

1 **Review**

2 **Approaches to three-dimensional reconstruction of plant shoot topology and**
3 **geometry**

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10 There are currently 805 million people classified as chronically undernourished, and yet the World's
11 population is still increasing. At the same time, global warming is causing more frequent and severe
12 flooding and drought, thus destroying crops and reducing the amount of land available for agriculture.
13 Recent studies show that without crop climate adaption, crop productivity will deteriorate. With access
14 to 3D models of real plants it is possible to acquire detailed morphological and gross developmental
15 data that can be used to study their ecophysiology, leading to an increase in crop yield and stability
16 across hostile and changing environments. Here we review approaches to the reconstruction of 3D
17 models of plant shoots from image data, consider current applications in plant and crop science, and
18 identify remaining challenges. We conclude that although phenotyping is receiving an increasing
19 amount of attention – particularly from computer vision researchers – and numerous vision approaches
20 have been proposed, it still remains a highly interactive process. An automated system capable of
21 producing 3D models of plants would significantly aid phenotyping practice, increasing accuracy and
22 repeatability of measurements.

23 **Additional keywords:** image-based, plant modelling, reconstruction, three-dimensional.

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25 Reconstruction of plant shoot topology and geometry

26 The need for increased crop yields is becoming urgent as the amount of arable land available is reduced
27 and environmental factors worsen, however, plant phenotyping has been identified as a key bottleneck
28 in the process of improving crop yields. Here we review approaches to 3D shoot reconstruction to
29 improve phenotyping using image-based methods. An automated system capable of producing 3D
30 models of plants would significantly aid phenotyping practice, increase accuracy and repeatability of
31 measurements and potentially aid the process of improved crop yields.

32 **Introduction**

33 Understanding the mechanisms underlying the growth of agriculturally important plant
34 species is becoming increasingly critical to society, particularly as the quantity of food

35 produced must double by 2050 if it is to meet the demands of the expanding global
36 population, which is likely to exceed nine billion (Sticklen 2007; Faaij 2008; Paproki *et al.*
37 2012). The Food and Agriculture Organisation of the United Nations (FAO) already considers
38 805 million, or one in nine people ‘chronically undernourished’. Moreover, population growth
39 is not the sole contributor towards an increasing demand for food: the spread of prosperity
40 throughout the world, predominantly in developing countries such as India and China, is
41 increasing food intake per capita and driving demand for a richer, more varied diet (Kearney
42 2010; Bonhommeau *et al.* 2013). Consequently, increasing pressure is being placed on
43 agriculture to improve crop yields (Sutton *et al.* 2011).

44 During the decades following the ‘Green Revolution’ (Evenson and Gollin 2003), annual
45 improvements in crop yield were typically 2–5% (Gaud 1968). However, over the past two
46 decades this has plateaued at around 1%, leading to concerns that some fundamental limit
47 may have been reached (Khush 1996). The severity of the situation is such that rice demand
48 recently exceeded supply for 2 years (2009–11), and world stocks of grains are now the
49 lowest they have been for 45 years (Furbank *et al.* 2009; Furbank and Tester 2011).

50 Changes in climate and the shortage of arable land constitute further challenges for
51 sustainable agriculture, as global warming has been shown to cause more frequent and severe
52 flooding and drought, which destroy crops (Adeloye 2010). Recent work has shown that
53 without crop climate adaption, crop productivity will actually deteriorate (Tester and
54 Langridge 2010; Challinor *et al.* 2014). It is clear that a new approach to a sustainable
55 increase in crop yield is necessary (Furbank and Tester 2011).

56 In the face of these challenges, an understanding of the relationship between genotype and
57 environment on plant phenotype is invaluable to the agricultural community. An improved
58 understanding of phenotypes would aid breeding and inform genetic modification, facilitating
59 increased nutrient use and photosynthetic efficiency and thereby increasing crop yield and
60 stability across hostile and changing environments (Quan *et al.* 2006). This would
61 significantly alleviate a majority of problems defined by the FAO and help lift farmers out of
62 poverty by generating additional income. In addition to pre-breeding applications,
63 phenotyping currently constitutes a major bottleneck in basic research, particularly in the
64 construction of quantitative models of plant development (Preuksakarn *et al.* 2010).

65 Phenotyping methods and technologies have attracted significant and rapidly increasing
66 attention in recent years. Major phenotyping projects are now underway across Europe,
67 Australia, Canada and the United States of America. Emphasis is being placed on fully-
68 automatic, high-resolution, high-throughput, quantitative measurement of plant structure and

69 function. Techniques have been proposed for the quantification of a wide range of properties
70 of roots, shoots, leaves and seeds.

71 A majority of these methods are image-based (Fahlgren *et al.* 2015), relying on the
72 automatic extraction of traits from, usually, colour images (Lobet *et al.* 2013). Simple
73 analysis of colour can be important when examining plant response to biotic and abiotic
74 stresses. When structural traits are needed, images are typically segmented to identify plant
75 components, or key features identified, before measurements are made. These measurements
76 are expressed on the (2D) image plane in pixel units. Conversion to real-world dimensions
77 (e.g. mm) requires some pre-calibration of the image acquisition equipment, and a final pixel-
78 to-mm conversion step. If angular measures are to be made, the camera must be arranged to
79 ensure that angles measured in the image plane reflect the real-world angle of interest. It is
80 common to find that the set of measurements obtainable from this type of system is
81 determined by the relative placement of sample and camera.

82 The reconstruction of 3D models of the viewed plant provides an alternative approach. In
83 this method, measurements are made across a representation of the 3D shape of the target
84 object that is first reconstructed from sensor data rather than in the image plane. Assuming
85 that a sufficiently accurate and detailed model can be created, a wide variety of traits can be
86 computed. More importantly, if new traits are required at a later date they are likely to be
87 computable from the same model. In the 2D, image-centred approach, some traits may not be
88 recoverable from the available image(s). The features required may not be visible, or the
89 calibration information needed to make real-world measurements might not have been
90 recorded.

91 Access to 3D models that capture morphological and developmental data is also significant
92 in the use of simulation approaches to study the ecophysiology of plants (Larcher 2003): for
93 example, the modelling of photosynthesis. It is unclear whether plant species have an optimal
94 arrangement for photosynthesis, and further studies using accurate plant representations need
95 to be conducted to determine this (Pound *et al.* 2014). Detailed 3D representations of real
96 plants allow numerous simulations, e.g. ray-tracing techniques to simulate illumination
97 conditions, within a range of artificial canopies (Burgess *et al.* 2015).

98 It is clear that 3D models have the potential to provide the continued refinement of plant
99 phenotyping methods required to quantify plant growth, development, tolerance and
100 physiology. The cost associated with the 3D model-based approach is, however, that an
101 appropriate reconstruction method is required.

102 In this review we appraise available approaches to the reconstruction of plant shoot
103 topology and geometry from image data, reviewing their actual and potential contribution to

104 the construction of accurate 3D models. The remainder of the paper is organised as follows:
105 we begin by introducing the reader to 3D modelling in general, providing an overview of the
106 various approaches before providing a more in-depth review of image-based modelling
107 approaches; then we discuss how these have been applied to plants, and the challenges and
108 opportunities facing plant modelling before adding our concluding remarks.

109 **Background: three-dimensional modelling and plants**

110 Three dimensional (3D) modelling has been applied to a wide range of scenarios from
111 medical usage, creating a 3D representation of a brain using magnetic resonance imaging
112 (MRI) (Lauterbur 1973), for example, to the creation of environments for films and
113 animations. 3D models are ubiquitous, and becoming increasingly prevalent as modern, low-
114 cost machines and sensors now have the capability to capture and render them.

115 Many 3D reconstruction methods focus on objects with relatively simple structures; those
116 lacking occlusions and specularities but containing textured areas, or manmade objects with
117 easily identifiable symmetry or shapes (Furukawa and Ponce 2010). Plants, however, are
118 complex and challenging objects to model and, until the late 1960s, botanical drawings were
119 the primary means of representing plant architecture. Today, with the use of high performance
120 computers and the availability of portable cameras and sensors, many approaches exist, from
121 those relying on depth data obtained by lasers to those drawn free-hand.

122 Approaches to model plant architecture typically fall into two categories, known as rule-
123 and image-based approaches. Rule-based methods capture knowledge of plant structure and
124 form in a set of user-defined rules, which can then be applied to generate example models
125 consistent with that knowledge. There are many approaches to rule based modelling such as
126 L-Systems (Lindenmayer 1968; Prusinkiewicz *et al.* 2000; Karwowski and Prusinkiewicz
127 2003; Prusinkiewicz 2003; Ole and Winfried 2008; Boudon *et al.* 2012), Relational Growth
128 Grammars (Kurth 2007) and AMAP (de Reffye *et al.* 1988), which have been applied to a
129 variety of problems (Lintermann and Deussen 1996; Deussen and Lintermann 1997;
130 Shlyakhter *et al.* 2001; Boudon *et al.* 2003, 2012).

131 Rule-based methods are used to simulate plant growth, creating synthetic plant structures.
132 These are exemplars of the class of plant simulated, but do not necessarily capture the detailed
133 structure of any existing, real plant. They are, however, highly valuable as the basis of
134 functional structural plant models (FSPMs). FSPMs are used to study the ecophysiology, how
135 plants sense and respond to environmental change, of a plant by combining the 3D, structural
136 representation with a model of some physiological function (Vos *et al.* 2010).

137 In contrast, image-based methods use real-world data to develop detailed 3D models of real
138 plants, often relying on techniques developed by the computer vision community. These

139 models can be used to support both simulations of plant function and the extraction of the trait
140 measurements required for phenotyping. Although image-based modelling has made
141 significant progress towards achieving photorealism, that is constructing a model as
142 realistically as possible, over the past decade, creating accurate representations remains a
143 research problem. This is, in part, due to the complexity of the plants and the environments
144 they inhabit, and also the lack of a single definition of image-based modelling (McMillan and
145 Bishop 1995): multiple approaches to the problem have been proposed, each with its own
146 strengths and weaknesses. Fig. 1 provides an overview of current approaches, along with an
147 indication of their current range of application in plant modelling.

148 Plant architecture, as defined by Godin (2000), is difficult to model due to the dynamic
149 behaviour of plants, from short-term changes such as the reorganisation of foliage to long-
150 term growth patterns, and intricate phyllotaxis (Ivanov *et al.* 1995; Tan *et al.* 2003; Reche-
151 Martinez *et al.* 2004; Zeng *et al.* 2006; Kang and Quan 2009). A plant may consist of
152 hundreds of leaves spanning arbitrary directions and angles – even a small plant could require
153 a large number of polygons to define every facet digitally (Weber and Penn 1995).

154 Moreover, mature crop plants, which are of primary interest to the phenotyping and
155 breeding communities, typically have a more complex 3D architecture than laboratory-based
156 model plants such as *Arabidopsis thaliana*.

157 Despite these challenges, previous work (Tan *et al.* 2007) suggests that image-based
158 approaches offer the best solution to 3D reconstruction. Image acquisition is usually
159 straightforward, the tools involved have shown promising results and do not require their
160 users to have high levels of expertise (Tan *et al.* 2007).

161 **Image-based 3D modelling**

162 Image-based approaches reduce, although do not eliminate, the complexity associated with
163 rule-based approaches. They delineate real world plants by extracting geometry directly from
164 images, with the elusive goal of achieving photorealism (Weber and Penn 1995). Capture
165 techniques can be categorised as either active or passive, where active is significantly more
166 expensive and requires specialist hardware to project some form of light into the scene. Light
167 detection and ranging (LiDAR) and laser-based ‘digitisation’ are perhaps the best known
168 active approaches.

169 Space carving, shape-from-silhouette (SFS), shape-from-shading (Cryer and Shah 1999),
170 shape-from-contour, stereo vision and structure-from-motion (SFM) (discussed below) are
171 passive approaches commonly conducted using standard hand-held cameras. The challenge
172 for these methods is to produce 3D representations under normal, ideally natural, illumination
173 conditions. Approaches such as shape-from-shading (Horn and Brooks 1989), shape-from-

174 texture (Kender 1981) and shape-from-edges (Wahl 2001) are used but are uncommon in
175 plant modelling due to the complexity of the object and their reliance on a single image,
176 making them more susceptible to occlusion, a common occurrence in plants.

177 Image based approaches can be further categorised into those that begin with an existing,
178 generic, plant model that is fitted to the image data, known as top-down, or those that apply a
179 series of processes to the contents of images, to create an increasingly accurate and realistic
180 plant model, known as bottom-up.

181 Top-down approaches use an existing model that is adjusted to fit the image data, so that
182 the new plant representation is consistent with what is observed. The application of top-down
183 approaches to inter-species is unclear, as differences between the expected and actual
184 geometry of a plant or leaf increases. Bottom-up approaches, reviewed in this paper, are
185 methods beginning with one or more images which reconstruct a plant model based only on
186 the observed pixel data. We focus here on bottom-up approaches, as they provide the greatest
187 opportunities for generic (species-independent) 3D reconstruction of plants. The top-down
188 approach, although of interest, also suffers from a lack of models with which to guide
189 analysis.

190 *Active approaches*

191 LiDAR, a remote sensing technology based on the extension of principles in radar
192 technology, measures the distance between itself, the scanner, and the target object by
193 illuminating the object with a laser and analysing the time it takes the reflected light to return
194 (Northend 1967; Killinger 2014). LiDAR has two distinct fields of application; airborne
195 LiDAR, in which the scanning device is commonly attached to a plane or helicopter, and
196 terrestrial laser scanning (TLS), which is conducted on the ground and the scanner is either
197 stationary or attached to a ground-based vehicle (Ullrich and Pfennigbauer 2011).

198 Laser scanning acquires information from an object by digitising selected co-ordinates and
199 representing these as a 3D point cloud by recording the scanned distance to each. Just like
200 cameras, they have a cone shaped field of view and capture multiple views in order to
201 perform complete reconstruction. The main difference in resultant data between cameras and
202 time-of-flight lasers is that the latter stores depth in each pixel whereas cameras store colour
203 (Curless 1999).

204 ‘Structured light’ techniques provide an alternative approach to depth measurement. Here
205 the light source (usually laser, or near-infrared) is positioned a short distance from an imaging
206 device (usually a camera fitted with appropriate filters). Light leaves the emitter and is
207 reflected into the camera by the target object. Knowledge of the light source, and use of
208 appropriate filters, makes the emitted light pattern easy to detect in the image. The relative

209 positions and orientations of light emitter and imaging device are also known, allowing 3D
210 data to be recovered from the position of key points of the emitted pattern by triangulation. A
211 variety of light patterns have been used including spots, lines and 2D grids. Perhaps the most
212 common example of a structured light device is the Microsoft Kinect, which emits a
213 rectangular dot pattern in near-infrared. Microsoft's KinectFusion (Newcombe *et al.* 2011)
214 software also allows depth data gathered from multiple views to be combined in a single
215 model.

216 Structured light methods can be effective, and in recent years have become more easily
217 obtainable and affordable, as components of RGB-D (red, green, blue, depth) devices such as
218 the Kinect. RGB-D cameras combine depth sensing with common camera functionality,
219 providing both 3D and colour measurements.

220 Unfortunately, however, structured light approaches suffer several drawbacks when applied
221 to plants. They can be difficult to use in bright light, e.g. glasshouses, where background
222 illumination makes the projected pattern hard to detect. Highly reflective leaf surfaces can
223 also act as (partial) mirrors, reflecting a significant proportion of the emitted pattern away
224 from the imaging device and again making it hard to detect. Narrow objects, e.g. rice leaves,
225 can fall between the key points of the emitted pattern (e.g. Kinect's dots) and simply fail to
226 reflect the pattern back.

227 With recent advances in technology such as readily available software to deal with the
228 large computational requirements of these approaches and the development of 'multi-pulsed'
229 LiDAR (Su *et al.* 2015), LiDAR is becoming more commonly used, and can easily be
230 deployed in both airborne and ground-based forms. The airborne approach is particularly
231 useful for reconstructing forest canopies and tree structure from dense forestry, enabling the
232 reconstruction and acquisition of geometric properties from remote locations, which other
233 image-based approaches may find difficult due to accessibility.

234 *Passive approaches*

235 Although LiDAR can be effective it requires expensive equipment that is out of reach of
236 many. Passive approaches are therefore gaining an increasing amount of popularity, as they
237 only require a standard 'off-the-shelf' digital camera to capture overlapped images,
238 simultaneously or sequentially, and a basic computer to process them. As passive methods use
239 only the radiation present in the scene, specialist lighting is often not required.

240 A variety of passive approaches exist which manipulate the 2D image information in
241 various ways. One of these enables 3D objects to be reconstructed from 2D silhouettes by
242 back-projecting them from their cameras' viewpoints and intersecting the resulting cones.
243 SFS (shape-from-silhouette), introduced by Laurentini (1994), does exactly this. The aim is to

244 construct a 3D model by projecting the 2D silhouette of the object from multiple images into
245 a single 3D space in which intersecting projections produce the 3D model, known as the
246 visual hull.

247 The visual hull determines the largest possible shape that is consistent with the available
248 images. In many cases, where the number of input images is high, the resulting model will be
249 a good approximation. However, as the scene becomes increasingly complex, for example, a
250 scene with concavities and occlusions, the dissimilarity between the resulting model and the
251 actual object will increase. A complex plant canopy consisting of multiple overlapping plants,
252 for example, will produce poor results in which leaf thickness is overestimated and
253 concavities are missed or underestimated.

254 SFS is simple to implement, requiring only a set of arbitrary views of an object from
255 known camera positions, which can be obtained through camera calibration (Salvi *et al.*
256 2002). The biggest challenge lies in ensuring the foreground (object) and background can be
257 separated to find the object's silhouette. In natural conditions this can be a challenging
258 problem, however at present much phenotyping work is conducted in controlled environments
259 where there exist several techniques for background and foreground separation, for example;
260 the Canny algorithm (Canny 1986) or frame differencing (Piccardi 2004). A comprehensive
261 review of SFS is provided by Dyer (2001).

262 Space carving was introduced by Kutulakos and Seitz (2000) as a solution to the
263 difficulties associated with SFS. It starts with a bounding box big enough to encapsulate the
264 entire object or scene, whose size is often pre-defined by the user. The bounding box is
265 partitioned into a series of voxels, cubes in three-dimensional space represented by co-
266 ordinates and size. The algorithm relies on measures of the photo-consistency of voxels,
267 where a voxel is said to be photo-consistent if, and only if, the colour of the voxel appears to
268 be (approximately) the same in all of the images in which it is visible. It is assumed that if
269 some voxel is the same colour then it lies on the object's surface and is marked as seen. The
270 set of voxels that are marked as 'seen' then make up the 3D model of the object.

271 The algorithm is again simple to implement, iterating through each voxel of the bounding
272 box, projecting to each image and removing (carving) those voxels that are not photo-
273 consistent. Each time a voxel is carved away it potentially uncovers a new voxel, which also
274 requires evaluation for photo-consistency, and the process continues until all visible empty
275 voxels are removed or some user defined stopping criteria is met.

276 Other less common voxel techniques used for 3D reconstruction include voxel colouring
277 (Seitz and Dyer 1999) and generalised voxel colouring (Culbertson *et al.* 2000), which, like
278 space carving, rely on the consistency of colours between images to determine whether some

279 seen voxel lies on the surface of the object. However, unlike space carving, the camera
280 positions are often constrained in order to determine colour consistency more easily, limiting
281 the views that can be used, and so the complexity of the objects that can be modelled.

282 Stereo vision differs significantly from SFS and is based on key functionality of the human
283 vision system – the ability to see the same scene but from slightly different viewpoints,
284 achieved through the distinct lateral positioning of the eyes – known as binocular vision.
285 Stereo vision aims to mimic this process, extracting 3D information by processing two 2D
286 images captured simultaneously from slightly different horizontal angles, focusing on the
287 same point in space.

288 Stereo vision has three main processing steps: stereo calibration, feature extraction and
289 correspondence matching. These are discussed in turn below.

290 Stereo calibration finds the intrinsic parameters (focal length, principal point, radial and
291 tangential distortion) of each camera and the extrinsic parameters (rotation matrix and
292 translation vector) linking the two cameras. It allows 3D world co-ordinates to be mapped to
293 2D image co-ordinates.

294 Feature extraction identifies features of interest, independently, in each image. Features
295 vary widely and range from simple image patches to extended straight lines, circles and
296 regions corresponding to viewed objects. A common middle ground is to define features by
297 their local image properties, most often their gradients. Edges and corners are widely used,
298 these are points at which image values vary significantly (i.e. the gradient of image values is
299 large) in one or more directions.

300 Correspondence matching links features found during feature extraction between views. If
301 the image features associated with a particular object feature can be identified in multiple
302 images, taken from different viewpoints, knowledge of the cameras' positions and
303 orientations allow its 3D location to be determined. The disparity associated with each match
304 – the difference in the image co-ordinates of the matched features – is obtained and can be
305 used to create a disparity map which in turn can be used to acquire depth information.

306 Structure-from-motion (SFM) follows the same process. However, where stereo vision
307 captures two images simultaneously, SFM captures images sequentially, estimating 3D points
308 from an extended sequence of images. 3D data is then estimated either sequentially, by
309 matching pairs of images, or globally, matching features between all images. A review of
310 early vision dating back to the 1970s and 1980s can be found in work by [Barnard and Fischler
\(1982\)](#) and [Dhond and Aggarwal \(1989\)](#), respectively, and [Brown *et al.* \(2003\)](#) provide a
311 comprehensive review of the advances in modern stereo vision.
312

313 Binocular stereo and structure from motion rely on points on the target object projecting to
314 different locations in each of a set of images. By finding image features arising from those
315 points, and matching them between views, they can reverse the projection process to recover
316 3D. Photometric stereo (Woodham 1989) takes a different approach. Here, multiple images
317 are taken from a fixed camera, but the lighting conditions are varied between each image
318 acquisition. Object points therefore project to the same location in each image, but appear
319 different due to changes in illumination. Knowledge of the lighting used, and of the image
320 formation process, allows 3D information, usually surface orientation, to be computed from
321 these variations on appearance.

322 Photometric stereo is less widely used in practise than binocular stereo and SFM, as it can
323 be difficult to adequately control and quantify lighting conditions. Surface orientation must
324 also be integrated to obtain depth estimates, which can pose further problems. Photometric
325 stereo is, however, now attracting interest within the controlled environment phenotyping
326 community.

327 Less common methods such as concept sketching, which is the process of digitally drawing
328 3D shapes or is the process of creating a 3D model from a 2D sketch, have also been applied
329 to plant reconstruction (Masry and Lipson 2007), focusing more specifically on structure. The
330 sketching technique is less relevant in modern times, as the available computing resources
331 make methods based on real mages practicable.

332 Sketching does, however, have some advantages, such as the ability to use freehand
333 drawing, allowing shapes to be accurately captured and contours to be easily identified
334 (Anastacio *et al.* 2006). Sketching commonly uses an interface to enable direct manipulation
335 of the plant simulation, allowing even novice users to create plant structures (Masry and
336 Lipson 2007). Though, as with rule-based approaches, the model does not represent a real
337 plant.

338 *Representing 3D data*

339 Though all the methods discussed here recover 3D information from images, different
340 methods represent 3D data in different forms.

341 Voxel-based methods (SFS, voxel colouring, space carving) produce a volumetric
342 description of the target object. This is a 3D array of cells – effectively a 3D image – in which
343 each cell (voxel) contains one of two possible values. These values indicate whether or not
344 that voxel is occupied by the object, effectively separating (3D) object material from (3D)
345 space. Volumetric representations are compact, and their accuracy can be controlled by
346 varying voxel size; larger voxels result in a more ‘blocky’ representation. The set of shape
347 and other measures, i.e. traits, directly available from voxel descriptions is, however, limited.

348 Total object volume can be estimated by counting occupied voxels, and fitting a convex hull
349 or similar structure around those voxels provides crude object dimensions. More detailed
350 characteristics require further processes, however, and it is common to fit a surface over the
351 object voxels using the marching cubes algorithm (Lorensen *et al.* 1987), or similar. Further
352 measures and features can then be extracted from the surface description.

353 LiDAR, structured light, binocular stereo and structure from motion typically produce a
354 point cloud representation: a set of unconnected x,y,z co-ordinates describing the locations of
355 matched points. Again, coarse, summary traits can sometimes be obtained directly from this
356 data structure, but it is common to first link nearby points to form a mesh, and fit some form
357 of surface.

358 Photometric stereo is unusual, in that it typically produces local surface orientation
359 estimates, from which depth must be recovered to produce a full surface representation.
360 Whatever the route, surface-based representations are usually required in plant phenotyping
361 and simulation work.

362 In a majority of cases, the final surface representation produced by 3D reconstruction
363 methods is piecewise. Rather than fit a single, mathematically complex, surface over the
364 whole object, a large set of simpler surfaces is used. These are linked together to produce a
365 complete description. Small triangular planes are most commonly used, as these can be linked
366 along their edges to describe a wide range of complex shapes.

367 **Application to plants**

368 It is crucial to construct precise 3D representations of plants to facilitate accurate
369 assessments of physiology. With the use of accurate 3D plant models more subtle traits can be
370 identified, leading to a greater amount of, and more useful, information with respect to plant
371 architecture and growth. Models can be used to measure the geometric structural parameters
372 of plants, which is of utmost importance in understanding the biological and physical
373 processes of growth, a vital element in increasing crop yield (Wang *et al.* 2009). Height,
374 dimensions, leaf area, angle and distribution are important parameters, all of which relate
375 directly to the growth and photosynthetic properties of plants.

376 Plant architecture is known to be a determinant of the productivity of canopies. On a simple
377 level this arises via the relationship between vertical leaf area index (LAI), leaf area
378 distribution (LAD) and leaf angle. The penetration of light that results is mathematically
379 described by the Mons–Saeki equation derived from Beer's law (Hirose 2005). Vertical
380 distribution of leaf photosynthesis is dominated by the interaction between light gradients and
381 the individual light response curve of each leaf. A vertical canopy thus permits a higher
382 optimal LAI and a higher overall rate of canopy photosynthesis. Many existing productive

383 crops have an ‘erectophile’ tendency. However, the dependence on a high LAI can lead to
384 higher nutrient requirements and weed problems. Therefore, there is still a need to understand
385 the relationship between photosynthesis dynamics and precise canopy architecture.

386 LAI and LAD estimates are two measurements that offer significant insight into the ability
387 of a plant to capture radiation for photosynthesis. These measures can be obtained manually,
388 though the process is often tedious and error prone, for example, an operator has to manually
389 measure a leaf segment using callipers. As a result, observers may have varying opinions, and
390 the approach tends to be intrusive and accuracy decreases compared with the automatic
391 measurements. However, with the use of modern technology, approaches are becoming less
392 interactive and are increasingly becoming more accurate and automated. One such image-
393 based approach, which calculates the leaf area as the area of the surface of the 3D model by
394 summing the area of triangles, is applied to corn plants by Wang (2009). Hosoi (2006)
395 develop a method known as voxel-based canopy profiling to measure the LAI and LAD of
396 small trees (namely *Camellia sasanqua* and *Deutzia crenata*) using both mobile ground-based
397 and airborne LiDAR, obtaining results as accurate as 0.7 up to 17% for the minimum leaf
398 thickness for the measurements of LAI and LAD. Automatic measurements were compared
399 with those obtained by stratified clipping, where plant parts are manually measured in
400 segments, one a plant segment has been manually measured it was removed to provide access
401 to the next part, typically starting from the top of the plant and working downwards.
402 Alternatively, a stereo vision approach can be used to obtain measurements and identify
403 branch and leaf segments, for example, Paproki *et al.* (2011) applied this to cotton plants.
404 Using a top-down approach, they recursively segment the plant into regions, at each iteration
405 determining which segmentation algorithm to apply in order to extract a specific limb from
406 the model. With this they accurately identified 20 out of 22 cotton plant segments.

407 The ability to automatically identify and extract single leaf data would significantly
408 improve the process of calculating LAI and LAD. Biskup (2007) proposed an approach that
409 uses stereo vision in a field setting to track the nocturnal and daytime movement of leaves and
410 determine drought stress, with a particular focus on soybean plants. Some approaches use a
411 skeleton representation of the plant to identify regions. The skeleton representation is a thin
412 version of the shape emphasising its topological properties. In most cases the skeleton is a
413 thin, connected, line aligned with the centre of the object. The process of creating a skeleton
414 model is referred to as skeletonisation. Jin (2009) used a real-time stereo vision approach with
415 a skeletisation algorithm to identify individual corn plants and highlight leaves from stems,
416 they report that they were able to accurately detect 96.7% of corn plants and that they were
417 within 1–5 cm accuracy when determining the plant centre.

418 **Cai and Miklavcic (2012)** used 2D skeletons to extract the 3D structure of cereal plants.
419 They reported that they were able to deal with difficulties such as overlapping plant parts and
420 broken segments resulting in smooth, connected 3D cereal structures. Stereo vision and SFM
421 have been used to reconstruct plant models in many other similar scenarios, from the
422 construction of trees to maize canopies (**Ivanov et al. 1995**; **Andersen et al. 2005**; **Quan et al.**
423 **2006**; **Wang et al. 2009**; **Hartmann et al. 2011**; **Lou et al. 2014**). Pound (2014) proposed a
424 fully automated stereo vision approach to reconstruct plant shoots, namely wheat (*Triticum*
425 *aestivum*) and rice (*Oryza sativa*). The reconstruction process works on segments of leaves
426 and develops each individually using level sets, which optimises the model based on image
427 information. The effects of occlusion are reduced by identification of the best image for each
428 segment, requiring few assumptions to be made.

429 LiDAR has received a vast amount of attention in recent years because hardware has
430 become more affordable and applicable to a range of plant species. For example, the
431 geometric structure of white clover canopies has been assessed by **Rakocevic (2000)** using
432 electromagnetic digitising apparatus. They used corner flags to aid calibration, thus improving
433 the accuracy of the reconstruction, and applied a destructive approach. The canopy was
434 pruned from the top downwards and scanned at each stage, with results showing that the
435 semi-automated measurements varied between 5–20% in comparison to the manual
436 measurements. The error in this work could, however, lie within either the manual or
437 automatic measurements and without the use of an independent, confirmed ground truth it is
438 not possible to tell.

439 Similarly, **Paproki et al. (2012)** presented a mesh-based, 3D LiDAR approach for
440 reconstructing *Gossypium hirsutum*, which partitioned the plant into morphological regions.
441 They stated that they were able to match leaves in 95% of the cases and that LAI accuracy
442 was within 10% of manual measurements.

443 Aside from single leaf and small crop measurements, other larger plants have received a
444 great deal of attention. Trees, for example, are particularly valuable due to their functional
445 roles in the environment and have received considerable interest aimed at calculating the tree
446 crown volume, 3D architecture and branching structure. LiDAR is the most common
447 approach for the reconstruction and approximation of trees (**Weber and Penn 1995**; **Sinoquet**
448 **and Rivet 1997**; **Sakaguchi 1998**; **Shlyakhter et al. 2001**; **Boudon et al. 2003**; **Reche-Martinez**
449 **et al. 2004**; **Phattaralerphong and Sinoquet 2005**; **Hosoi and Omasa 2006**; **Rutledge and**
450 **Popescu 2006**; **Neubert et al. 2007**; **Omasa et al. 2007**; **Tan et al. 2007**; **Livny et al. 2010**;
451 **Preuksakarn et al. 2010**; **Van Leeuwen et al. 2010**; **Tang et al. 2013**), making it possible to
452 estimate forest attributes, such as height, diameter and canopy closure, all of which are

453 essential parts of forest management. Other modelling approaches are often limited in their
454 capacity to retrieve individual tree and crown attributes due to occlusion or canopy gaps.

455 Skeletons can be used to represent the branching structure of trees, which can provide vital
456 information, particularly when occluded by leaves. Tang (2013) used TLS to obtain skeletons
457 from trees and Livny (2010) created a tree model from laser scans captured using a moving
458 vehicle. They applied a series of global optimisations to the branching structure – a constraint
459 ensuring branches are thicker closer to the root, for example, making it robust to noisy and
460 incomplete data, before scans are employed to consolidate a point cloud representing one or
461 more tree objects as skeletal structures. This optimisation aimed to reconstruct the major
462 branches of the captured tree(s), resulting in a graph structure that they defined as the branch-
463 structure-graph (BSG). The finer branching structures were then reconstructed from the
464 BSGs, with the assumption that the finer parts of the tree structure are made up of the same
465 branching structure as the core of the tree.

466 In the modelling of trees, canopy height models (CHMs), are used to represent horizontal
467 and vertical properties of tree canopies. However, retrieving these characteristics is
468 challenging and several difficulties have been identified, primarily the underestimating of
469 height which can occur when the earth's surface is occluded by the tree canopy (Pitkänen *et*
470 *al.* 2004; Zhao, Kaiguang 2007). Van Leeuwen (2010) proposed an airborne solution, the
471 parametric height model (PHM), to overcome the problem of underestimating tree height in
472 CHMs by describing the forest canopy as a series of cones fitted to the raw LiDAR point
473 cloud (Illingworth and Kittler 1988).

474 Other approaches to tree modelling exist: Shlyakhter *et al.* (2001) used visual hulls to
475 generate the skeleton of the tree augmented with an L-System approach, Neubert *et al.* (2007)
476 used a space carving approach to estimate tree volume, and Reche-Martinez *et al.* (2004)
477 combined volumetric opacity estimate with view-dependent texturing to reconstruct trees
478 from images. LiDAR is seldom used in smaller plant representations due to high processing
479 times but it is capable of producing adequate results, for example, Hosoi and Omasa (2009)
480 estimated the vertical area of wheat canopies.

481 More recently, Apelt *et al.* (2015) introduced Phytotyping^{4D}, a light-field camera system
482 which produced grey-scale images, depth information and a focus image, to measure plant
483 features in 4D. They successfully monitored rosette and individual leaf growth in
484 *Arabidopsis*.

485 **Challenges and opportunities**

486 With accurate 3D models various traits such as the tolerance, resistance, architecture,
487 physiology and growth can all be easily obtained, and more complex traits such as LAI, LAD

488 and photosynthesis measurements can be made. One recent method, proposed by Burgess *et*
489 *al.* (2015), automatically obtains the light distribution in three different wheat (*Triticum*
490 *aestivum*) lines without the need for manual measures. 3D models are captured using the
491 stereo vision approach proposed by Pound *et al.* (2014). The methods reviewed here have also
492 been shown to extract plant traits from 3D models that may otherwise have been tedious and
493 error prone.

494 However, 3D reconstruction is a challenging problem and complications arise irrespective
495 of the approach. Image-based models typically suffer from errors and omissions introduced
496 by occlusion, in which aspects of the scene are obscured relative to the camera, or parallax, in
497 which objects appear differently depending on their position relative to the camera (Kutulakos
498 and Seitz 2000). Active approaches can struggle in natural illumination conditions and with
499 reflective surfaces. These challenges, and others discussed here, make the complete
500 reconstruction of scenes and objects, with any method, a complex task. Table 1 provides a
501 summary of the advantages and disadvantages/challenges of these approaches.

502 Much of the previous work in this field has been focussed on single plant reconstruction,
503 where some success has been achieved. More recently, however, there has been an increased
504 interest in canopies, particularly those grown in the field, which is proving more difficult. In
505 cases where plant structure has proved too complex, approaches have relied on semi-
506 automatic reconstruction, i.e. (Rakocevic 2000), with a user guiding the reconstruction in
507 areas of ambiguity.

508 *Computer vision challenges*

509 Despite advances in technology, resources and increased interest in plant-related problems
510 from the computer vision community, approaches to the production of automated systems for
511 3D reconstruction are cumbersome. Few fully automated approaches – those capable of
512 capturing data, performing the intermediate steps and producing an output as a 3D model –
513 have been proposed. Many of the image-based approaches require user input, most commonly
514 during segmentation (for example, separating the background from foreground or leaf from
515 stem) or during image acquisition. However, the need for an automatic, robust and flexible
516 image analysis tool for plant modelling clearly exists (Hartmann *et al.* 2011), as does a desire
517 to extend these techniques to multiple plants and to install them in field environments.

518 For stereo vision, occlusion is perhaps the biggest challenge yet to be overcome. Images
519 are often captured from only two viewpoints, which restricts the view of the rear of an object,
520 resulting in a ‘2.5D’, rather than a complete 3D model. For this reason, stereo cameras are
521 often used from above for canopy or rosette analysis where a detailed 3D structure is not
522 necessary. Improved results may be obtained using multi-view stereo, or structure from

523 motion (Dhond and Aggarwal 1989). Although techniques exist to make this process more
524 computationally efficient, by e.g. exploiting epipolar geometry (Zhang 1998) or by using leaf
525 orientation (Laga and Miklavcic 2013), it still remains challenging. The problem of occlusion
526 is particularly common in plants where complex leaf structure may cause higher levels of
527 occlusion than is often seen in other stereo vision tasks (Pound *et al.* 2014). A given leaf
528 patch may not be visible in enough images, or its appearance may be so similar to that of its
529 neighbours that it may not be possible to ensure the correct correspondence is made.

530 Silhouette-based approaches offer some advantages. They are often simple to implement
531 and do not require a calibration target. Utilising multiple views, they form a complete model
532 representing the plant being imaged. However, these approaches are also ill-suited to the high
533 amounts of occlusion exhibited by some plants, and plant canopies (Mulayim *et al.* 2003),
534 also failing to account for concave surfaces, which will be interpreted as solid.

535 As a result, a silhouette approach commonly has to be augmented with another approach
536 that is capable of removing excess voxels (Mulayim *et al.* 2003). In extremely crowded
537 scenes, the reconstruction will fail to adequately capture the scene, even with post processing,
538 and an accurate reconstruction is impossible to obtain. Furthermore, silhouette approaches are
539 a poor choice for reconstruction when surfaces are thin, as leaves often are. Silhouette-based
540 plant reconstruction methods often result in blocky, overestimated data because the size of the
541 voxels representing the object being larger than the object itself. Leaves are usually either
542 poorly represented or, often, excluded.

543 Active methods such as LiDAR have the advantage of avoiding the correspondence
544 problem often seen in stereo imaging, and can deal well with complex object boundaries. A
545 primary concern with laser-based approaches is that their scanning time is directly related to
546 the resolution required. For example, LiDAR struggles with single leaf analysis, where the
547 required resolution dramatically increases the scanning time. This has been highlighted in
548 much of the work where high resolution scans are required. For example, Watanabe *et al.*,
549 (2005) modelled small rice plants using a continuous plant and fractal generator (CPFG)
550 approach with a 3D sonic digitiser to capture the initial point cloud. The digitisation process
551 can take up to an hour to complete for each rice plant. As a result, capturing high resolution
552 scans can only be achieved in a controlled environment where wind is avoided and other
553 environmental conditions can be monitored and controlled (Biskup *et al.* 2007). Rakocevic
554 (2000) claimed that the digitisation process for their approach to reconstruct white clover
555 canopies required between 3 and 7 h, which also involves a destructive approach to obtain a
556 complete reconstruction. This eliminates the possibility of repeating the experiment using the
557 same plant. The initial cost of hardware is also often prohibitive.

558 Non-laser approaches can also suffer from high processing requirements if too much
559 information is acquired. When using image-based reconstruction, determining the optimal
560 number of samples (images) is often problematic. Collecting excess samples is known as
561 ‘oversampling’, and will inevitably lead to a more intensive data acquisition model, higher
562 capacity requirements and greater redundancy (Shum and Kang 2000). In many cases
563 oversampling will lead to significantly higher computational requirements, without notable
564 benefits in output quality. Indeed, in some cases oversampling can lead to degradation in
565 reconstruction quality.

566 In contrast, incomplete and inaccurate reconstruction is a classic consequence of
567 ‘undersampling’, where an inadequate number of images fail to deal with the issues of
568 occlusion in the scene, and some regions of the model remain unobserved. The issues of
569 under or oversampling can be partly addressed by a robust image acquisition strategy using an
570 automated capture system. This can be quickly adapted to a variety of plant species or
571 experimental requirements, and the number optimal number of images derived.

572 The determination of an appropriate image acquisition strategy is challenging, particularly
573 given the dynamic structure of plants. Existing approaches typically rely on the use of
574 manually captured images or static camera positions that do not change, regardless of plant
575 species. With the use of active vision more flexible image acquisition approaches can be
576 adopted, dynamically changing to reflect the size of the plant. Gibbs *et al.* (2015), for
577 example, developed an active vision system that is capable of capturing images of plants
578 using a robot arm and a turntable overcoming the problems of static camera positioning. This
579 approach improves the data in comparison to fixed camera positions and produces a more
580 detailed point cloud, thus enabling a more accurate reconstruction.

581 Some plants may have to be moved if the camera position is static, for thin plants this can
582 cause difficulties in reconstruction as the leaf setup may vary between images. Though the
583 problem can be alleviated; for example, Kumar *et al.* (2012) reconstructed a plant using two
584 cameras and twin mirrors enabling the back of the plant to be seen from a front view and as a
585 result the plant does not need to be moved from its original setup. Alternatively, Kumar *et al.*
586 (2014) proposed a method in which the plant remains static and the camera rotates at a fixed
587 height around it.

588 Some image-based approaches require a calibration target – an object in the scene that is
589 used as a reference point to determine correspondence between two images – that is ideally
590 visible in each image. This can limit the types of plants modelled as they may occlude the
591 calibration target. Approaches that require a calibration target add further challenges to field
592 based phenotyping, where they are harder to include.

593 Moreover, phenotyping methods in general often make over-simplifying assumptions, such
594 that the object is of a specific shape or size, that the background is a certain colour, that the
595 object is green, or that each leaf is the same shape. With these specific conditions the
596 approaches lack robustness and struggle to deal with varying plant species. The approach by
597 [Pound *et al.* \(2014\)](#) provides a more robust approach with respect to plant species and is able
598 to reconstruct a variety of plants due to the ability to work on smaller areas (patches),
599 manipulate image data and lacks plant specific constraints which often reduce the robustness
600 of reconstructions.

601 Phenotyping is receiving an increasing amount of attention and is now recognised on a
602 global scale. Computer vision experts are becoming more involved, offering insights to
603 biologists. Conferences such as Computer Vision Problems in Plant Phenotyping (CVPPP)
604 and the International Workshop on Image Analysis Methods for Plant Science (IAMPS) are
605 becoming increasingly popular and provide a way to collaboratively improve approaches.
606 Training courses for biologists are also becoming more easily and frequently available.

607 *Validation challenges*

608 3D reconstruction has been a topic of interest in the wider computer vision community for
609 many years. As new reconstruction methods have been proposed it has been increasingly
610 important that some objective evaluation and comparison criteria be adopted. Several
611 approaches present themselves. First, standard test objects, of which at least some dimensions
612 have been precisely measured, can be used. Evaluation then becomes measurement of the
613 difference (error) between those measurement and corresponding values reported by the
614 proposal reconstruction method. This approach can be used to assess plant reconstruction
615 methods, but the complex and flexible nature of plant shoots can make it difficult to provide
616 appropriate ground-truth measurements.

617 An alternative approach is to create artificial images from existing 3D plant models (e.g.
618 [Pound *et al.* 2014](#)). Here, computer graphics techniques are used to produce images which can
619 be re-analysed by competing techniques. Evaluation is performed by comparing the newly
620 reconstructed and original 3D models. Once again, the complex and variable properties of
621 plant shoots (this time their appearance) can make this method challenging.

622 Regardless of the approach taken, there is a pressing need for sizeable plant reconstruction
623 datasets, including both images and ground truth, to be created and made available to the
624 development community. Recently, [Minervini *et al.* \(2015\)](#) released a first of its kind dataset
625 to investigate approaches in state of the art leaf segmentation. [Scharr *et al.* \(2016\)](#) provided a
626 collation of previous segmentation approaches and applied these to the CVPPP dataset,
627 discussing the methods and findings of the application.

628 *From laboratory to field*

629 At present phenotyping experiments are commonly conducted in controlled environments
630 where natural conditions such as light and wind can be monitored and manipulated. Much of
631 the work focuses on single plant reconstruction, though small canopies are now being used in
632 controlled environments too.

633 When constructing a dense plant, or a canopy, approaches to 3D modelling often require
634 intrusive, (moving the plant foliage in order to obtain further information), and destructive,
635 (the removal of plant parts), approaches to plant reconstruction in order to acquire plant
636 geometry. This allows image capture of aspects of a plant or canopy that may not otherwise
637 be seen, but makes repeat experiments, or capture of time series data, impossible. Destructive
638 approaches often require manual pruning of plants, adding additional time to the acquisition
639 process and increasing the potential for irreversible error, i.e. pruning too low, resulting in an
640 incomplete acquisition process. Despite these drawbacks, destructive methods continue to be
641 one of the few reliable methods for extending reconstruction approaches to dense canopies,
642 where occlusion is at its highest level. Indeed, most existing image-based approaches will fail
643 quickly as the number of plants is increased – a problem for which a reliable solution is yet to
644 be found. In principle, a surface based reconstruction approach could be extended to denser
645 canopies, but any results have yet to be presented. Field based phenomics still proves
646 challenging in this regard due to the ever changing environment and the need to reconstruct
647 crowded scenes containing multiple plants and many leaves. [White *et al.* \(2012\)](#) explain the
648 difficulties associated with field based phenomics, concluding that it provides too much of a
649 challenge for existing technology and that advances need to be made.

650 Directly related to field based phenomics are the difficulties associated with tree
651 reconstruction. Tree height, dynamic surroundings and the inability to conduct investigations
652 in controlled environments make modelling trees difficult. Key difficulties lie within physical
653 accessibility, availability of objective and efficient measurement techniques and the associate
654 costs ([Lovell *et al.* 2003](#)). Furthermore, [Jin and Tang \(2009\)](#) found that during experiments in
655 natural conditions the acquisition of images under direct sunlight turned out to be severely
656 saturated when compared with those taken under cloudy lighting conditions.

657 Using LiDAR in field environments is challenging as daylight can make it difficult to
658 capture data where the sun interferes with the reflection back to the scanner. If the
659 illumination of a single object changes during data acquisition further difficulties arise, such
660 as the colour of the object changing. Most LiDAR hardware is also affected by nearby metal
661 structures and magnetic sources, making experiments in urban environments challenging.

662 With respect to stereo vision, the matching problem is further complicated by issues of
663 illumination changes and poorly textured surfaces. Illumination is a key area that prevents
664 correct matching between a left and right view of the scene, in many cases adding noise, or
665 preventing parts of the 3D model being recovered (Paprocki *et al.* 2011). Furthermore,
666 approaches such as space carving and voxel colouring that rely on colour consistency between
667 images become impractical reconstruction choices. Even in a controlled environment it is
668 often overlooked that when using a turntable with fixed lighting and a rotating object, the
669 light hitting the surface will change at each rotation and as a result produces different shades
670 in each image.

671 Although field based phenomics is still challenging, experiments in controlled
672 environments show promising results and the use of robotics and active vision to
673 automatically capture images of plants used to perform reconstruction are further enhancing
674 the process improving both the quality and control.

675 **Concluding remarks**

676 A variety of methods have been proposed that seek to recover quantitative data on plant
677 traits from image sensor data captured in laboratories, glasshouses and field environments.
678 Some important plant traits, such as plant height, can be extracted directly from carefully
679 acquired images. Others, for example, capturing the detailed shape of wheat spikes or leaves,
680 require intermediate representations to be acquired first. Although phenotyping techniques
681 based on 3D representations are beginning to appear (Vadez *et al.* 2015; Cabrera-Bosquet *et*
682 *al.* 2016), the construction of 3D models of real plants remains a challenge. The ability to
683 recover physically correct representations of the 3D shape and structure of plants and plant
684 components from image data would underpin the measurement of rich sets of plant traits, and
685 thus accurate phenotypic information.

686 Different approaches to the 3D reconstruction of plants have been examined and it is clear
687 that reconstruction remains a challenging computer vision problem in which advances in
688 technology and optimal data acquisition techniques are required. Reductions in the cost of
689 equipment with regards to laser scanners and computers offering extensive computational
690 power, along with reduced costs in outdoor sensing equipment, is one area that is actively
691 improving, though the size of 3D models and the required detail is also increasing.

692 Although image-based approaches can produce realistic looking plant models, they still
693 remain highly interactive. A fully-automated system is clearly a necessity. However, an active
694 vision approach, that is an approach capable of manipulating the camera viewpoint in order to
695 investigate the environment, is required along with the ability to determine objects of
696 importance without user interaction or assumptions being made beforehand. Advanced

697 computing and algorithms and a reduction in hardware costs are necessary before this
698 becomes a reality and until then semi-automated approaches must be used.

699 Field-based phenomics are especially challenging due to environmental challenges and data
700 acquisition processes. Capturing data on a large crop is intrusive and requires modification to
701 the land setup, providing space to access the plants along single rows. Furthermore, the
702 process of acquiring data is resource intensive with multiple vehicles required in order to
703 capture rows more than once per day. With the lack of arable land it isn't feasible to approach
704 FBP like this and improving current crop yields is necessary beforehand.

705 It is encouraging to see phenotyping receiving increasing attention, particularly from
706 computer vision researchers, and as a result several conferences, workshops and training
707 courses are now available. Utilising 3D data will aid phenotyping practice and we expect to
708 see an increase in the development and uptake of 3D approaches in the near future.

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995 Manuscript received 4 May 2016, accepted 23 July 2016

996 **Fig. 1.** Three-dimensional modelling classification and uses for plant reconstruction shaded according
997 to the key. (Best viewed in colour).

998 **Fig. 2.** 3D plant reconstruction using structure-from-motion (SFM); (a) one of the original images of
999 the plant; (b) the point cloud generated by SFM; and (c) the final reconstructed model of the plant.

1000 **Table 1. Summary of advantages and disadvantages of methods for 3D plant**
1001 **reconstruction**

| Advantages | Disadvantages/challenges | Notes |
|-----------------------------------------------|--------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------|
| <i>Shape-from-silhouette</i> | | |
| Easy to implement and use | Unable to deal with concavities | Applicable for simple non-occluded plants with no concavities. Best conducted in a controlled environment |
| Supports arbitrary view points | Quality depends on depth of data structure | |
| No calibration target required | Can fail to reconstruct crowded scenes | |
| – | Difficulties with thin surfaces | |
| <i>Space carving</i> | | |
| Easy to implement and use | Relies on photo consistent measures | Can deal with more complex plants than SFS but relies on photo consistent measures. Most suited for controlled environments and textured surfaces |
| Guarantees the entire object will be captured | Quality depends on depth of data structure | |

| | | |
|-------------------------------------------------------|---------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Arbitrary viewpoints | Requires a bounding box is specified in advance | |
| No calibration target required | Can fail to reconstruct crowded scenes | |
| | <i>Stereo vision</i> | |
| Arbitrary viewpoints | Struggles with occlusions | Ability to reconstruct more complex plants but not well suited for high levels of occlusion. Most suited for controlled environments. |
| Ability to deal with concavities | Does not guarantee the entire object will be faithfully represented | |
| Can work on complex objects | Over/under sampling | |
| Affordable - requires only a standard handheld camera | Potentially high computational requirements | |
| – | Correspondence and parallax | |
| | <i>Structure-from-motion</i> | |
| Arbitrary viewpoints | Requires a calibration target | Suitable for complex plants and can deal with occlusions given an efficient image section strategy. Potential for field, but currently best suited for controlled environments |
| Ability to reconstruction complex objects | Over/under sampling | |
| Requires only a standard handheld camera | Potentially high computational requirements | |
| Deals with concavities | Does not guarantee the entire object will be faithfully represented | |
| – | Correspondence and parallax | |
| | <i>LiDAR</i> | |
| Can be deployed as both airborne and ground-based | Struggles with highly reflective surfaces | Suitable for moderately complex objects and is conducted in both controlled and field environments. More suitable for trees outdoors and would struggle with crops |
| Can handle concavities | Difficult to conduct under natural conditions (sunlight) | |
| Ability to reconstruct complex objects | Initial setup is still expensive | |
| No correspondence problem | Large computational requirements | |
| – | – | |