



Numerical modelling of intra-wave sediment transport on sandy beaches using a non-hydrostatic, wave-resolving model

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Abstract

The mutual feedback between the swash zone and the surf zone is known to affect large-scale morphodynamic processes such as breaker bar migration on sandy beaches. To fully resolve this feedback in a process-based manner, the morphodynamics in the swash zone and due to swash-swash interactions must be explicitly solved, e.g., by means of a wave-resolving numerical model. Currently, few existing models are able to fully resolve the complex morphodynamics in the swash zone, and none is practically applicable for engineering purposes. This work aims at improving the numerical modelling of the intra-wave sediment transport on sandy beaches in an open-source wave-resolving hydro-morphodynamic framework (e.g., non-hydrostatic XBeach). A transport equation for the intra-wave suspended sediment concentration, including an erosion and a deposition rate, is newly implemented in the model. Two laboratory experiments involving isolated waves and wave trains are simulated to analyse the performance of the model. Numerical results show overall better performance in simulating single waves rather than wave trains. For the latter, the modelling of the morphodynamic response improves in the swash zone compared with the existing sediment transport modelling approach within non-hydrostatic XBeach, while the need of including additional physical processes to better capture sediment transport and bed evolution in the surf zone is highlighted in the paper.

Keywords Wave-resolving modelling · Hydro-morphodynamics modelling · Intra-wave sediment transport · Suspended sediment concentration · Swash zone

1 Introduction

Sandy beach evolution plays a key role in coastal vulnerability, influencing the stability of ecosystems and coastal communities' economy and safety. Their morphodynamical evolution and response to drivers such as increased storminess remain difficult to predict (Wong et al. 2014).

The exchange of sediments between the swash zone and the surf zone determines the evolution of the beach

and shoreface (Masselink and Puleo 2006; Brocchini and Baldock 2008; Alsina et al. 2012; Masselink and Gehrels 2014). These two regions behave as interacting and co-evolving morphodynamic subsystems. Consequently, it is difficult to separate the contributions of the surf zone and swash zone to the development and migration of breaker bars. Moreover, swash-swash interactions present in wave trains can affect the offshore-directed sediment transport that feeds the migration of bars (Alsina et al. 2012).

Wave-resolving hydro-morphodynamic models are needed to provide an accurate description of these complex dynamics because they include intra-wave physical processes, which make these models suitable to fully solve swash morphodynamics. The models of this type in the literature use as governing hydrodynamic equations one of the following alternatives: the Non-Linear Shallow Water Equations (NLSWE) (e.g., Li et al. 2002, Postacchini et al. 2012, Zhu and Dodd 2015, Incelli et al. 2016, see Briganti et al. 2016 for a review), the non-hydrostatic NLSWE (e.g., Smit et al. 2010, Ma et al. 2012, Ruffini et al. 2020), or Boussinesq-type equations (e.g., Xiao et al. 2010, Wenneker

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et al. 2011, Kim et al. 2017). While hydrostatic NLSWE do not allow frequency dispersion, thus limiting their application, the other two aforementioned sets of flow equations are widely used for wave propagation from intermediate waters to the shoreline. The non-hydrostatic NLSWE are used in the open-source Non-Hydrostatic version of the XBeach (XBNH) model (Smit et al. 2010; Roelvink et al. 2018). To enable the computation of morphodynamics, these models would require sub-models that compute suspended and bed load sediment transport based on intra-wave hydrodynamics, from which in turn bed level change can be computed.

In the framework of non-hydrostatic NLSWE, formulations of sediment transport have been extensively tested for gravel beaches (e.g., McCall et al. 2015), but not for sandy beaches. Ruffini et al. (2020) showed that application of a wave-averaged sediment transport equation (Van Thiel de Vries 2008; Van Rijn 2007) in XBNH led to inaccurate simulated beach morphodynamics, which was related to inaccuracies in modelled sediment concentrations, particularly during flow reversal.

The aim of this work is to improve the modelling of intra-wave sediment dynamics in XBNH. To this end, the Pritchard and Hogg (2003) and Meyer-Peter and Müller (1948) formulations are chosen because of their good performance in the swash zone (see Zhu and Dodd 2015). The present study focuses on modelling the dynamics of sediment in the nearshore zone in all stages of the flow both for solitary waves, i.e., isolated waves, and wave trains, with significant swash-swash interactions. First, the proposed hydro-morphodynamic model is verified against a high-resolution numerical solution of an idealised bore generated by a solitary wave over an erodible sloped beach. Subsequently, two experimental case studies are simulated involving bichromatic wave groups and consecutive non-interacting solitary waves over sandy beaches. For the former, a sensitivity analysis of the results to the parameters used in the Pritchard and Hogg (2003) sediment transport equation is also carried out.

This paper is organised as follows: XBNH, with a focus on the sediment transport and bed-updating modelling, is described in Section 2; verification of the proposed model is illustrated in Section 3; the performance of the model against two laboratory experiments is presented in Sections 4 and 5, respectively; discussion of results and concluding remarks with recommendations for future works are given in Sections 6 and 7, respectively.

2 Model description

XBNH consists of coupled wave-resolving hydrodynamics and morphodynamics equations. The existing approach

for suspended and bed load transport in XBNH were originally developed for the Wave-Averaged Sediment Transport (WAST) modelling (see Appendix 1). Therefore, in the present work, a wave-resolving formulation for the suspended sediment transport is implemented in the model. To this end, the transport advection equation of Pritchard and Hogg (2003) is chosen. XBNH computes the bed load transport using the Meyer-Peter and Müller (1948) expression. The combined use of the newly implemented Pritchard and Hogg (2003) equation with the Meyer-Peter and Müller (1948) formula within XBNH for the Intra-Wave Sediment Transport (IWST) modelling is herein referred as XBNH-IWST. In this work, only the cross-shore direction is considered; Fig. 1 shows a schematisation of a typical cross-shore profile with the main variables used.

The model performance is quantified by computing the normalised Root-Mean-Square Error (nRMSE), defined as:

$$nRMSE = \frac{\sqrt{\frac{1}{N} \sum_i^N (y_{m,i} - y_{ref,i})^2}}{s_{y_{ref}}}, \quad (1)$$

where $y_{m,i}$ is the i -th sample of the modelled quantity y , and $y_{ref,i}$ is the i -th sample of the corresponding reference variable (e.g., semi-analytical, experimental); N is the number of samples; $s_{y_{ref}}$ is the standard deviation of the reference quantity, y_{ref} , and it is defined as:

$$s_{y_{ref}} = \sqrt{\frac{1}{N-1} \sum_i^N (y_{ref,i} - \bar{y}_{ref})^2}, \quad (2)$$

with $\bar{y}_{ref} = (1/N) \sum_i^N y_{ref,i}$ being the mean value of y_{ref} . nRMSE = 0 indicates perfect agreement between model predictions and reference quantities, whereas nRMSE = 1 indicates that the Root-Mean-Square Error (RMSE) equals $s_{y_{ref}}$.

Following Bosboom et al. (2020), the Root-Mean-Square Transport Error (RMSTE) is also computed to quantify the model performance in terms of final bed changes. The RMSTE (m^2) measures the mismatch between the predicted final bed level, $z_{b_{f,m}}$, and the reference one, $z_{b_{f,ref}}$, in terms of the minimum (i.e., optimal) quadratic sediment transport cost required to transform the predictions into the reference field, and it is computed as:

$$RMSTE = \sqrt{\frac{1}{N} \sum_i^N Q_i^2}, \quad (3)$$

where Q_i is i -th sample along the cross-shore coordinate, x , of the sediment volume, Q , required to transform $z_{b_{f,m}}$ into $z_{b_{f,ref}}$. The conservation of mass is satisfied so that $\partial Q / \partial x = z_{b_{f,m}} - z_{b_{f,ref}}$ and $Q_{i=1} = 0$ is assumed (with $i = 1$ referring to the onshore boundary of the x -domain, located landward of the maximum run up).

To further assess the correlation between time series of modelled and reference quantities, Pearson's cross-correlation coefficient, $-1 \leq \rho_{mr} \leq 1$, is used and it is defined as:

$$\rho_{mr} = \frac{\text{cov}(y_{ref}, y_m)}{s_{y_{ref}} s_{y_m}}, \quad (4)$$

where $\text{cov}(y_{ref}, y_m)$ is the covariance of the time series of modelled and reference quantities and it is computed as:

$$\text{cov}(y_{m,i}, y_{ref,i}) = \frac{1}{(N-1)} \sum_i^N (y_{m,i} - \bar{y}_m)(y_{ref,i} - \bar{y}_{ref}), \quad (5)$$

where $\bar{y}_m = (1/N) \sum_i^N y_{m,i}$ is the mean value of y_m , and s_{y_m} is the standard deviation of the time series of the predicted quantity.

2.1 Hydrodynamics

The hydrodynamics in XBNH is similar to the one-layer version of SWASH (Zijlema et al. 2011). The depth-averaged flow is computed using the non-hydrostatic 1D (one-dimensional) NLSWE:

$$\frac{\partial \eta}{\partial t} + \frac{\partial hu}{\partial x} = 0, \quad (6)$$

$$\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} - \frac{\partial}{\partial x} \left(v_h \frac{\partial u}{\partial x} \right) = -\frac{1}{\rho} \frac{\partial (\rho p_{nh} + \rho g \eta)}{\partial x} - \frac{\tau_b}{h}, \quad (7)$$

where t is time, η is the water surface elevation from the Still Water Level (SWL), u is the depth-averaged cross-shore velocity, h is the total water depth, v_h is the horizontal viscosity, ρ is the density of water, p_{nh} is the depth-averaged dynamic pressure normalised by the density, g is the gravity acceleration constant and τ_b is the total bed shear stress, which is computed as:

$$\tau_b = \rho c_f u |u|, \quad (8)$$

where c_f is the dimensionless friction coefficient. Relatively simple unsteady Bottom Boundary Layer (BBL) models, such as the momentum integral method (Sumer et al. 1987) used also in NLSWE solvers (e.g., Briganti et al. 2011), could be considered. However, the results in terms of τ_b are comparable with simpler formulations, such as the one considered in this study (see e.g., Briganti et al. 2018). Also, phase differences could be significant and more complex BBL models should be used (e.g., Rijnsdorp et al. 2017). Nevertheless, the detailed modelling of the BBL is outside the scope of the present work.

p_{nh} allows to account for wave dispersion with similar accuracy to that of weakly non-linear Boussinesq-type models (Bai et al. 2018). In the cases analysed in this study, the dispersivity parameter, $k_w d$ is lower than 0.5, where k_w is the wave number (defined as $k_w = 2\pi/L$, with L being the local wave length) and d is the still water depth (see

Fig. 1). Therefore, the celerity error in the description of frequency dispersion is of the order of 1% (Bai et al. 2018).

Wave breaking in XBNH is modelled by using the Hydrostatic Front Approximation (HFA) of Smit et al. (2013), in which the non-hydrostatic pressure term is set to 0 when $\frac{\partial \eta}{\partial t} > 0.4c$ (with $c = \sqrt{gh}$ the wave celerity in shallow water). After this condition is reached, waves propagate as hydrostatic bores. The reader is referred to Smit et al. (2010) and McCall (2015) for a full description of the XBNH model.

2.2 Intra-wave sediment transport modelling

In this study, the Pritchard and Hogg (2003) advection equation for the intra-wave suspended sediment transport is included in XBNH:

$$\frac{\partial hC}{\partial t} + \frac{\partial huCS_{sl}}{\partial x} = m_e \left(\frac{\tau_b - \tau_{b,cr}}{\tau_{ref}} \right)^R - w_s C_{nb} = E - D, \quad (9)$$

where C is the depth-averaged suspended sediment concentration; its maximal value, C_{max} , is herein considered the higher physically possible sediment concentration for a fluidised bed and defined as $C_{max} = 1 - n_{p,d}$, with $n_{p,d} = 0.6$, the porosity for a fluidised bed; S_{sl} represents the bed slope effects computed following Deltares (2015):

$$S_{sl} = 1 - \alpha_{sl} \frac{\partial z_b}{\partial x}, \quad (10)$$

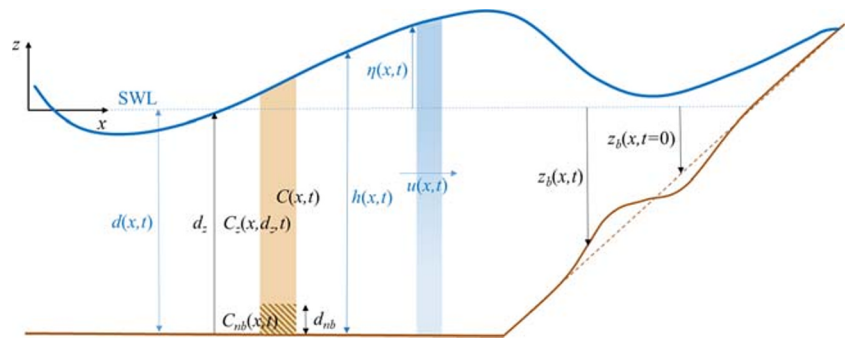
where $\alpha_{sl} = 1.6$ according to Deltares (2015) and z_b is the bed level. Therefore, the suspended sediment transport rate, q_s , is defined as $q_s = huCS_{sl}$. m_e is the mobility parameter, which determines the erodibility of the sediment as suspended load, $\tau_{b,cr}$ is the critical bed shear stress, τ_{ref} is the reference bed shear stress, $R > 0$ is a dimensionless exponent (Pritchard and Hogg 2003), w_s is the sediment settling velocity and C_{nb} is the near-bed suspended sediment concentration at a small near-bed reference height, d_{nb} , above z_b . The two terms on the right side in Eq. (9) represent the erosion rate, E , and the deposition rate, D , respectively. C_{nb} in D is computed as:

$$C_{nb} = CK_C, \quad (11)$$

where the shape factor, K_C , represents the relative importance of sediment settling and mixing. When good mixing is assumed $K_C = 1$. Since the suspension is assumed to be sufficiently diluted, there is no feedback between the suspended sediment and the vertical distribution of turbulence. Therefore, K_C depends only on sediment properties and the depth-averaged hydrodynamics. Consequently:

$$K_C = \frac{(1 - B)}{d'_{nb} \left(d'^{B-1}_{nb} - 1 \right)}, \quad (12)$$

Fig. 1 Schematisation of cross-shore profile and main variables considered, which are explained in the text



where B is the Rouse number defined as:

$$B = \frac{w_s}{\kappa u_*}, \quad (13)$$

where $\kappa = 0.4$ is the von Karman constant and u_* is the friction velocity: $u_* = (\tau_b/\rho)^{1/2}$. d'_{nb} is the dimensionless near-bed reference height, given by a simplified form of Van Rijn formula as shown in Soulsby (1997) with the relationship:

$$d'_{nb} = \frac{d_{nb}}{h} = 0.519 \left(\frac{D_{50}}{\lambda} \right)^{0.3}, \quad (14)$$

in which D_{50} is the median grain diameter, and λ is a reference length scale.

The model described above allows expressing the vertical distribution of suspended sediment by a power-law profile as in Soulsby (1997):

$$C_z(d_z) = C_{nb} \left(\frac{d_z}{d_{nb}} \right)^{-B} \quad \text{in which} \quad d_{nb} \leq d_z \leq h, \quad (15)$$

where d_z is the vertical elevation from z_b (see Fig. 1). The concentration profile described by Eq. (15) corresponds to a linearly increasing eddy diffusivity of the sediment with the height above the bed. Note that C_z is not a model output, but it is herein computed in the aftermath of the numerical simulations.

The bed load transport rate, q_b , is calculated using the equation derived by Meyer-Peter and Müller (1948). The reader is referred to McCall (2015) for the existing implementation of this formula in XBNH, and it is summarised here, following with the main equation:

$$q_b = 8(\theta - \theta_{cr})^{1.5} \sqrt{\Delta g D_{50}^3} \frac{\tau_b}{|\tau_b|} S_{sl}, \quad (16)$$

where θ and θ_{cr} are the Shields and critical Shields parameters, respectively; $\Delta = (\rho_s - \rho)/\rho$, in which ρ_s is the sediment density. θ is computed as $\theta = \tau_b/(\Delta \rho g D_{50})$, and θ_{cr} is given by Soulsby (1997).

The Meyer-Peter and Müller (1948) formula is considered appropriate for the swash zone according to previous studies (see Chardón-Maldonado et al. 2016 among others) and variations of the formula have been tested, for example in Postacchini et al. (2012) for sand and Briganti et al. (2018) for coarse sand. When compared with the original Meyer-Peter and Müller (1948) formula, the Postacchini et al. (2012) formulation showed very similar results in terms of net bed changes (see Briganti et al. 2016). Therefore, in this study we did not test other formulas because of the limited differences in the swash zone shown in the literature.

2.3 Bed-updating modelling

The bed-updating is modelled using the Exner-type equation:

$$(1 - n_p) \frac{\partial z_b}{\partial t} + E - D + \frac{\partial q_b}{\partial x} = 0, \quad (17)$$

where n_p is the bed porosity; E and D are formulated as shown in Eq. (9), and q_b is computed as in Eq. (16).

2.4 Numerical scheme

XBNH uses a staggered grid where depth, water level and sediment concentration are defined in the cells centres, and velocity and sediment flux at the cells interfaces. The hydrodynamic equations are solved by applying a limited version of the McCormack (1969) predictor-corrector scheme, which is second-order accurate where the solution is smooth and reduces to first-order accuracy in proximity of discontinuities. The method is mass and momentum conservative (Smit et al. 2010).

For the sediment transport and bed-updating modelling, a finite volume approach is applied, where upwind approximations are used (Deltares 2015). XBNH uses a dynamically adjusted time step. Thus, a value for the maximum Courant Number, CN, is defined and the program in turn adjusts the time step, Δt , in order to guarantee that $u \Delta t / \Delta x < \text{CN}$, where Δx is the computational grid size. In this study, CN = 0.7 was used.

3 Model verification

In this section, the performance of the hydro-morphodynamic model proposed in this study is verified against the high-resolution numerical solution obtained by Zhu and Dodd (2015), in which an idealised bore generated by a solitary wave over an erodible sloped beach was simulated.

3.1 Zhu and Dodd (2015) model set-up

Figure 2 shows the model domain in Zhu and Dodd (2015). In the region $x < -10$ m the bed is flat, while for $x \geq -10$ m an erodible 1:15 sloped beach is considered. The initial shoreline position is located at $x = 5$ m. The initial conditions of η and u along the cross-shore direction were given by Mei (1989) and the hydrodynamic Riemann condition, respectively. As shown in Fig. 2, at the initial condition, the wave crest is located at $x = -22$ m. The wave height, H , is equal to 0.60 m. The governing equations in Zhu and Dodd (2015) were solved using the Method Of Characteristics (MOC), and the hydrodynamics were solved using the hydrostatic NLSWE, which included bed shear stress. The suspended sediment transport was computed using the Pritchard and Hogg (2003) transport equation, assuming a well-mixed condition (i.e., $K_C = 1$). The bed load was given by the Meyer-Peter and Müller (1948) formula.

3.2 Model set-up and parameters

The model set-up and physical parameters followed closely those used in Zhu and Dodd (2015). Time series of η and u were provided by Zhu and Dodd (2015) at $x_0 = -20$ m, i.e., where the wave does not propagate as a bore. Thus, as shown in Fig. 2, the upstream boundary in the model domain is located at x_0 ; the computational domain extended to $x = 25$ m. $\Delta x = 0.05$ m was chosen. The simulated

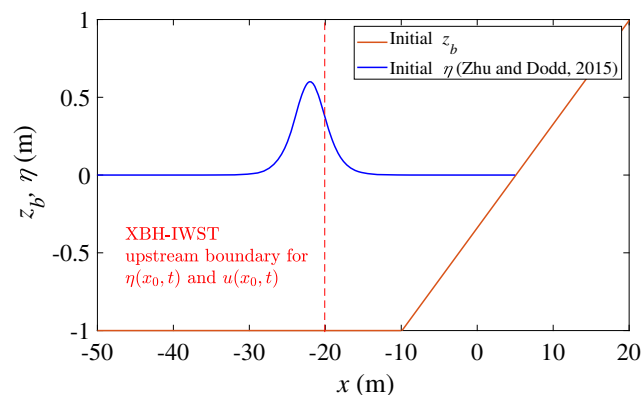


Fig. 2 Model domain and initial condition in Zhu and Dodd (2015) and upstream boundary location in XBH-IWST model domain (red-dashed line)

time was approximately 33 s. Table 1 shows a summary of the main parameters included and conditions assumed in the Pritchard and Hogg (2003) equation. Similarly to Zhu and Dodd (2015), the well-mixed condition was assumed (i.e., $K_C = 1$ was set). Consistently with the cited study, bed slope effects in the computation of q_s and q_b were not taken into account. To compare the response of the model proposed in this study with Zhu and Dodd (2015) in terms of intra-wave sediment transport, the hydrostatic approach was considered by turning off the non-hydrostatic pressure term. This model configuration is herein referred to as XBH-IWST.

3.3 Comparison between model predictions and Zhu and Dodd (2015)

Comparison of model predictions with Zhu and Dodd (2015) for the hydrodynamics is shown in Appendix 2; here, only the modelling of beach morphodynamics is discussed.

Figure 3 shows the final bed profiles, z_{b_f} (a), and the final bed changes, $\Delta z_{b_f} = z_b(t = t_f, x) - z_b(0, x)$ (b); t_f is the time at the end of the simulation. Despite the height of the bed step being underestimated by 20% with respect to Zhu and Dodd (2015), XBH-IWST captures the erosion and deposition well. nRMSE = 0.0085 for Δz_{b_f} and RMSTE = 0.003 m², showing good performances of XBH-IWST in simulating the solution of Zhu and Dodd (2015). Similarly to Briganti et al. (2012), Δz_{b_f} was post-processed by using a moving average. Spurious oscillations are shown in the region $x > 2$ m during the backwash bore, which runs down the beach and generates a sharp deposition at $x \simeq 2$ m. Note that Zhu and Dodd (2015) used a shock-fitting scheme. Increasing Δx by an order of magnitude reduces the oscillations; however, as expected, it was found that the much lower resolution would lead to the underestimation of the height of the backwash step by 50%. While not being the aim of this study, the implementation of a shock-capturing numerical scheme could help overcome this issue.

Table 1 Main parameters and conditions in the Pritchard and Hogg (2003) transport equation

Pritchard and Hogg (2003) equation	
c_f	= 0.01
w_s	= 0.03 m/s
m_e	= 0.002 m/s
$\tau_{b,cr}$	= 0 N/m ²
λ	= 1 m
τ_{ref}	= $\rho c_f u_{ref} u_{ref} $, where $u_{ref} = \sqrt{g\lambda}$
R	= 1
K_C	= 1 (set constant in XBH-IWST; assumption of well-mixing)

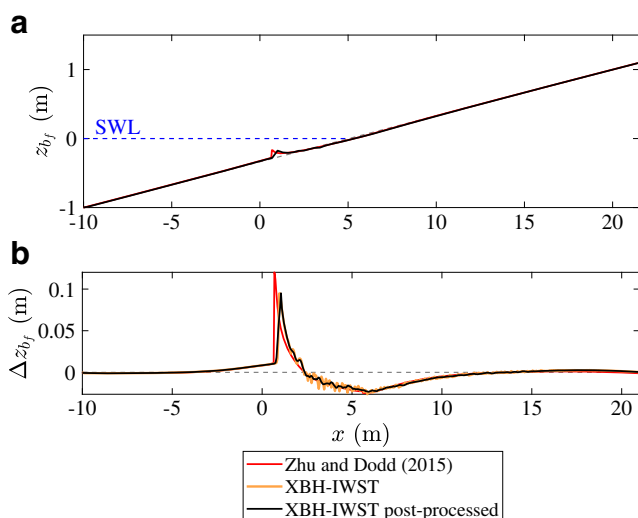


Fig. 3 z_{bf} **a** and Δz_{bf} **b**; reference line: grey-dashed line

Figure 4 shows the time series of C at two different locations along x . The corresponding nRMSE are 0.2142 ($x = 0$ m) and 0.3200 ($x = 5$ m). The high correlation between the predicted C and that computed by Zhu and Dodd (2015) is confirmed by $\rho_{mr} = 0.9922$ ($x = 0$ m) and $\rho_{mr} = 0.9877$ ($x = 5$ m).

4 Numerical modelling of bichromatic wave groups on an intermediate beach

In this section, the performance of XBNH-IWST is assessed against the experiments conducted within the Hydralab IV

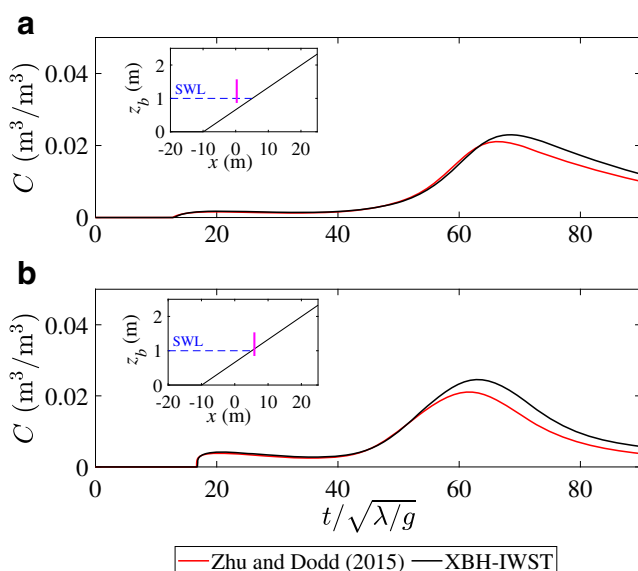


Fig. 4 Time series of C at $x = 0$ m **a** and $x = 5$ m **b**; the two subplots in **a** and **b** show the two cross-shore locations in the model domain, respectively

- CoSSedM (Coupled High Frequency Measurement of Swash Sediment Transport and Morphodynamics) project (see Alsina et al. 2016). The experiments studied the hydro-morphodynamics of bichromatic wave groups on a 1:15 sloped beach built at prototype scale with commercial sand characterised by $D_{50} = 0.25$ mm, $w_s = 0.034$ m/s and $n_p = 0.36$, which showed clearly swash-swash interactions.

Two bichromatic wave group conditions with the same energy content were generated in the flume: BE1.2 (broad-banded wave condition) and BE4.2 (narrow-banded wave condition), respectively, with varying wave group period, T_g , and repeat period, T_r . For BE1.2, $T_g = 15$ s and $T_r = 195$ s, whereas for BE4.2, $T_g = T_r = 27.7$ s (see also Alsina et al. 2018). $T_g = 1/f_g$, where f_g is the group frequency, which is defined as the difference of the primary frequencies, f_1 and f_2 . A summary of the bichromatic wave groups is shown in Table 2, where H_1 and H_2 are the wave heights of the primary components.

For each wave condition, starting from the same initial z_b (1:15 uniform sloped bed), eight successive bichromatic wave sequences, from SEG1 to SEG8, each of 1800 s duration, were generated. Figure 5 shows the initial z_b and the location of the instruments in the wave flume and selected for comparison. Wave Gauges (WG) and Acoustic Wave Gauges (AWG) measured η ; Acoustic Doppler Velocimeters (ADV) measured the local flow velocity. Optical Back-Scattering sensors (OBS) and Conductivity Concentration Measurements (CCM⁺) tanks measured C_z and time-dependent z_b in the swash zone, respectively. d in the horizontal part of the domain was 2.48 m for BE1.2 and 2.46 m for BE4.2.

The beach is classified using the dimensionless settling velocity, Ω , defined as Gourlay and Meulen (1968): $\Omega = H_{rms}/(w_s T_p)$, where H_{rms} is the root-mean-square wave height computed at WG3 (i.e., $H_{rms} = 0.39$ m for BE1.2 and $H_{rms} = 0.40$ m for BE4.2) and $T_p = 1/(f_1 + f_2)/2 = 3.70$ s is the mean primary wave period for both wave conditions. It is computed that $1 < \Omega < 6$, which indicates an intermediate beach.

The reader is referred to Alsina et al. (2016) for a detailed description of the experimental procedure.

Table 2 Bichromatic wave groups for wave conditions BE1.2 and BE4.2

	BE1.2	BE4.2
f_1 (Hz)	0.303	0.288
H_1 (m)	0.30	0.28
f_2 (Hz)	0.237	0.252
H_2 (m)	0.26	0.30
f_g (m)	0.067	0.036

4.1 Model set-up and parameters

The model domain is the same as Ruffini et al. (2020). As shown in Fig. 5, the upstream boundary in the model is located at $x_0 = 30.55$ m, where the WG3 was installed. Thus, the model domain extended from WG3 to the end of the beach, located at $x = 85.05$ m, and like the cited study $\Delta x = 0.1$ m. Time series of η and u , updated as offshore forcing, were the same as those used in Ruffini et al. (2020) as boundary conditions. For the computation of c_f , a slightly lower value of the Manning coefficient, n , than in Ruffini et al. (2020) was used. $n = 0.018$ s/m^{1/3} was calibrated considering the best compromise between the accuracy of maximum run-up and morphological evolution. The value chosen still reflects the characteristics of the considered sandy beach. Model parameters, which are not mentioned herein, were set to their default values defined in Deltares (2015).

The calibration of the sediment transport model in XBNH-IWST was carried out by varying m_e , R and λ . Table 3 summarises the main parameters included and conditions assumed in the Pritchard and Hogg (2003) transport equation. This set of parameters was chosen as it provided the best modelling in the sensitivity analysis shown in Section 4.2.

Only the first two segments, SEG1 and SEG2, were simulated for both BE1.2 and BE4.2 because those segments showed larger morphological changes than the subsequent ones. For BE1.2, the experimental bed evolution reached an equilibrium more rapidly compared with BE4.2. However, SEG1 and SEG2 were far from equilibrium for both cases.

4.2 Sensitivity analysis for the Pritchard and Hogg (2003) transport equation

The sensitivity analysis of the results to the parameters used in the Pritchard and Hogg (2003) transport equation was carried out for SEG1 of BE1.2 wave condition. The aim of the sensitivity analysis is to show the relative effects of these parameters in terms of the modelled C and Δz_{bf} =

$z_b(t = t_f, x) - z_b(0, x)$; t_f is the time at the end of SEG1. The parameters considered are m_e , R and λ . Note that λ also affects τ_{ref} (see Table 3) and K_C following Eqs. (12) and (14). According to Zhu and Dodd (2015), $\tau_{b,cr}$ is not analysed because the effect of a threshold for suspended load is negligible for fine sand; hence, $\tau_{b,cr} = 0$ N/m².

Each parameter is varied by keeping the others to their reference values as in Zhu and Dodd (2015) (i.e., $m_e = 0.002$ m/s, $\lambda = 1$ m and $R = 1$). m_e is the least well-determined parameter, due to the lack of data to provide its estimates. Since $m_e = 0.002$ m/s is found to underestimate both Δz_{bf} and C , the sensitivity analysis for m_e was carried out by increasing it by up to two orders of magnitude with respect to the reference value. $R > 0$ is a numerical parameter and it was increased and decreased with respect to $R = 1$ considering $R = 0.25, 0.5, 1.5$. Values of λ were chosen to be physically representative of the Alsina et al. (2016) configuration. Therefore, $\lambda = H_{rms} = 0.39$ m and $\lambda = d = 2.48$ m at WG3 were selected.

Figure 6 shows the sensitivity analysis for the parameters considered in terms of Δz_{bf} (Fig. 6a, b and c) and C (Fig. 6d, e and f), respectively. The corresponding nRMSE, ρ_{mr} and RMSTE are presented in Table 4. Note that the experimental C was computed as the average of the observed C_z at OBS4 and OBS7, which were located at two different d_z above the initial z_b at AWG7 (OBS4 at $d_z = 0.03$ m and OBS7 at $d_z = 0.08$ m). The OBSs did not measure when the free surface was lower than the instrument sensor. Therefore, the corresponding nRMSE and ρ_{mr} were computed when at least one of the two OBSs was submerged.

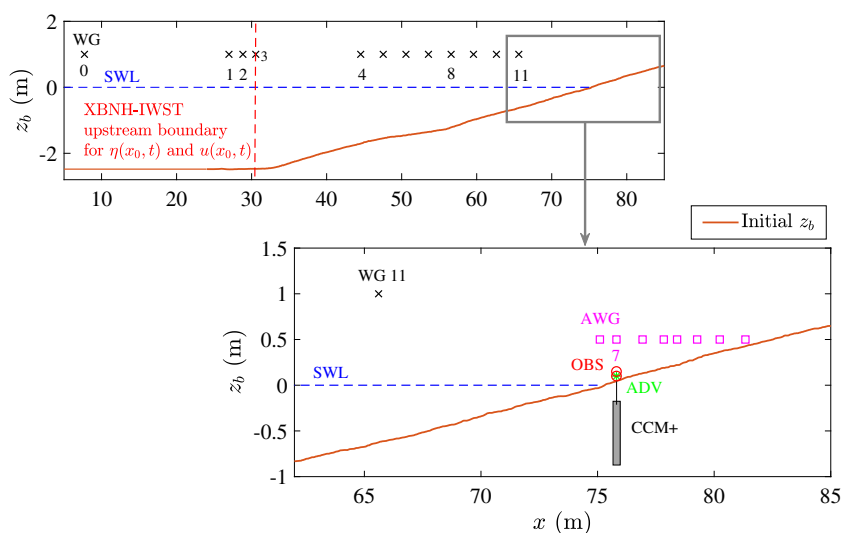
The sensitivity analysis reveals that m_e is the most influencing parameter within the ranges considered for both the predicted C and Δz_{bf} . Variations of λ and R affect C more than Δz_{bf} in terms of nRMSE. By increasing λ or R , C decreases and the nRMSE increases due to the increasing underestimation of C . For both λ and R , the maximum relative difference in terms of nRMSE is 14%. Instead, for m_e , the difference between the maximum and minimum nRMSE is 73%. The sensitivity analysis shows that the variation of the parameters included in the Pritchard and Hogg (2003) model leads to a variability of its peaks and magnitude, as a consequence of the variability of C . However, for all the parameters considered, the low values of ρ_{mr} highlight a poor correlation between the modelled and experimental C . For Δz_{bf} , variations of λ and R lead to negligible differences in terms of the corresponding nRMSE; differences in terms of RMSTE are lower than 0.05% and 0.8% for λ and R , respectively. Δz_{bf} is quantitatively more sensitive to the variation of m_e , with the difference between the maximum and minimum RMSTE being 25%. From a qualitative point of view, XBNH-IWST is able to capture the peak of the accretion in the upper swash zone if m_e is increased by two orders of

Table 3 Main parameters and conditions in the Pritchard and Hogg (2003) transport equation

Pritchard and Hogg (2003) equation

m_e	= 0.01 m/s
$\tau_{b,cr}$	= 0 N/m ²
λ	= Considered wave height at the upstream boundary
τ_{ref}	= $\rho c_{f,ref} u_{ref} u_{ref} $, where $c_{f,ref} = g n^2 / \lambda^{1/3}$ and $u_{ref} = \sqrt{g \lambda}$
R	= 1.5
K_C	≥ 1 (computed by XBNH-IWST)

Fig. 5 Alsina et al. (2016) experimental domain with instrumentation installed and location of upstream boundary location in XBNH-IWST model domain (red-dashed line)



magnitude with respect to the values suggested in Zhu and Dodd (2015). In particular, the predicted erosion pattern in the upper swash region evolves into a deposition one for $m_e \geq 0.05$ m/s. Also, by increasing m_e , the erosion in the lower swash region increases and the peak of deposition in the surf zone moves shoreward.

Different combinations of values for m_e , λ and R were selected within the ranges considered, for the model calibration. Results are shown in Fig. 7 and the corresponding nRMSE, ρ_{mr} and RMSTE are presented in Table 5. Figure 7 shows that by increasing m_e by an order of magnitude with respect to $m_e = 0.002$ m/s, in combination with different

values of λ and R than their reference values, the predicted Δz_{bf} and C (Fig. 7a and b) are qualitatively comparable with those obtained with $m_e \sim 10^{-1}$ m/s and the other parameters set to their reference values. None of the sets of parameters tested allows obtaining a better reproduction of the time history of C . The combination $m_e = 0.01$ m/s, $\lambda = 0.39$ m and $R = 1.5$ was chosen for both the Alsina et al. (2016) and Young et al. (2010) test cases because it allows better capturing the magnitude of the deposition in the upper swash zone and the erosion in the lower swash region. This is confirmed by the corresponding lower RMSTE than the other values tested.

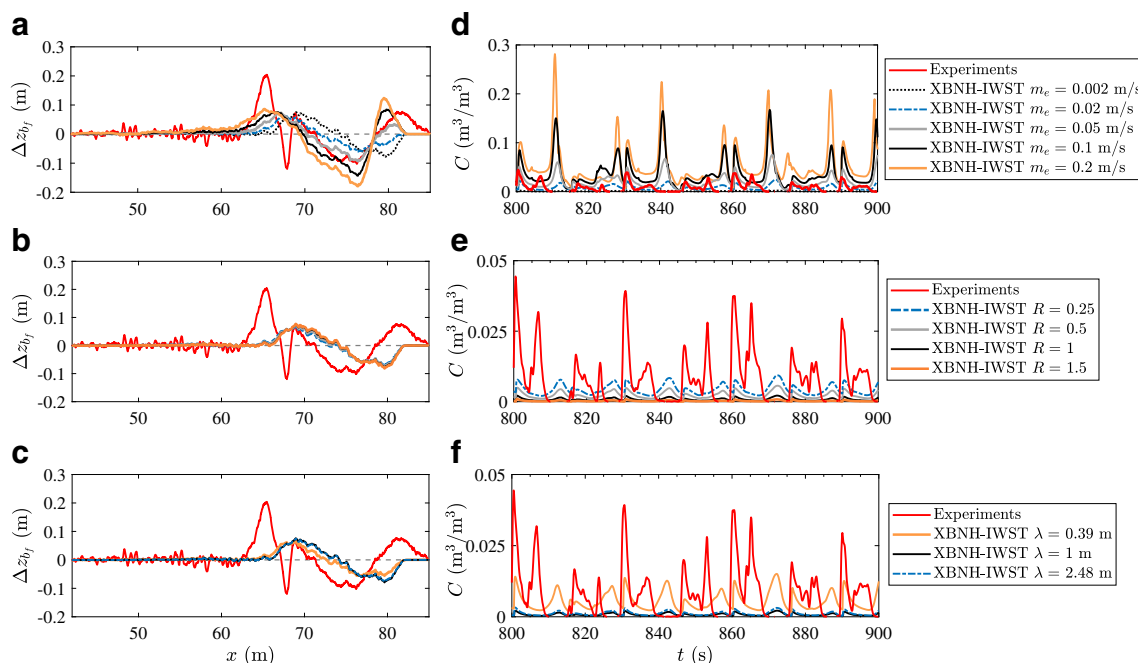


Fig. 6 Δz_{bf} after SEG1 and time series of C over SEG1 for different values of m_e **a** and **d**, R **b** and **e**, and λ **c** and **f** for BE1.2; for each parameter, the others are set to their reference values (i.e., $m_e = 0.002$

m/s, $R = 1$ and $\lambda = 1$ m); reference line: grey dashed line. Note that the scale of the vertical axis in **e** and **f** is an order of magnitude lower than that in **d**

Table 4 nRMSE and ρ_{mr} for C , and nRMSE and RMSTE Δz_{bf} for different values of m_e , R and λ ; note that for each parameter the others are considered to their default values

		m_e (m/s)					R			λ (m)	
		0.002	0.02	0.05	0.1	0.2	0.25	0.5	1.5	0.39	2.48 m
C	nRMSE	1.1385	1.0195	1.7786	3.2594	3.8642	1.0046	1.0696	1.1634	0.9757	1.1204
	ρ_{mr}	0.1319	-0.0784	-0.0997	-0.0688	-0.0532	0.0344	0.0721	0.2164	0.1028	0.1486
Δz_{bf}	nRMSE	0.0580	0.0484	0.0403	0.0397	0.0469	0.0550	0.0565	0.0587	0.0519	0.0574
	RMSTE (m^2)	0.1792	0.1800	0.1876	0.2022	0.2414	0.1932	0.1834	0.1791	0.1802	0.1799

4.3 Comparison between model predictions and observations

The hydrodynamics response of XBNH-IWST is very similar to that presented in Ruffini et al. (2020). For this reason only the nRMSE and ρ_{mr} for η at selected cross-shore locations are shown in Table 6.

Figures 8 and 9a show the variation of H_{rms} along the beach profile during SEG2 for BE1.2 and BE4.2, respectively. For both wave conditions, the model is able to capture the evolution of H_{rms} across the domain. z_{bf} and $\Delta z_{bf} = z_b(t = t_f, x) - z_b(0, x)$ (with t_f being the time at the end of SEG2) are illustrated in Figs. 8 and 9 (b and c, respectively); see Table 7 for the corresponding computed nRMSE and RMSTE. Numerical results show a better performance for BE1.2 than BE4.2, in both the surf and swash zones. This is indicated by the lower nRMSE for BE1.2 compared with BE4.2. For the former, XBNH-IWST can capture the deposition in the upper swash zone and the erosion in the lower swash region, whereas the development of the breaker bar is not accurately simulated for both wave conditions. Consequently, H_{rms} is more underestimated in the shoaling zone for BE4.2 than in BE1.2. Indeed, the experimental results suggest that reflection occurred in the shoaling zone due to the bar; thus, H_{rms} increased more than the predicted one.

The net sediment transport rate, \bar{q}_{sed} , over SEG1 and SEG2 is shown in Figs. 8 and 9d for BE1.2 and BE4.2,

respectively. This was computed using a sediment balance, which was numerically integrated over the x -domain between the start of SEG1 and the end of SEG2:

$$\bar{q}_{sed}(x = x_i) = \bar{q}_{sed}(x = x_{i-1}) - (1 - n_p) \frac{\Delta z_{b_{SEG1-2}} \Delta x}{\Delta t_{SEG1-2}}, \quad (18)$$

where q_{sed} is the instantaneous sediment transport and the bar refers to the averaging over the duration of the two segments, Δt_{SEG1-2} ; the subscript i refers to the i th point along the x -domain for both the numerical mesh and the experimental domain, where z_b is available. Thus, $i = 1, \dots, N$, with $i = 1$ at the onshore boundary of the domain (i.e., landward of the maximum run-up limit), where $q_{sed} = 0$ is assumed, and $i = N$ at the offshore start of the beach. $\Delta z_{b_{SEG1-2}}$ is the difference between z_b at the end of SEG2 and at the start of SEG1. Figure 8 (d) highlights that XBNH-IWST is able to simulate the magnitude of the onshore-directed sediment transport in the upper swash zone and the offshore-directed one in the lower swash region and surf zone up to the crest of the bar, located at $x = 65$ m (see also Appendix 3). For BE4.2, the model can capture the sign of \bar{q}_{sed} up to the bar at $x = 63$ m (Fig. 9d), but the magnitude is underestimated. This might be explained by the more prominent bar observed in BE4.2 than BE1.2, which XBNH-IWST cannot reproduce. Therefore, the exchange of sediment between the swash and surf zones is not well simulated, resulting in a deterioration

Fig. 7 Δz_{bf} a after SEG1 and time series of C b over SEG1 for BE1.2 for different combinations of values of m_e , R and λ ; reference line: grey dashed line

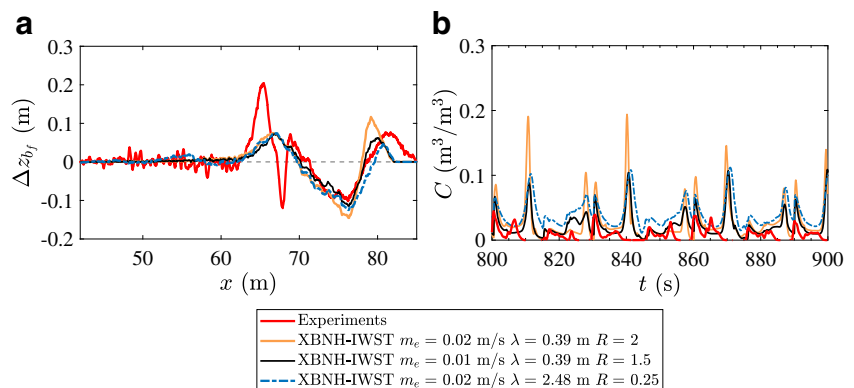


Table 5 nRMSE and ρ_{mr} for C_z , and nRMSE and RMSTE Δz_{bf} for different combinations of values of m_e , R and λ

	m_e (m/s)	0.02	0.01	0.02
	λ (m)	0.39	0.39	2.48
	R	2	1.5	0.25
C_z	nRMSE	2.8873	2.1614	3.0819
	ρ_{mr}	0.0921	-0.0913	-0.1314
Δz_{bf}	nRMSE	0.0418	0.0412	0.0404
	RMSTE (m ²)	0.1896	0.1688	0.2918

in the overall modelling of \bar{q}_{sed} . For both wave conditions, some limitations are visible in the shoaling region and surf zone up to the bar crest, where the experimental onshore-directed \bar{q}_{sed} is not predicted by the model. Indeed, when the experimental \bar{q}_{sed} changes in sign, the modelled one continues being negative for both wave conditions. Note that for BE4.2 the observed \bar{q}_{sed} goes to zero at the offshore boundary, which is not shown in Fig. 9d. However, the positive and quasi-uniform value of the observed \bar{q}_{sed} in the shoaling zone is most likely affected by measurement effects due to the mechanical wheel profiler used to measure the bed level. This instrument has a wheel that is too large to detect individual ripples. Therefore, the change in the bed level is below the sensitivity of the instrument. Moreover, the modelled θ at the offshore side of the bar is larger than θ_{cr} for the most part of the event.

A detailed analysis of the local sediment transport dynamics within SEG2 at AWG7 ($x = 75.81$ m) is shown in Figs. 10 and 11 for BE1.2 and BE4.2, respectively. Note that the observed u is a local measurement and herein assumed depth-uniform. The experimental time-dependent z_b recorded by the CCM+ tank at the same x was used to compute C_z for XBNH-IWST with Eq. (15). For BE1.2, only two groups are selected from the sequence of groups within T_r over SEG2. Figure 10b and c show the time series of C_z for both the model and observations at OBS4 and OBS7, respectively. Results show that the initial peak of the intra-wave C_z corresponding to the first bore of both groups (at $t/T_r \simeq 0.005$ and $t/T_r \simeq 0.084$, respectively) is captured by XBNH-IWST, as well

Table 6 nRMSE and ρ_{mr} for η at three locations: WG4 ($x = 44.54$ m), WG8 ($x = 56.59$) and AWG7 ($x = 75.81$ m), for wave conditions BE1.2 and BE4.2

	nRMSE		ρ_{mr}	
	BE1.2	BE4.2	BE1.2	BE4.2
WG4	0.3427	0.2935	0.9434	0.9047
WG8	0.3703	0.3480	0.9319	0.7091
AWG7	0.6343	0.4928	0.8492	0.7387

as the order of magnitude of C_z corresponding to the peaks of u . However, the correlation between the predicted and observed C_z is affected by the underestimation of C_z close to flow reversal, as confirmed by the corresponding nRMSE and ρ_{mr} , shown in Table 7, which reflect a lower performance of XBNH-IWST compared with the hydrodynamics modelling. Figure 10d shows the modelled q_s and q_b ; q_s being always higher than q_b . In the broad-banded wave condition, large backwashes are allowed to develop. Consequently, the suspension of sediment particles is dominant with respect to the sediments settling.

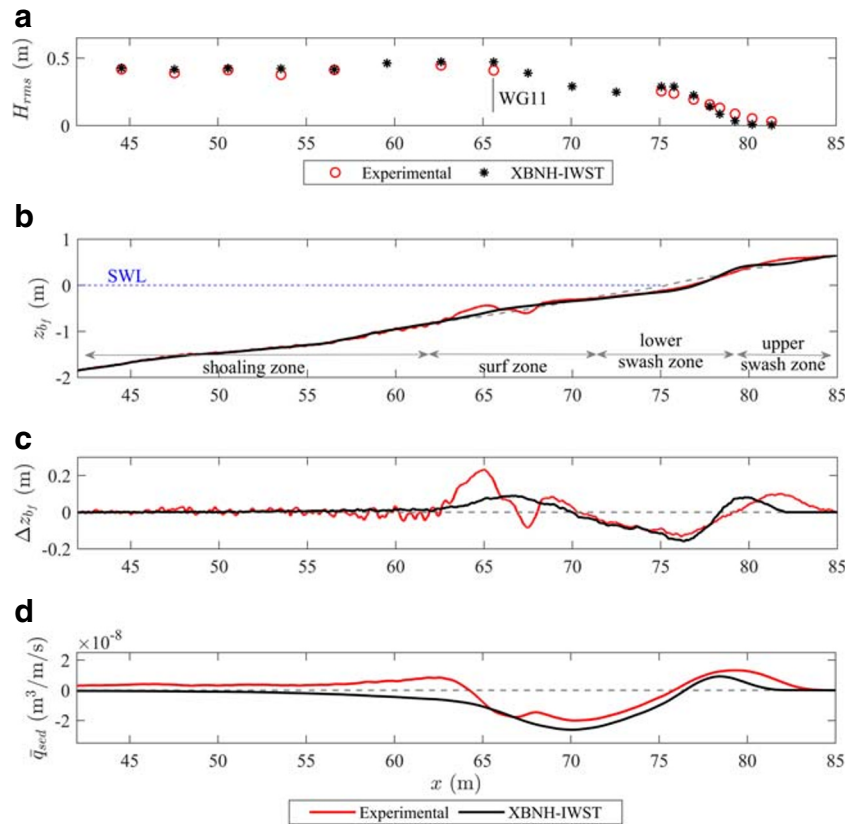
BE4.2 allows analysis of results within one group over SEG2, since $T_r = T_g$. Note that the observed u was filtered with a low-pass filter (cut-off frequency set to 3 Hz) to remove the noise in the measurements. Similarly to BE1.2, XBNH-IWST is able to capture the order of magnitude of the observed C_z after the first event due to swash-swash interactions present in the group at OBS4, whereas, except for the first uprush within the group, C_z is underestimated at OBS7 (Fig. 11b and c, respectively). The peak in the modelled C_z corresponding to the first wave (at $t/T_r \simeq 0.095$) might be the result of a larger bore-induced advection than observations. The lower model performance for BE4.4 than BE1.2 is reflected by the higher nRMSE for C_z , while the values of ρ_{mr} are of the same order of magnitude of those for the broad-banded wave condition (see Table 7). In BE4.2, a higher number of swash-swash interactions occurred within the group than in BE1.2. Therefore, backwashes corresponding to subsequent events were allowed to develop for a shorter duration compared with the broad-banded wave condition. Consequently, the observed and predicted C_z are lower and the difference between the modelled q_s and q_b (Fig. 11d) is smaller than in BE1.2. Indeed, $q_b > q_s$ during the backwash events within the group.

5 Numerical modelling of consecutive non-interacting solitary waves over a sloped beach

In this section, the performance of XBNH-IWST is further tested against the experiments of an erodible sloped beach exposed to nine consecutive non-interacting solitary waves presented in Young et al. (2010). Similarly to Zhu and Dodd (2015), this case allows an individual swash event and the evolution of the beach to be examined without the presence of swash-swash interactions occurring in wave groups.

Figure 12 shows the experimental set-up and the location of the instrumentation installed in Young et al. (2010) and considered for comparison in this study. For η , WG8 ($x = 23$ m) and the Distance Sonic, DS2 ($x = 29$ m) sensors were considered. For u , ADV8 ($x = 23$ m) and ADV5 ($x =$

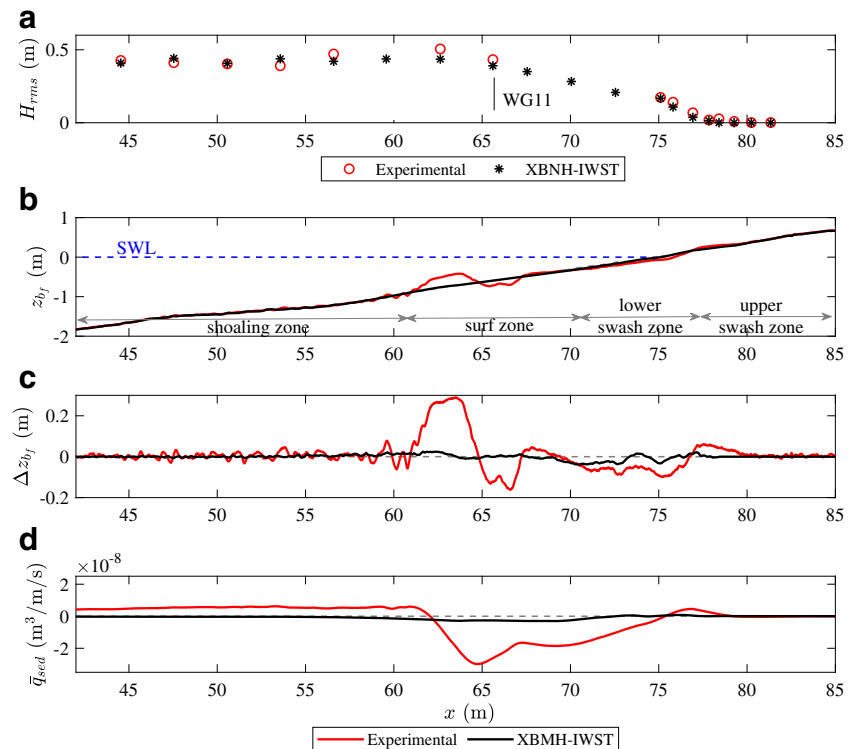
Fig. 8 Cross-shore profile of H_{rms} **a** over SEG2; z_{bf} **b** and Δz_{bf} **c** after SEG2; \bar{q}_{sed} over SEG1 and SEG2 **d** for BE1.2; reference line: grey dashed line



29 m), sensors were selected. For the suspended sediment concentration, OBS3 and OBS4 sensors were considered ($x = 23$ m). The OBS3 and OBS4 sensors recorded C_z at

two different d_z from the initial z_b (OBS3 at $d_z = 0.19$ m and OBS4 at $d_z = 0.09$ m). The initial z_b is a wave-modified 1:15 sloped beach, made of well-sorted sand with $D_{50} =$

Fig. 9 Cross-shore profile of H_{rms} **a** over SEG2; z_{bf} **b** and Δz_{bf} **c** after SEG2; \bar{q}_{sed} over SEG1 and SEG2 **d** for BE4.2; reference line: grey dashed line



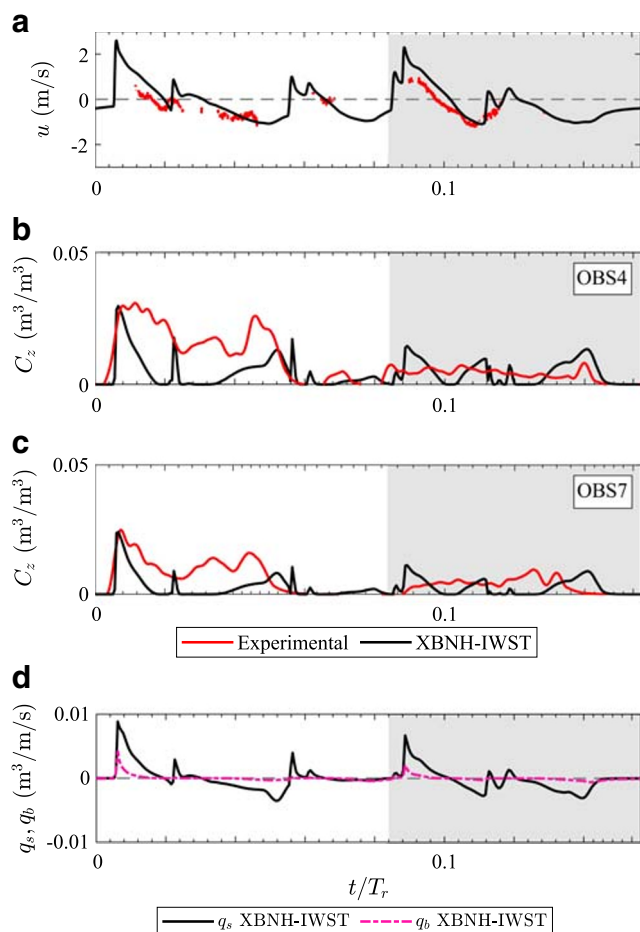


Fig. 10 Time series of flow and sediment transport variables at AWG7 over SEG2 for BE1.2: **a**: u ; **b**: C_z at OBS4; **c**: C_z at OBS7; **d**: q_s and q_b ; the shaded area distinguishes the two wave groups; reference line: grey dashed line

0.2 mm and $n_p = 0.4$. This configuration was the result of previous runs on the nominal 1:15 sloped z_b , such that it can be considered as a near-equilibrium profile beach state.

5.1 Model set-up and parameters

The model domain was set up following the experimental settings, described in detail in Young et al. (2010). The computational domain was $x_0 = 0 \leq x \leq 40$ m and $\Delta x = 0.05$ m. The initial wave-modified z_b was used as the initial z_b in the simulations. As shown in Fig. 12, time series of η and u were updated at the upstream boundary located at x_0 , and were given by Titov and Synolakis (1995), considering a solitary wave over the initial $d = 1$ m:

$$\eta(x_0, t) = H \operatorname{sech}^2 \left[\sqrt{\frac{3H}{4d^3}} (ct - x_0) \right], \quad (19)$$

where $H = 0.60$ m and u is:

$$u(x_0, t) = \eta(x_0, t) \sqrt{\frac{g}{h}}. \quad (20)$$

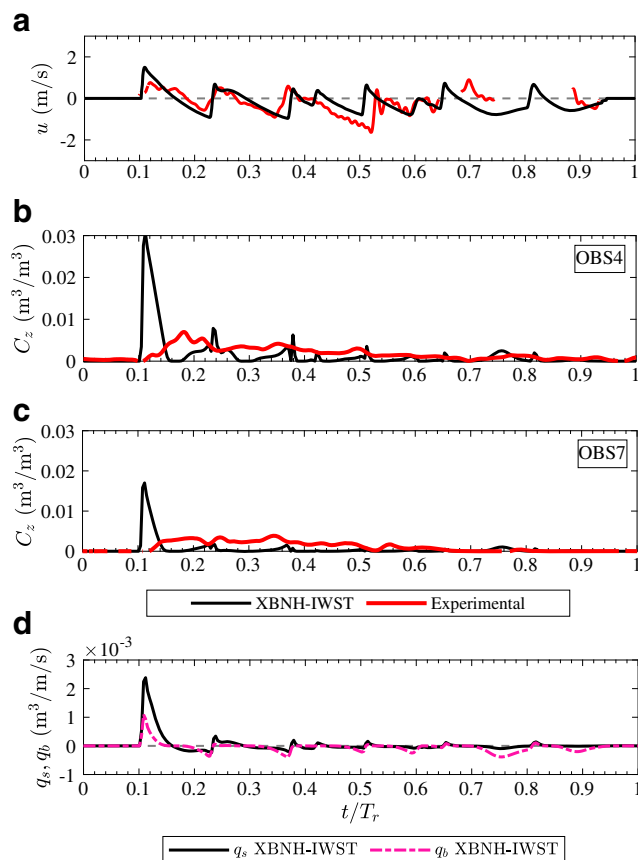


Fig. 11 Time series of flow and sediment transport variables at AWG7 over SEG2 for BE4.2: **a**: u ; **b**: C_z at OBS4; **c**: C_z at OBS7; **d**: q_s and q_b ; reference line: grey dashed line

Moreover, to be consistent with the observations, a reflection was taken into account at the upstream boundary. The sediment transport model was set up similarly to the Alsina et al. (2016) test case (see Table 3), with $\lambda = H$. c_f was modelled using $n = 0.025$ s/m^{1/3}, which was chosen matching the simulated maximum run up with the observations. The maximum excursion point was observed at $x = 38.5$ m. Parameters that were not mentioned in this study were set to their default values defined in Deltares (2015). Numerical simulations were performed for the first three waves of the nine experimental runs. Following the

Table 7 Values of nRMSE, RMSTE and ρ_{mr} for Δz_{bf} and H_{rms} along x , u and C_z at $x = 75.81$ m for wave conditions BE1.2 and BE4.2

	BE1.2	BE4.2	BE1.2	BE4.2	BE1.2	BE4.2
	nRMSE		ρ_{mr}		RMSTE (m ²)	
Δz_{bf}	0.0464	0.0712			0.4078	0.3217
H_{rms}	0.2402	0.3005				
u	0.5706	0.8526	0.6443	0.5103		
C_z (OBS4)	1.0665	3.0683	0.3319	0.3033		
C_z (OBS7)	1.0805	2.4130	0.2521	0.2148		

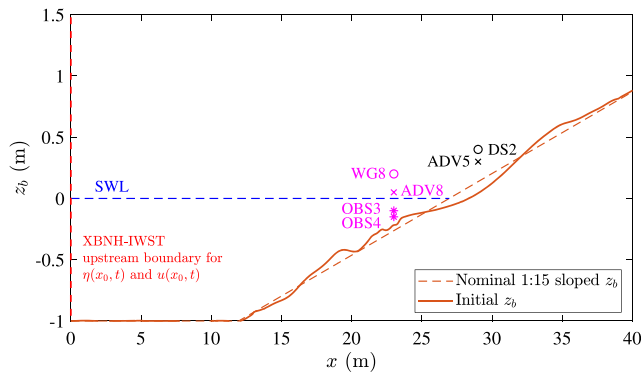


Fig. 12 Young et al. (2010) experimental set-up with instruments installed and location of the upstream boundary in XBNH-IWST model domain (red dashed line)

experimental procedures, the simulated time for each wave was 900 s, in order to allow the water to calm.

5.2 Comparison between model predictions and observations

Figure 13 shows the numerical and experimental time series of η and u within one wave at selected x . In general, XBNH-IWST is able to capture the hydrodynamics. However, a shift of 4 s in the prediction of the reflected wave due to the finite size of the flume is also visible, which affects the corresponding nRMSE and ρ_{mr} (see Table 8). At WG8 (Fig. 13a), the average overestimation of η after the wave run-down, including the reflected wave (i.e., for $t > 22$ s), is equal to 8%. Comparison at ADV5 (Fig. 13d) is affected by some noise in the collected signal at $t = 10$ s and when the water level dropped down the sensor ($17 < t < 37$ s); hence, no signal was recorded.

Figure 14 shows z_{bf} (a) and Δz_{bf} (b) after 3 waves ($z_{bf} = z_b(x, t_f)$, with t_f = time at the end of the third run). Despite the overestimation of the deposition in the upper swash zone and the erosion in the lower swash region for $x > 30.5$ m, XBNH-IWST is able to reproduce the observed

Table 8 Values of nRMSE and ρ_{mr} for η , u and C at selected positions and Δz_{bf} along x , and RMSTE for Δz_{bf}

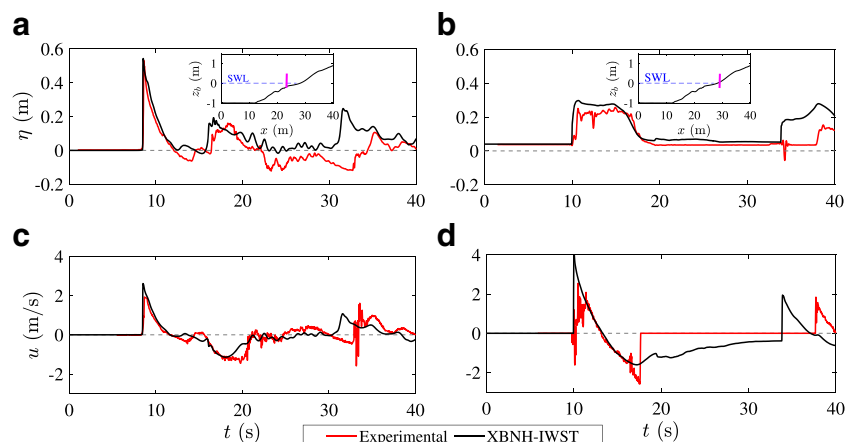
			nRMSE	ρ_{mr}	RMSTE (m ²)
1 wave	WG8	η	1.1839	0.5612	
	ADV8	u	0.7095	0.7465	
	DS2	η	0.9819	0.7642	
	ADV5	u	1.4419	0.4609	
	OBS3-4	C	5.7473	0.5296	
3 waves		Δz_{bf}	0.0227		0.0866

erosion and deposition patterns. From a quantitative point of view, this is confirmed by the corresponding nRMSE and RMSTE, which are shown in Table 8.

An analysis of the intra-wave sediment transport within one wave is shown in Fig. 15 for $x = 23$ m. Time series of C are shown in Fig. 15b. Note that the experimental C was computed as the average of the observed C_z at OBS3 and OBS4. The corresponding computed nRMSE and ρ_{mr} are shown in Table 8. Numerical results show that the largest peak of C corresponds to the backwash phase of the flow (Fig. 15a) (at $t \simeq 20$ s). According to Young et al. (2010), the large peak of C observed between $t = 20$ s and $t = 25$ s was possibly due to the dispersion of sediment generated by the hydraulic jump observed during the experiments at $x = 24$ m.

Time series of the modelled q_s and q_b are shown in Fig. 15c. At the early stage of the uprush $q_b \simeq q_s$. This is consistent with the observations, where the experimental C is almost zero in the uprush, which means that sediment motion mainly occurred as near-bed sediment transport. The reason might be addressed by the location of the OBS sensors, which was seaward of the wave plunging point. As the stirred up sediments are entrained in the water column, the contribution of the modelled q_s also increases. Close to flow reversal, sediment settling occurs and both predicted q_s and q_b decrease. During the backwash, q_b and q_s increase until $q_s > q_b$ in the stage of the run-down.

Fig. 13 Time series of η and u at two representative locations: WG8 and ADV8, $x = 23$ m a and c; DS2 and ADV5, $x = 29$ m b and d; reference line: grey-dashed line. The two subplots in a and b show the cross-shore location of the sensors in the model domain, respectively



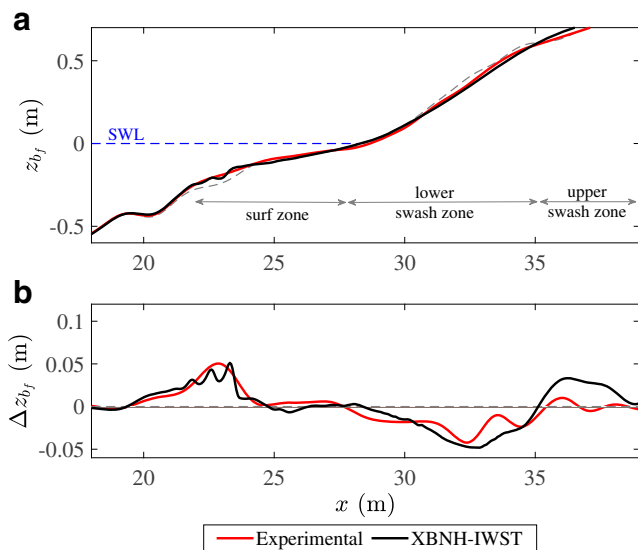


Fig. 14 z_{bf} **a** and Δz_{bf} **b** after 3 waves; reference line: grey-dashed line

6 Discussion

First, the XBNH-IWST modelling of sediment transport and morphodynamics is discussed by comparing the results of numerical simulations of the Alsina et al. (2016) case obtained in the present study with those of Ruffini et al. (2020) using the XBNH-WAST approach. Figure 16 shows the XBNH-IWST and XBNH-WAST predictions for SEG2, with a focus on the swash zone for BE1.2 and BE4.2, respectively. Comparison between the modelled and experimental C is shown in Fig. 16d and h and the corresponding nRMSE, ρ_{mr} and RMSTE are presented in Table 9. The accuracy of XBNH-IWST in the prediction of C in terms of nRMSE and ρ_{mr} is similar to that of XBNH-WAST (see Table 9). XBNH-ISWT, however, is able to better describe the sediment suspension observed after the first bore generated by swash-swash interactions within the group and C close to flow reversal. Also, the accuracy of XBNH-IWST in terms of nRMSE and ρ_{mr} is higher when the comparison is carried out for C_z (see also Table 7).

Differences in the predictions of C for the two approaches lead, in turn, to differences in the simulated Δz_{bf} (Fig. 16a and e). XBNH-IWST shows a better performance in the prediction of Δz_{bf} than XBNH-WAST; for BE1.2, the RMSTE of the former approach is lower by 21% than that of the latter one, while for BE4.2 the difference is 10%. XBNH-IWST better simulates the deposition in the upper swash zone and the erosion in the lower swash region. In fact, Δz_{bf} predicted with XBNH-WAST diverges from observations, especially in the upper swash zone. This might be explained by the behaviour of the sediment transport model in XBNH-IWST near flow reversal

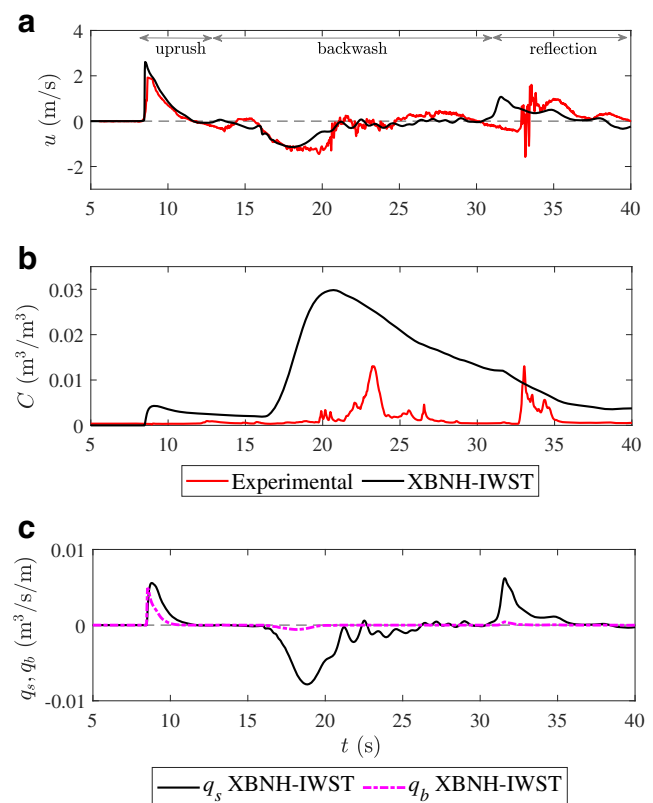


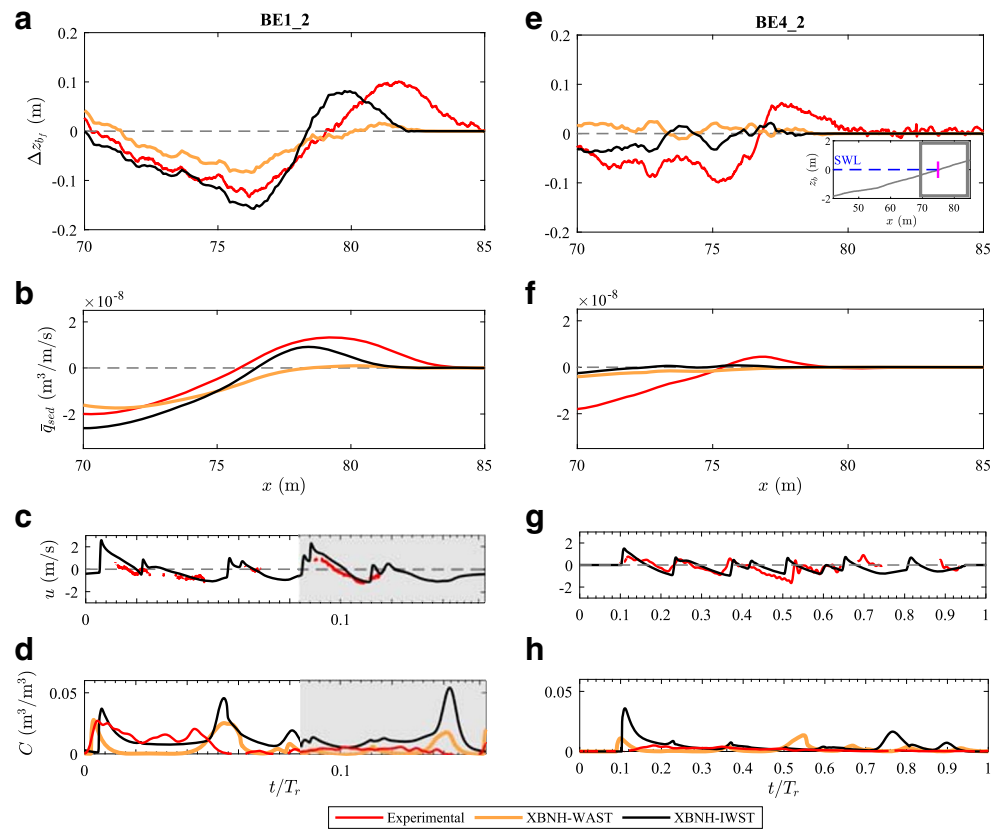
Fig. 15 Time series of u **a**, C **b**, q_s and q_b **c** at $x = 23$ m; reference line: grey dashed line

(i.e., $u = 0$ m/s), when sediment particles are allowed to settle. The better performance of the present approach is confirmed by the modelling of \bar{q}_{sed} (Fig. 16b and f). Unlike the model proposed in this study, XBNH-WAST does not capture the sign of \bar{q}_{sed} in the upper swash zone.

For the Young et al. (2010) experiments, the predicted Δz_{bf} shows lower nRMSE and RMSTE than for the Alsina et al. (2016) case (see Table 8) by 60%, and by an order of magnitude respectively. Regarding the intra-wave sediment transport, the experimental C was obtained by averaging the measurements performed by OBS3 and OBS4 in the surf zone, where, as indicated in Young et al. (2010), C_z was observed to vary a lot along the depth. Therefore, discrepancies between observations and numerical predictions are due to some limitations of the model performance, but uncertainty in the comparison exists because of the low resolution of the measurements.

For both the simulated laboratory experiments, the performance of the Meyer-Peter and Müller (1948) formulation is consistent with results of previous studies (e.g., Xiao et al. 2010 and Postacchini et al. 2012). The modelled θ for Young et al. (2010) at $x = 23$ m is higher than θ_{cr} for almost the whole duration of both the uprush and backwash events (with maximum values of approximately 15 and 4, respectively).

Fig. 16 Comparison between XBNH-IWST and XBNH-WAST (Ruffini et al. 2020) results. Δz_{bf} **a, e**; \bar{q}_{sed} **b, f**; time series of u **c, g** and C **d, h** at $x = 75.81$ m for BE1_2 and BE4_2, respectively; reference line: grey dashed line; the shaded area distinguishes the two wave groups; the subplot in **e** indicates the location of the results shown in the main plots along the domain



A note of caution should be provided regarding the parameters of the Pritchard and Hogg (2003) transport equation. The sensitivity analysis presented in Section 4.2 showed that m_e is the parameter that mostly influences the prediction of Δz_{bf} and C (see Table 4 and Fig. 6). However, because no field data are available to provide its estimates, the only comparisons with the findings of the present study are previous numerical studies, such that of Zhu and Dodd (2015). The value of m_e that showed best modelling in this study is an order of magnitude larger than that used by the cited study for a single solitary wave when a well-mixed condition is assumed (i.e., $K_C = 1$). The optimal m_e found was used in combination with $R = 1.5$ (R being an arbitrary numerical parameter), λ equal to the considered wave height at the upstream boundary, and by considering $K_C \geq 1$. To simplify the choice of the values corresponding to the parameters considered in the Pritchard and Hogg (2003) expression, $\tau_{b,cr}$ was set equal to 0. This choice was justified following Zhu and Dodd (2015) who pointed out that the effect of a threshold for suspended load is not significant for sandy beach morphodynamics. λ is an arbitrary length scale, which in turn, affects the other scale parameter, τ_{ref} . Therefore, representative values of λ were selected for the model calibration (see Section 4.2). τ_{ref} was computed similarly to Zhu and Dodd (2015) for all the simulations carried out.

Although the proposed parameter set allows obtaining a lower RMSTE and a better prediction of erosion and deposition patterns than the other combinations tested, the prediction of C is still inaccurate in XBNH-ISWT as well as the process of bar formation, indicating the need of explicitly modelling further important physical processes. The missing explicit representations of processes such as wave breaking-induced turbulence in the HFA model, phasing effects of the velocity in the BBL, such as the earlier flow reversal near the bottom with respect to the rest of the water column in the swash zone (see e.g., Zhang and Liu 2008), are certainly factors that concur to this inaccuracy.

Table 9 RMSTE for Δz_{bf} along the swash zone, and nRMSE and ρ_{mr} for C at $x = 75.81$ m for BE1_2 and BE4_2, respectively; comparison between XBNH-IWST and XBNH-WAST (Ruffini et al. 2020 results)

	BE1_2		BE4_2	
	XBNH-IWST	XBNH-WAST	XBNH-IWST	XBNH-WAST
nRMSE				
C	1.3333	1.2906	5.9385	2.3647
ρ_{mr}				
	0.0785	−0.1005	0.2696	−0.1405
RMSTE (m²)				
Δz_{bf}	0.1669	0.2089	0.0675	0.0755

7 Conclusions

In this study, the implementation of the Pritchard and Hogg (2003) intra-wave sediment transport equation in XBNH was presented, together with the verification of the model against a high-resolution numerical solution. A sensitivity analysis allowed choosing the set of parameters included in the Pritchard and Hogg (2003) equation that provided the best modelling and the performance of the resulting model was assessed with two laboratory test cases.

Verification of XBH-IWST against Zhu and Dodd (2015) highlighted that the Pritchard and Hogg (2003) transport equation performs qualitatively and quantitatively well when compared with a high-resolution numerical solution of NLSWE. Therefore, this modelling approach is suitable for solving the intra-swash sediment transport in the context of wave-resolving models.

Numerical simulations of the Alsina et al. (2016) and Young et al. (2010) laboratory experiments showed that XBNH-IWST is able to simulate the beach evolution driven by isolated waves, whereas the exchange of sediments between the swash and surf zones under wave trains is not accurately predicted yet. The sediment transport modelling approach herein used is able to improve the simulation of the intra-swash sediment transport within XBNH, especially in terms of C at flow reversal, and in turn, the prediction of the beach accretion in the upper swash zone for the Alsina et al. (2016) case. However, it is not sufficient to accurately capture the mutual feedback between the swash and surf zones when swash-swash interactions are present.

In evaluating the comparisons with the laboratory data, consideration was given to the associated uncertainty. In the Alsina et al. (2016) experiments, a state of the art measurement system was used with high resolution in space and time for the suspended sediment transport. The OBS sensors inevitably provide low-resolution data in the water column. On the other hand, the previous Young et al. (2010) experiments were conducted with fewer instruments. This provides limited resolution for the data. High-resolution experiments of solitary waves on mobile bed are particularly valuable because the intra-wave dynamics could be investigated in depth. Therefore, such experiments are highly recommended for future studies.

At present, there are still limitations in the qualitative and quantitative representation of the morphodynamics and sediment transport with XBNH-IWST. The inclusion of the wave-resolving Pritchard and Hogg (2003) sediment transport equation in XBNH represents a first step to improve the morphodynamics prediction of the model in the context of sandy beaches evolution. Future work is necessary for an accurate prediction of the mutual feedback between the surf and swash zones. Further work will be addressed to the improvement of the intra-wave sediment transport

modelling within XBNH-IWST. Additional physical processes, such as BBL effects and turbulence, and the inclusion of the vertical structure of sediment concentration and flow, need to be included in a formulation suitable for the class of models at hand. A simplified wave breaking-induced turbulence model, similar to those used by Alsina et al. (2009) and Reniers et al. (2013), could be considered to take into account the turbulence diffusion in the computation of $C(z)$ and, in turn, in the prediction of C with XBNH-IWST.

Notation

Symbols

$A_{b,s}$	(-)	Bed load and suspended load coefficients
B	(-)	Rouse number
c	(L/T)	Wave celerity
C	(L ³ /L ³)	Depth-averaged suspended sediment concentration
c_f	(L/T)	Dimensionless friction coefficient
$c_{f,ref}$	(L/T)	Reference dimensionless friction coefficient
C_{eq}	(L ³ /L ³)	Total equilibrium concentration
$C_{eq,b,s}$	(L ³ /L ³)	Bed load and suspended load equilibrium concentrations
C_{max}	(L ³ /L ³)	Maximum sediment concentration
C_{nb}	(L ³ /L ³)	Near-bed suspended sediment concentration
C_z	(L ³ /L ³)	Parametric vertical sediment concentration
d	(L)	Still water depth
D	(L/T)	Deposition rate
d_{nb}	(L)	Near-bed reference height
d'_{nb}	(L)	Dimensionless near-bed reference height
d_z	(L)	Vertical distance above the bed
D_{50}	(L)	Median grain diameter
E	(L/T)	Erosion rate
f_g	(T ⁻¹)	Wave group frequency
f_1	(T ⁻¹)	First component primary wave frequency
f_2	(T ⁻¹)	Second component primary wave frequency
Fr	(-)	Froude number
g	(L/T ²)	Gravity acceleration constant
h	(L)	Total water depth
H	(L)	Wave height
H_{rms}	(L)	Root-mean-square wave height
H_1	(L)	First component primary wave height
H_2	(L)	Second component primary wave height

K_C	(-)	Shape factor	Δt	(T)	Computational time interval
k_w	(-)	Wave number	Δt_{SEG2}	(T)	Duration of SEG2
L	(L)	Wave length	Δx	(L)	Computational x -grid size
m_e	(-)	Mobility parameter	Δz_b	(L)	Bed changes
n	(-)	Manning coefficient	Δz_{bf}	(L)	Final bed changes
n_p	(-)	Bed porosity	$\Delta z_{b_{SEG2}}$	(L)	Difference between final and initial bed level of SEG2
$n_{p,d}$	(-)	Bed porosity for a fluidised bed			
N	(-)	Number of samples	η	(L)	Water surface elevation
p_{nh}	(L/T ²)	Normalised depth-averaged dynamic pressure	θ	(-)	Shields parameter
Q	(L ²)	Sediment volume in RMSTE	θ_{cr}	(-)	Critical Shields parameter
q_b	(L ³ /L/T)	Sediment transport rate for bed load	κ	(-)	von Karman constant
q_s	(L ³ /L/T)	Sediment transport rate for suspended load	λ	(L)	Reference length scale
q_{sed}	(L ³ /L/T)	Instantaneous sediment transport rate	ν_h	(-)	Horizontal viscosity
q_{tot}	(L ³ /L/T)	Total sediment transport rate	ρ	(M/L ³)	Water density
$q_{tot,mean}$	(L ³ /L/T)	Wave-averaged total sediment transport rate	ρ_{mr}	(-)	Pearson's cross-correlation coefficient
R	(-)	Exponent in Pritchard and Hogg (2003)	ρ_s	(M/L ³)	Sediment density
s_{ym}	(-)	Standard deviation of the modelled quantity	τ_b	(M/L/T ²)	Total bed shear stress
s_{yref}	(-)	Standard deviation of the reference quantity	$\tau_{b,cr}$	(M/L/T ²)	Critical bed shear stress
S_{sl}	(-)	Bed slope effects term	τ_{ref}	(M/L/T ²)	Reference bed shear stress
t	(T)	Time	ϕ	(-)	Generic mathematical function
t_f	(T)	Final time	Ω	(-)	Dimensionless settling velocity
T_g	(T)	Wave group period	Abbreviations		
T_p	(T)	Mean primary wave period	ADV		Acoustic Doppler Velocimeter
T_r	(T)	Repeat period	AWG		Acoustic Wave Gauge
T_s	(T)	Adaptation time	BBL		Bottom Boundary Layer
u	(L/T)	Depth-averaged cross-shore velocity	BE1_2		Broad-banded wave condition
u_{mean}	(L/T)	Wave-averaged, depth-averaged cross-shore velocity	BE4_2		Narrow-banded wave condition
u_{ref}	(L/T)	Reference scale velocity	CCM+		Conductivity Concentration Measurements
u_{rms}	(L/T)	Orbital wave velocity	CN		Courant Number
u_*	(L/T)	Friction velocity	HFA		Hydrostatic Front Approximation
w_s	(L/T)	Sediment settling velocity	IWST		Intra-Wave Sediment Transport
x	(L)	Cross-shore coordinate	MOC		Method Of Characteristics
x_0	(L)	Model upstream boundary cross-shore location	NLSWE		Non-Linear Shallow Water Equations
y_m	(-)	Modelled quantity	nRMSE		normalised Root-Mean-Square Error
y_{ref}	(-)	Reference quantity	OBS		Optical Back-Scattering Sensor
z	(L)	Vertical coordinate	RMSTE		Root-Mean-Square Transport Error
z_b	(L)	Bed level	SEG		Segment
z_{bf}	(L)	Final bed level	WG		Wave Gauge
$z_{bf,m}$	(L)	Modelled final bed level in RMSTE	WAST		Wave-Averaged Sediment Transport
$z_{bf,ref}$	(L)	Reference final bed level in RMSTE	XBNH		Non-Hydrostatic XBeach
α_{sl}	(-)	Calibration coefficient for bed slope effects	1D		One-dimensional
Δ	(-)	Relative density			

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Appendix 1: Sediment transport modelling in XBNH-WAST

In XBNH-WAST, the advection equation for the sediment transport is formulated as:

$$\frac{\partial hC}{\partial t} + \frac{\partial huC}{\partial x} = \frac{hC_{eq} - hC}{T_s} = E - D, \quad (21)$$

where T_s is the adaptation time, which represents the entrainment of the sediment, depending on h and w_s , and C_{eq} is the total equilibrium sediment concentration. XBNH-WAST calculates the equilibrium concentration using the the Van Rijn et al. (2007), Van Thiel de Vries (2008) formulations. For both the bed load and the suspended load, referred to as b and s , respectively, the equilibrium

concentrations are expressed in function (“ ϕ ”) of u and the wave orbital velocity, u_{rms} , as:

$$C_{eq,b,s} = A_{b,s}\phi(u, u_{rms}), \quad (22)$$

where $A_{b,s}$ represents, alternatively, the bed load and suspended load coefficients, depending on sediments' grain size and flow properties. The Van Rijn et al. (2007) and Van Thiel de Vries (2008) sediment transport formulations were originally developed for the wave-averaged version of XBeach, where u represents the wave-averaged cross-shore flow velocity, computed by means of NLSWE, and u_{rms} is computed as a parameterisation of the short-wave energy (Roelvink et al. 2009). XBNH solves the intra-wave flow through the extended NLSWE, and the total intra-wave cross-shore velocity is included in the term “ u .” Consequently, in XBNH-WAST, the term “ u_{rms} ” in Eq. (22) is equal to 0. For a more detailed implementation of XBNH-WAST, the reader is referred to Deltares (2015).

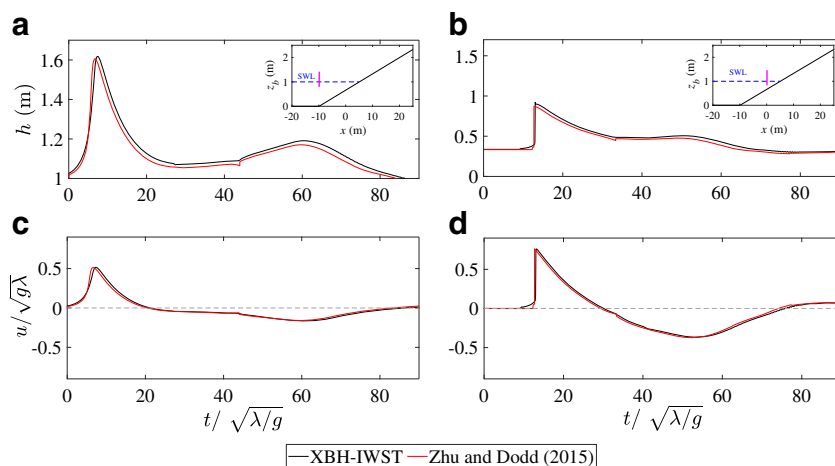
Appendix 2: Comparison of XBH-IWST and Zhu and Dodd (2015) for the hydrodynamics

Figure 17 shows the time series of h and the scaled velocity, $u/\sqrt{g\lambda}$, at two different cross-shore locations. Overall, results show a very good agreement in terms of

Table 10 nRMSE and ρ_{mr} for h and $u/\sqrt{g\lambda}$ at two different cross-shore locations

	nRMSE		ρ_{mr}	
	h	$u/\sqrt{g\lambda}$	h	$u/\sqrt{g\lambda}$
$x = -10$ m	0.2078	0.1382	0.9881	0.9915
$x = 0$ m	0.2576	0.1684	0.9794	0.9860

Fig. 17 Time series of h at $x = -10$ m **a** and $x = 0$ m **b**, and $u/\sqrt{g\lambda}$ at $x = -10$ m **c** and $x = 0$ m **d**; reference line: grey dashed line; the two subplots in **a** and **b** show the two cross-shore locations in the model domain, respectively



hydrodynamics response between XBH-IWST and Zhu and Dodd (2015) (see also Table 10).

Appendix 3: Representation of the net return flow in XBNH-IWST

Since XBNH is based on the one-layer version of the SWASH model, no vertical discretisation of the velocity profile is available. Therefore, only a depth- and phase-averaged net current can be obtained from the model. Results show that the predicted net current is directed offshore. Figure 18 shows the modelled and experimental u for SEG1 of BE1.2 for the Alsina et al. (2016) case and the wave-averaged velocity over the wave group period, $T_g = 15$ s, $u_{mean} = -0.46$ m/s for XBNH-IWST and $u_{mean} = -0.48$ m/s for the experiments. Figure 18 also shows the modelled $q_{tot} = q_s + q_b$ for the same segment. q_{tot} is also depth-averaged, and the presence of a net depth-averaged velocity leads to net mean offshore transport, $q_{tot,mean} = -0.001$ m³/m/s, even if entrainment is considered.

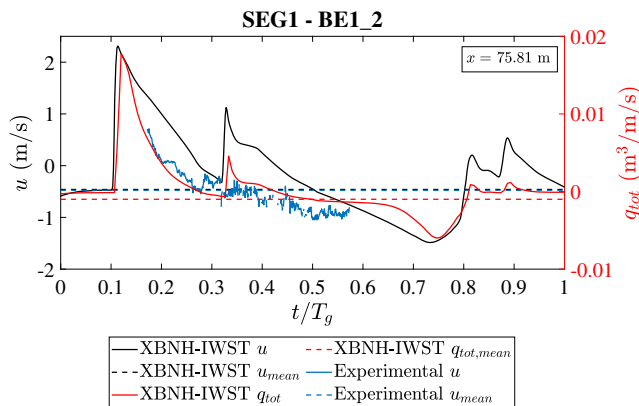


Fig. 18 Time series of u and q_{tot} , and u_{mean} and $q_{tot,mean}$ at $x = 75.81$ m over T_g for SEG1 of BE1.2 (Alsina et al. 2016)

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