs

Group name	CE: %	CA: %	FA: %	CAS: %	UCS: MPa	Increase percentage after stabilisation: %	Group
CA2-FA4	0	2	4	0	0.183	454.5	I
CA2-FA6	0	2	6	0	0.248	651.5	I
CA2-FA8	0	2	8	0	0.320	869.7	I
CA2-FA10	0	2	10	0	0.194	487.9	II
CA2-FA12	0	2	12	0	0.209	533.3	II
CA4-FA8	0	4	8	0	0.256	675.8	II
CA4-FA12	0	4	12	0	0.255	672.7	II
CA4-FA16	0	4	16	0	0.274	730.3	II
CA6-FA12	0	6	12	0	0.306	827.3	II
CA6-FA18	0	6	18	0	0.327	890.9	II
CA6-FA24	0	6	24	0	0.308	833.3	I
CA2-FA4-CE2	2	2	4	0	0.326	887.9	I
CA2-FA4-CE3	3	2	4	0	0.451	1266.7	I
CA2-FA4-CE4	4	2	4	0	0.600	1718.2	I
CA2-FA4-CE2-CAS0.5	2	2	4	0.5	0.367	1012.1	I
CA2-FA4-CE2-CAS1	2	2	4	1.0	0.378	1045.5	I
CA2-FA4-CE2-CAS1.5	2	2	4	1.5	0.431	1206.1	I
CA2-FA4-CE2-CAS2	2	2	4	2.0	0.464	1306.1	I
CA2-FA4-CE2-CAS3	2	2	4	3.0	0.442	1239.4	II
CA2-FA4-CE2-CAS4	2	2	4	4.0	0.469	1321.2	II
CA2-FA4-CE2-CAS5	2	2	4	5.0	0.444	1245.5	II
CA3-FA6-CE2-CAS1	2	3	6	1.0	0.522	1481.8	I
CA3-FA6-CE3-CAS1	3	3	6	1.0	0.542	1542.4	I
CA4-FA8-CE2-CAS1	2	4	8	1.0	0.582	1663.6	I
CA4-FA8-CE4-CAS1	4	4	8	1.0	0.927	2709.1	I

CA, lime; CE, cement; FA, fly ash; CAS, gypsum

- (c) The mixture was compacted into a steel mould layer by layer (three layers in total) within half an hour. Each layer interface surface was grooved.
- (d) The soil sample was carefully removed from the mould by a hydraulic demolding instrument.
- (e) Once finished, the specimens were sealed and cured under a constant temperature of 20°C and a humidity of 95% for 7 days.

The UCS tests were carried out by using a model E45 MTS universal tester (Figure 4) following BS 1377-7:1990 (BSI, 1990b). The specimens were 50 mm in diameter and 100 mm high. The loading rate of the UCS test carried out in this study was 1 mm/min until the specimen failed. In each test group, the test was replicated at least three times to ensure that the standard deviation is no larger than 0.05, and the averaged value was finally taken as the UCS of the test group.

## Results and discussion

### Quantitative analysis

The UCS test results are shown in Table 2. Figures 5–7 show the variation of UCS with different contents of the stabilisers. As can be seen in Figure 5(a), for given lime and fly ash contents, when the cement content was changed from 2 to 4%, the UCS proportionally increased by a magnitude of 274 kPa. This linear



Figure 4. Photograph of the model E45 MTS universal tester

relationship is consistent with previous findings (e.g. Pandey and Rabbani, 2017). When the cement content was increased from 0 to 2%, the UCS was raised by 143 kPa.

Compared with cement, the influences of lime and fly ash contents are relatively small. For instance, when increasing the lime or fly ash content from 4 to 6%, the UCS is raised by 51 kPa (Figure 5(b)) and 65 kPa (Figure 5(c)), respectively. Moreover, for a given lime content, there exists an optimum fly ash content that can maximise the UCS, which agrees with the finding of Kumar *et al.* (2007). It is further found that when the lime content is relatively high, the influence of the fly ash content becomes limited, as shown in Figure 6, and therefore, the increase of UCS in these cases is mainly attributed to the rise of the lime content. It can also be inferred from Figure 7 that the effect of cement is higher than the overall effect of lime and fly ash, since the growth trend of the UCS is changed from deceleration to acceleration due to some additional cement.

The influence of gypsum is demonstrated in Figure 5(d). It can be known that the strengths of the materials have been enhanced due to the addition of gypsum and an optimum content of gypsum is observed, above which the strength starts to decrease with increasing gypsum content. Huang and Hu (1998), Guo (2007), Huang *et al.* (2007) and Jin *et al.* (2014) had similar findings and explained that the excessive expansion of ettringites in gypsum may destroy the whole structure of the stabilised soil on the micro level, thereby resulting in a reduction in strength. Another possible reason is that the reaction process of gypsum is slow in the stabilised soil; if excess gypsum is added, the unreacted gypsum may weaken the bonds between soil particles and the cementitious compounds due to the platy shape of gypsum particles (Kolay and Pui, 2010; Kumar *et al.*, 2007). When the gypsum content is increased from 0 to 2%, the UCS is raised by 138 kPa, which is lower than that of cement but higher than those of lime and fly ash.

It can be concluded from the preceding quantitative analyses that cement has the most obvious effect on the UCS and the addition of gypsum can further increase its strength effectively. The effect of fly ash is limited, particularly when the lime content is high. Also, increasing the lime content alone could not affect the strength obviously. Moreover, it was found that a higher stabiliser content is normally in correspondence to a higher stiffness and a smaller deformation at failure, as shown in typical stress–strain curves in Figure 8. Also, note that the effects of fly ash and lime on the UCSs could become more obvious if a longer curing period is considered, as the hydration reaction rate for fly ash and pozzolanic reaction rate for lime are slow. Therefore, even though the effects of lime and gypsum are limited, their effectiveness on the long-term strength of stabilised soils needs further assessment in the future by considering longer curing periods.

### Grey relational analysis

In the grey relational analysis system, the UCSs in Table 2 were used as the reference sequence  $y_0(j) = y_0^1, y_0^2, \dots, y_0^m$ , where  $m$  represents the number of the group tests. Meanwhile, the contents

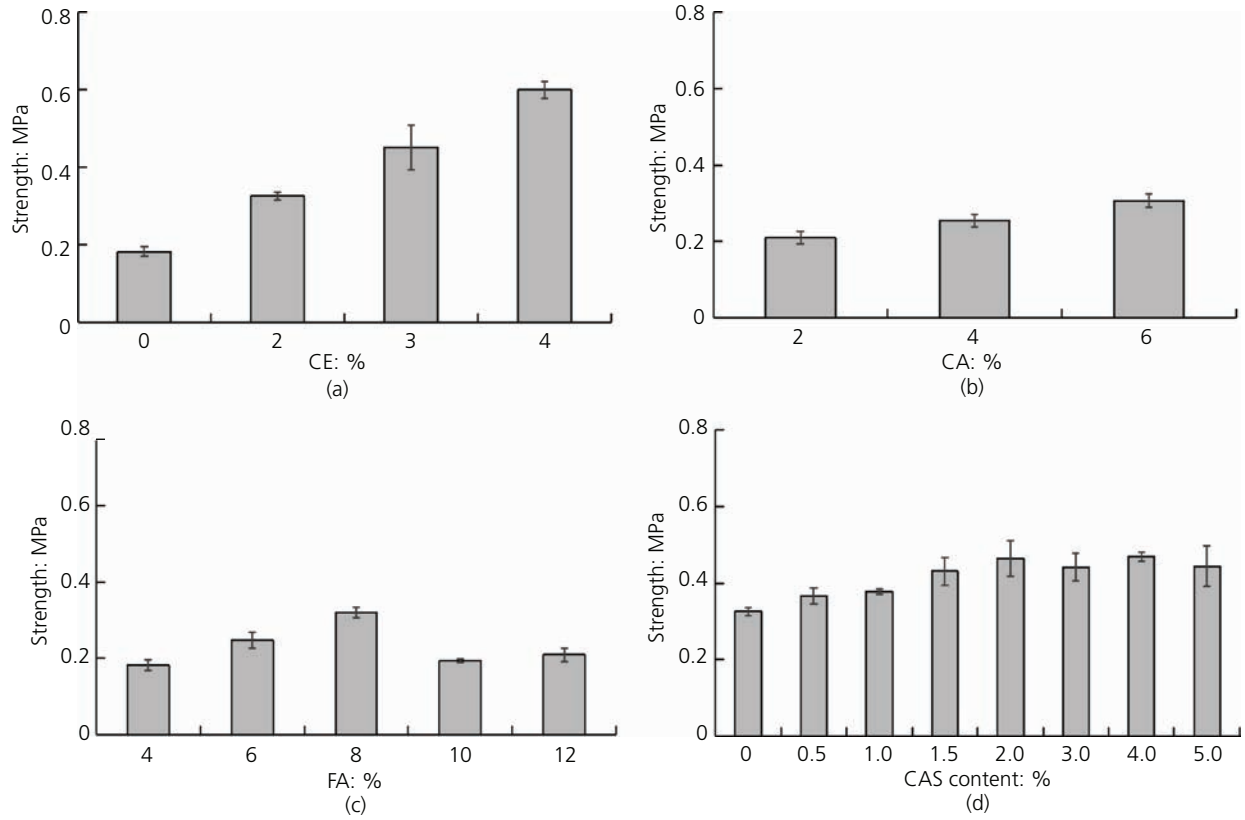


Figure 5. Influences of FA, CA and CE contents on UCS: (a) CA = 2%, FA = 4%; (b) FA = 12%; (c) CA = 2%; (d) CA = 2%, FA = 4%, CE = 2%

of the four stabilisers were set as comparison sequences  $y_i(j) = y_i^1, y_i^2, \dots, y_i^m$ , where  $i = 1, 2, \dots, n$ , representing the reference number of each stabiliser.

Following that, each sequence should be scaled using one normalisation method in order to eliminate the effect of various ranges of different sequences. In this study, five commonly used

normalisation methods (Equations 1–5) were considered and the most effective one can be determined referring to the quantitative analyses. Note that among those methods, the maximisation method will lead to an infinite value of  $x_i(j)$ ; thus, it will not be used in the following analysis. The data after each normalisation method are shown in Table 3.

(a) Initialisation

$$1. \quad x_i(j) = \frac{y_i(j)}{y_i(1)} \quad y_i(1) \neq 0$$

(b) Average

$$2. \quad x_i(j) = \frac{y_i(j)}{\bar{y}_i} \quad \bar{y}_i = \frac{1}{m} \sum_{j=1}^m y_i(j)$$

(c) Range

$$3. \quad x_i(j) = \frac{y_i(j) - \min[y_i(j)]}{\max[y_i(j)] - \min[y_i(j)]}$$

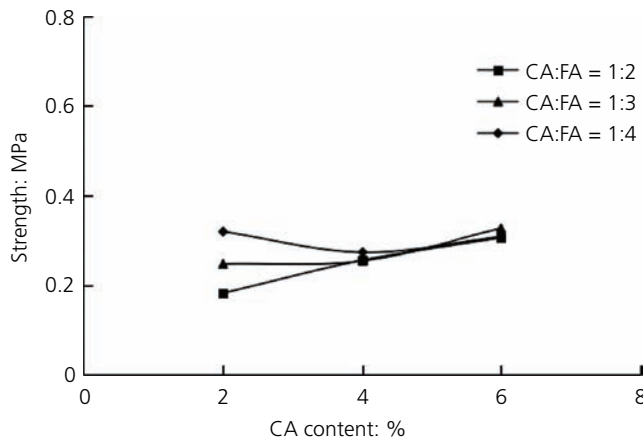


Figure 6. Influence of FA/CA ratio on UCS

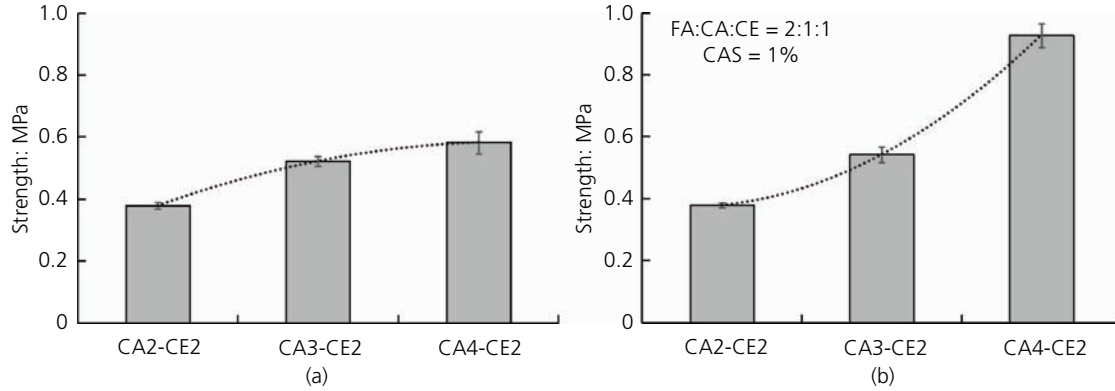


Figure 7. Influences of different proportions of stabilisers on UCS when (a) CA:FA = 1:2 and (b) CAS = 1%

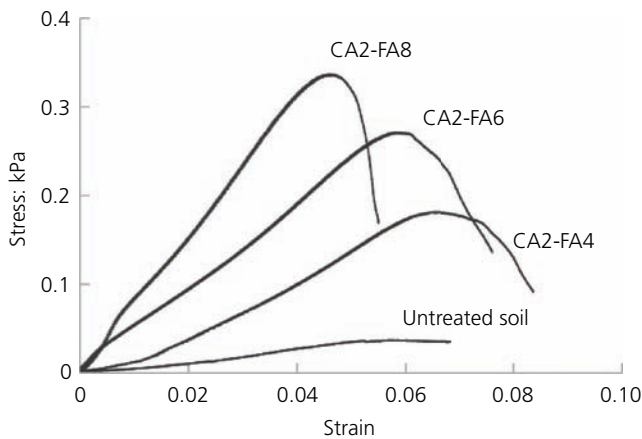


Figure 8. Stress–strain curves for raw and stabilised soils

(d) Maximisation

$$4. \quad x_i(j) = \frac{y_i(j)}{\min[y_i(j)]}$$

(e) Minimisation

$$5. \quad x_i(j) = \frac{y_i(j)}{\max[y_i(j)]}$$

Then, the absolute difference of sequences of  $x_0$  and  $x_i$  was calculated using Equation 6, in which the reference sequence  $x_0(j)$  for each normalisation method is the corresponding UCS sequence in Table 3.

$$6. \quad \Delta_i(j) = |x_0(j) - x_i(j)|$$

Based on those, the maximum and minimum values of  $\Delta_i(j)$  were obtained:

$$7. \quad \Delta_{\max} = \max_i \max_j [\Delta_i(j)]$$

$$8. \quad \Delta_{\min} = \min_i \min_j [\Delta_i(j)]$$

Moreover, the relational coefficient of each test was calculated:

$$9. \quad \xi_i(k) = \frac{\Delta_{\min} + \rho \Delta_{\max}}{\Delta_i(j) + \Delta_{\max}}$$

where  $\rho$  is a resolution coefficient, between 0 and 1, normally taken as 0.5.

Finally, the relevancy of each factor (stabiliser content) were obtained by calculating the relational coefficient:

$$10. \quad r_i = \frac{1}{n} \sum_{k=1}^n \xi_i(k)$$

For the cases in this study, relational coefficients obtained using different normalisation methods are shown in Table 4 and compared in Figure 9. Normally, a factor is considered more influential on the reference value if its relational coefficient is relatively high (Subhash *et al.*, 2020). Therefore, the order of the impact degree of various factors on the UCS can be obtained, as shown in Table 5. It can be seen that by using different normalisation methods, the orders are different. Using the average method, it appears that the effect of cement content is smaller than that of lime content, which is contradictory to the quantitative analysis. Table 4 also shows that either fly ash or gypsum has the lowest influence on the UCS. One possible reason is that the effects of fly ash and gypsum on the UCS are not

Table 3. Normalised data (arbitrary units) by using four normalisation methods

Group name	Initialisation					Average					Range					Minimisation				
	CE	CA	FA	CAS	UCS	CE	CA	FA	CAS	UCS	CE	CA	FA	CAS	UCS	CE	CA	FA	CAS	UCS
CA2-FA4-CE2-CAS0.5	1.0	1.0	1.0	1	1.00	1.47	0.68	0.51	0.60	0.93	1.47	0.68	0.51	0.60	0.93	0.5	0.33	0.17	0.1	0.40
CA2-FA4-CE2-CAS1	1.0	1.0	1.0	2	1.03	1.47	0.68	0.51	1.19	0.96	1.47	0.68	0.51	1.19	0.96	0.5	0.33	0.17	0.2	0.41
CA2-FA4-CE2-CAS1.5	1.0	1.0	1.0	3	1.18	1.47	0.68	0.51	1.79	1.10	1.47	0.68	0.51	1.79	1.10	0.5	0.33	0.17	0.3	0.46
CA2-FA4-CE2-CAS2	1.0	1.0	1.0	4	1.27	1.47	0.68	0.51	2.38	1.18	1.47	0.68	0.51	2.38	1.18	0.5	0.33	0.17	0.4	0.50
CA2-FA4-CE2-CAS3	1.0	1.0	1.0	6	1.21	1.47	0.68	0.51	3.57	1.13	1.47	0.68	0.51	3.57	1.13	0.5	0.33	0.17	0.6	0.48
CA2-FA4-CE2-CAS4	1.0	1.0	1.0	8	1.28	1.47	0.68	0.51	4.76	1.19	1.47	0.68	0.51	4.76	1.19	0.5	0.33	0.17	0.8	0.51
CA2-FA4-CE2-CAS5	1.0	1.0	1.0	10	1.21	1.47	0.68	0.51	5.95	1.13	1.47	0.68	0.51	5.95	1.13	0.5	0.33	0.17	1.0	0.48
CA3-FA6-CE2-CAS1	1.0	1.5	1.5	2	1.42	1.47	1.01	0.76	1.19	1.33	1.47	1.01	0.76	1.19	1.33	0.5	0.50	0.25	0.2	0.56
CA3-FA6-CE3-CAS1	1.5	1.5	1.5	2	1.48	2.21	1.01	0.76	1.19	1.38	2.21	1.01	0.76	1.19	1.38	0.8	0.50	0.25	0.2	0.58
CA4-FA8-CE2-CAS1	1.0	2.0	2.0	2	1.59	1.47	1.35	1.01	1.19	1.48	1.47	1.35	1.01	1.19	1.48	0.5	0.67	0.33	0.2	0.63
CA4-FA8-CE4-CAS1	2.0	2.0	2.0	2	2.53	2.94	1.35	1.01	1.19	2.36	2.94	1.35	1.01	1.19	2.36	1.0	0.67	0.33	0.2	1.00
CA2-FA4	0	1.0	1.0	0	0.50	0	0.68	0.51	0	0.46	0	0.68	0.51	0	0.46	0	0.33	0.17	0	0.20
CA2-FA6	0	1.0	1.5	0	0.68	0	0.68	0.76	0	0.63	0	0.68	0.76	0	0.63	0	0.33	0.25	0	0.27
CA2-FA8	0	1.0	2.0	0	0.87	0	0.68	1.01	0	0.81	0	0.68	1.01	0	0.81	0	0.33	0.33	0	0.34
CA2-FA10	0	1.0	2.5	0	0.53	0	0.68	1.26	0	0.49	0	0.68	1.26	0	0.49	0	0.33	0.42	0	0.21
CA2-FA12	0	1.0	3.0	0	0.57	0	0.68	1.52	0	0.53	0	0.68	1.52	0	0.53	0	0.33	0.50	0	0.23
CA4-FA8	0	2.0	2.0	0	0.70	0	1.35	1.01	0	0.65	0	1.35	1.01	0	0.65	0	0.67	0.33	0	0.28
CA4-FA12	0	2.0	3.0	0	0.69	0	1.35	1.52	0	0.65	0	1.35	1.52	0	0.65	0	0.67	0.50	0	0.27
CA4-FA16	0	2.0	4.0	0	0.75	0	1.35	2.02	0	0.70	0	1.35	2.02	0	0.70	0	0.67	0.67	0	0.30
CA6-FA12	0	3.0	3.0	0	0.83	0	2.03	1.52	0	0.78	0	2.03	1.52	0	0.78	0	1.00	0.50	0	0.33
CA6-FA18	0	3.0	4.5	0	0.89	0	2.03	2.27	0	0.83	0	2.03	2.27	0	0.83	0	1.00	0.75	0	0.35
CA6-FA24	0	3.0	6.0	0	0.84	0	2.03	3.03	0	0.78	0	2.03	3.03	0	0.78	0	1.00	1.00	0	0.33
CA2-FA4-CE2	1.0	1.0	1.0	0	0.89	1.47	0.68	0.51	0	0.83	1.47	0.68	0.51	0	0.83	0.5	0.33	0.17	0	0.35
CA2-FA4-CE3	1.5	1.0	1.0	0	1.23	2.21	0.68	0.51	0	1.15	2.21	0.68	0.51	0	1.15	0.8	0.33	0.17	0	0.49
CA2-FA4-CE4	2.0	1.0	1.0	0	1.64	2.94	0.68	0.51	0	1.53	2.94	0.68	0.51	0	1.53	1.0	0.33	0.17	0	0.65

Table 4. Correlation coefficients

Normalisation method	Lime	Fly ash	Cement	Gypsum	Order of impact on UCS
Initialisation	0.891	0.835	0.910	0.790	Cement > lime > fly ash > gypsum
Average	0.842	0.787	0.815	0.746	Lime > cement > fly ash > gypsum
Range	0.609	0.595	0.757	0.707	Cement > gypsum > lime > fly ash
Minimisation	0.700	0.621	0.723	0.569	Cement > lime > fly ash > gypsum

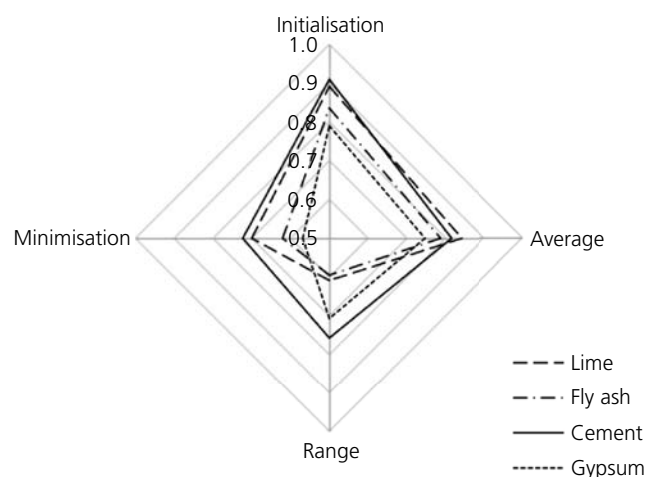


Figure 9. Comparison of correlation coefficients for different normalisation methods and stabilisers

always positive. Optimum contents can be observed in Figures 5(c) and 5(d). Therefore, grey relational analyses were further carried out by only using the data within the increase stage. All test results in Table 2 were divided into two groups. Group I refers to the cases where the rise of the stabiliser content has a clear positive impact, while group II represents the rest. Accordingly, the relational coefficients and the orders of impact were obtained and are shown in Table 5. According to the results obtained through the quantitative analysis, it is clear that the order obtained through the range method is more reasonable when compared with those of the other three methods.

### Conclusion

This study investigated the effects of four stabilisers on the UCS of a stabilised fine soil using quantitative analysis and grey relational analysis. In the quantitative analysis, it was found that there exists a positive linear relationship between the cement content and UCS. The effect of the cement content on the UCS is higher than that of gypsum, followed by those of lime and fly ash. For both fly ash and gypsum, there exist optimum contents that can maximise the UCS.

Table 5. Correlation coefficients for the increase stage

Normalisation method	Lime	Fly ash	Cement	Gypsum	Order of impact on UCS
Initialisation	0.949	0.930	0.930	0.833	Lime > cement ≈ fly ash > gypsum
Average	0.946	0.920	0.911	0.799	Lime > fly ash > cement > gypsum
Range	0.655	0.653	0.734	0.710	Cement > gypsum > lime ≈ fly ash
Minimisation	0.770	0.733	0.752	0.617	Lime > cement > fly ash > gypsum

In grey relational analysis, the selection of the normalisation method can change the correlation ranking of the stabilisers with respect to UCS. In this study, the analysis using the range-normalisation method gives a reasonable ranking of the stabilisers, whereas the average method is not applicable. The order of impact is also affected by the changing trend of the UCS, which is not explicitly shown in the calculated relational coefficients; therefore, grey relational analysis should be conducted with care when a change of trend is possible.

It can be further concluded that cement is the most effective stabiliser for fine soil. The addition of a proper content of gypsum can further increase its strength. The effects of quick lime and fly ash are limited on the early-stage (7-day) strength, but their influences on the long-term strength need further assessments.

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