
Access from the University of Nottingham repository:
http://eprints.nottingham.ac.uk/35661/1/Finite%20control%20set%20model%20predictive%20control%20for%20grid-tied%20quasi-Z-source%20based%20multilevel%20inverter.pdf

Copyright and reuse:

The Nottingham ePrints service makes this work by researchers of the University of Nottingham available open access under the following conditions.

This article is made available under the University of Nottingham End User licence and may be reused according to the conditions of the licence. For more details see:
http://eprints.nottingham.ac.uk/end_user_agreement.pdf

A note on versions:

The version presented here may differ from the published version or from the version of record. If you wish to cite this item you are advised to consult the publisher's version. Please see the repository url above for details on accessing the published version and note that access may require a subscription.

For more information, please contact eprints@nottingham.ac.uk
Finite Control Set Model Predictive Control for Grid-Tied Quasi-Z-Source based Multilevel Inverter

Mohamed Trabelsi¹, Sertac Bayhan¹,², Haitham Abu-Rub¹,³, Lazhar Ben-Brahim⁴, Pericle Zanchetta⁵
¹Department of Electrical and Computer Engineering, Texas A&M University at Qatar, Qatar Foundation, Doha, Qatar
²Department of Electronics and Automation, Gazi University, Ankara, Turkey
³Qatar Environment and Energy Research Institute (QEERI), HBKU, Qatar Foundation, Doha, Qatar
⁴Electrical Engineering Department, Qatar University, Doha, QATAR
⁵Department of Electrical and Electronic Engineering, University of Nottingham, United Kingdom
mohamed.trabelsi@qatar.tamu.edu

Abstract—In this paper, a finite control set Model Predictive Control (MPC) for grid-tie quasi-Z-Source (qZS) based multilevel inverter is proposed. The proposed Power Conditioning System (PCS) consists of a single-phase 2-cell Cascaded H-Bridge (CHB) inverter where each module is fed by a qZS network. The aim of the proposed control technique is to achieve grid-tie current injection, low Total Harmonic Distortion (THD) current, unity power factor, while balancing DC-link voltage for all qZS-CHB inverter modules. The feasibility of this strategy is validated by simulation using Matlab/Simulink environment.

Keywords—quasi-Z-Source Network; Power Conditioning System; Multilevel Inverter; Grid Integration.

I. INTRODUCTION

Power converters have become over the last decades an enabling technology for a wide range of renewable energy (RE) applications mainly due to their higher efficiency and performance in exploiting the energy from the sources. For instance in photovoltaic (PV) power generation systems, power converters are able to meet the increasing demand of load (extracting the maximum power), and injecting electric current to the grid with unity power factor. The rich diversity of applications require power electronic converters that have different power ratings operating at different voltage/current levels, and even having different types of dc input sources (current or voltage). Therefore, wide range of Multilevel Inverter (MLI) topologies have been developed over the years, particularly in the last decade to cater the needs and fulfill the specifications of each niche. MLIs can handle high volt/current by means of advanced medium-power semiconductor technology [1-2]. Several surveys have introduced these topologies [1, 3]. Indeed, using the same switching frequency, the output waveforms can be improved comparing with the classical two-level inverter topologies. Among the well-known MLI topologies, cascaded H-bridge (CHB) inverters are characterized by their reduction of filtering elements, high modularity, high flexibility in the multilevel voltage synthesis, high fault tolerance, and high reliability (presence of redundant states which gives flexibility in selecting switching control approaches for optimized output performance) [4-5]. Nevertheless, like any other inverter topology, the H-bridge module misses the boost feature. Thus, the integration of DC-DC boost converter between the DC source and the H-Bridge inverter is vital to get the required boosted AC voltage. This additional boost converter increases the cost, weight, size, control complexity, and lowers in turn the system efficiency and reliability. In addition, to have safe operation of the inverter (avoid short-circuit), a dead-time should always be introduced, which results in distortion of the output voltage waveform (cyclical fluctuations).

Recently, a qZS inverter topology has been developed (improvement of the Z-source topology characterized by lower component ratings and continuous DC source current) for connecting PV modules to the load/grid. This is a single-stage power converter topology that employs a capacitor-inductor network and has voltage-boost and voltage-buck capabilities [6-8]. The qZS-network utilizes shoot-through states to boost the input voltage and regulate the DC link voltage for the inverter. The peak DC link voltage appears across the load terminals during the active states of the inverter. Then, the DC link voltage is pulsating in nature between zero and peak DC link voltage. Moreover, a qZS-CHB topology for grid-tie PV systems was proposed in [9-14]. This mix-topology is characterized by high-quality staircase output voltage with lower harmonic distortions, independent DC-link voltage compensation with a special voltage step-up/down function in a single-stage power conversion, and independent control of power delivery with high reliability [13]. Moreover, this inverter solves the imbalance problem of DC-link voltage in traditional CHB inverters. It is worth noting that the accurate control of the DC-link peak voltage is very critical for the regulation of the amount of the total power delivered to the grid.

Usually, PID controllers used in conjunction with a modulation technique are the main solution for power electronic converters regulation. However many other advanced control methods have been developed in the past decades. Among them, MPC is one of the most promising control technique, because it combines in a very simple form the discrete nature of the
controller with the discrete nature of the power converter. MPC has been studied for nearly three decades [15] and is considered as one of the most advanced control theories available nowadays [16-23]. The development and application of Model-based Predictive Control was initially slowed down due to its high computational cost. However, in the last two decades, powerful digital control platforms have been developed, e.g., Field-Programmable Gate Arrays (FPGAs) and Digital-Signal-Processors (DSPs) have become the conventional solution for control of electrical and electronics engineering systems [24-25]. MPC is characterized by its capability to be used in a variety of processes and application and by its simplicity for advanced engineering systems with high number of dynamics, where hard-constraints, soft-constraints and non-linearities can be included easily into the control law. Conventional MPC is currently used in a wide range of fields from vehicle applications, thermal management [15], electrical drives to grid interfacing of renewable energies [26-31]. Moreover, MPC is considered as a real and effective solution to traditional controllers based on linear control theory and Pulse-Width-Modulation (PWM) [32-33]. Note that, [33] is the state-of-the-art in electrical systems based on power electronic converters where interchange of energy between different power sources is performed.

This paper first explains the principle of operation and mathematical modelling of the grid connected qZS-CHB topology. A finite set control MPC approach of the proposed system is then presented and discussed. The MPC structure is capable of generating unity power factor, while low THD current is delivered to the grid. Besides, the amount of total power delivered to the grid is regulated through a DC-link peak voltage control employed in every qZS-CHB module to balance the DC-link voltages (by controlling the shoot-through ratio). Simulations of the proposed system are conducted using Matlab/Simulink to validate the MPC technique. Simulation approach is applicable even for qZS-CHB inverters with a large number of cells.

II. THEORETICAL BACKGROUND

A. qZS-CHB topology

The proposed single-phase qZS based PCS is illustrated in Fig. 1. The shown system consists of two grid-tie CHB inverters through filtering inductors, where each cell is connected to qZS network. This network consists of two inductors, two capacitors and one diode. This switchless topology is used to interface the PV output voltage with the inverter input while having a boost capability.

The output voltage of the qZS-CHB inverter is multilevel type (5-level output voltage) resulting from the sum of the two module output voltages. This number of levels $L$ is given by:

$$L = 2n + 1$$

with $n$ is the number of cells.

B. Mathematical modeling

The qZS converter's operation modes can be alienated into two states; non-shoot-through and shoot-through states. During the non-shoot-through state, the inverter is controlled as a conventional H-Bridge inverter and the derivations of the state variables $i_{L;i}$, and $V_{c;i}$ for each cell ($i$ is the cell number) are obtained by (2) and (3).

$$C \frac{dV_{c;i}(t)}{dt} = i_{L;i}(t) - i_{g}(t)$$

$$L \frac{di_{L;i}(t)}{dt} = V_{in} - V_{c;i}(t)$$

In the shoot-through state, both switches in a same leg are turned on simultaneously. The system equations for this state are given by (4) and (5). The above-mentioned configurations as well as the different current and voltage polarities are illustrated in Fig. 2.

$$C \frac{dV_{c;i}(t)}{dt} = -i_{L;i}(t)$$

$$L \frac{di_{L;i}(t)}{dt} = V_{c;i}(t)$$

In addition, according to Fig. 1, the output voltage $V_{out}$ in terms of its current and filter parameters is given by:

$$V_{out}(t) = L_{f} \frac{di_{g}(t)}{dt} + r_{f} i_{g}(t) + V_{grid}(t)$$

![Fig. 1. Proposed 2-cell grid-connected power conditioning system](image1)

![Fig. 2. The operation modes of the qZS converter; (a) Non-shoot-through state, (b) shoot-through state](image2)
Considering \(T_{sw}\) as one switching cycle, \(T_0\) as the interval of the shoot-through mode, and \(T_1\) as the interval of non-shoot-through mode, their relationship is given by \(T_0+T_1=T_{sw}\) and the shoot-through duty ratio is calculated by \(D=T_0/T_{sw}\). Then, the capacitor voltages as well as the peak value (denoted by “\(^*\)”) of the DC-link voltage \(V_{in}\) can be obtained in steady state as given by (7).

\[
\begin{align*}
V_{C1} &= \frac{1-D}{1-2D} V_{in} \\
V_{C2} &= \frac{D}{1-2D} V_{in} \\
\hat{V}_m &= V_{C1} + V_{C2} = \frac{1}{1-2D} V_{in} = B V_{in}
\end{align*}
\]

where \(B\) is the boosting factor.

In order to generate the different voltage levels for the proposed topology, at non-shoot-through states, it is essential to control the switching variable \(S_0\) (i is the cell number and j is the switch number) in line with the following expression:

\[
V_{out} = V_{in} \sum_{i=1}^{C} (S_i - S_j)
\]

Including all voltage level redundancies, the total number of switching signal combinations is given by:

\[
C_s = 2^2 = 16
\]

Moreover, during the shoot-through states, three additional switching states can be noted. These switching combinations result from turning on at the same time both switches on the same leg for one of the cells or for both. Then, the total number of switching signal combination \(C_s\) becomes 19.

C. Model Predictive Control Strategy

The control objectives of the qZS-CHB based grid-tie PCS are the DC-link peak voltage regulation for all qZS-CHB modules, input current regulation in continuous mode, and power injection to the grid with unity power factor and low harmonic distortion. The overall control scheme shown in Fig. 3 is proposed to fulfill these purposes.

The shown scheme consists of three main stages, which are: 1) Generation of state variable references; 2) Model prediction; and 3) Cost function optimization.

1) Generation of references

As shown in Fig. 3, the phase-locked loop (PLL) senses the phase angle of the grid voltage to ensure the grid synchronization with unity power factor (the grid current is in phase with the grid voltage). Then a sine generator is used to generate the reference grid current. The reference inductor currents \(i_{L_i}^*\) are calculated by dividing the system power rating \(P\) over the input voltage \(V_{in}\) (10). The capacitor voltage references \(V_{c1}^*\) are also given by (4).

\[
\begin{align*}
\frac{d}{dt} (i_{L_i}) &= \frac{f^{k+1} - f^{k}}{T_i} \\
V_{c1}^{k+1} &= V_{c1}^k + \frac{T}{C_{c1}} (i_{L_i}^{k+1} - i_{L_i}^k) \\
i_{L_i}^{k+1} &= i_{L_i}^k + \frac{T}{L_{c1}} (V_{out}^k - V_{c1}^k) \\
i_{L_i}^k &= (1 - \frac{T_i}{L_{c1}}) i_{L_i}^{k-1} + \frac{T}{L_{c1}} (V_{out}^{k-1} - V_{c1}^{k-1})
\end{align*}
\]

3) Cost function

The proposed cost function has two objectives: minimize the error between the predicted grid current \(i_{L_i}^{k+1}\), inductor currents \(i_{L_i}^{k+1}\), and capacitor voltages \(V_{c1}^{k+1}\) and their references, and balance in turn the DC-link capacitor voltages. These control objectives are represented as follows:

\[
g = \sum_{i=1}^{n} \sum_{j=1}^{m} \lambda_{i,j} \left[ \left| i_{L_i}^* - i_{L_i}^{k+1} \right| + \left| V_{c1}^* - V_{c1}^{k+1} \right| + \left| i_{L_i}^* - i_{L_i}^{k+1} \right| \right]
\]

where \(\lambda_{i,j}\) and \(\lambda_{c}\) are the weighting factors, which can be adjusted according to the desired performance (the tuning of the weighting factors is done by trial and error strategy). The switching state that minimizes the cost function is chosen and then applied at the next sampling instant.
III. SIMULATION RESULTS

In order to validate the proposed concept, simulations were performed using MATLAB/SIMULINK® and results are presented to show the effectiveness of the proposed method in achieving grid-tie current injection, low current THD, and balancing the DC-link voltage for both qZS-CHB inverter modules. The system parameters are reported in Table I.

In the studied case, the peak value of the qZS-CHB reference grid current is set to 7A and the DC-link voltage reference \(v_{pn}^*\) is fixed at 240V \((B=1.6,\text{ with } B \text{ is the boosting factor})\). Thus, for the boost conversion mode, the qZS network is boosting the input voltage \(V_{in}(150\text{V})\) to the required reference value \(v_{pn}^*\) by varying the shoot through value \(D\). Fig. 4 shows the simulation results of the regulated DC-link voltage and capacitor voltages. It can be noted that the DC-link voltage is properly regulated around the reference value (240V), \(V_{c1}\) and \(V_{c2}\) are controlled around the reference values \((V_{c1}^*=195\text{V}, V_{c2}^*=45\text{V})\) given by (10).

Fig. 5 shows that the qZS inductor current is maintained in the continuous mode allowing reducing the input stress. In addition, Fig. 6 denotes a zoom of Fig. 4 and Fig. 5 presenting the evolution of the qZS variables with the shoot-through state. The lower part of the figure shows that the DC-link voltage is properly regulated around the reference value (240V), \(V_{c1}\) and \(V_{c2}\) are controlled around the reference values \((V_{c1}^*=195\text{V}, V_{c2}^*=45\text{V})\) given by (10).

Fig. 7 shows that the qZS inductor current is maintained in the continuous mode allowing reducing the input stress. In addition, Fig. 6 denotes a zoom of Fig. 4 and Fig. 5 presenting the evolution of the qZS variables with the shoot-through state. The lower part of the figure shows that the DC-link voltage is properly regulated around the reference value (240V), \(V_{c1}\) and \(V_{c2}\) are controlled around the reference values \((V_{c1}^*=195\text{V}, V_{c2}^*=45\text{V})\) given by (10).

Table I. Simulation Parameters

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Total output power (P_{out})</td>
<td>1.2 kW</td>
</tr>
<tr>
<td>AC grid RMS voltage (V_{grid})</td>
<td>240V</td>
</tr>
<tr>
<td>qZS inductances (L_{1}, L_{2})</td>
<td>2.5 mH</td>
</tr>
<tr>
<td>qZS capacitances (C_{1}, C_{2})</td>
<td>4.7 mF</td>
</tr>
<tr>
<td>Filtering inductance (L)</td>
<td>1 mH</td>
</tr>
<tr>
<td>PV array voltage for qZS-HBI module (V_{in})</td>
<td>150 V</td>
</tr>
<tr>
<td>AC load frequency (f)</td>
<td>50 Hz</td>
</tr>
</tbody>
</table>

Fig. 8 shows the current THD is given in Fig. 8. The 5-level output voltage is shown in Fig. 9. Finally, Fig. 10 shows the measured total output power as well as the grid current and the qZS inductor current during a step change of the active power reference.

Fig. 4. qZS DC-Link voltage
IV. CONCLUSIONS

A finite control set MPC for grid-tie qZS based multilevel inverter has been proposed in this paper. The proposed system consists of a single-phase 2-cell CHB inverter where each module is fed by a qZS network. The suggested multi-objective control strategy ensured the tracking of the grid current, qZS inductor currents and capacitor voltages with respect to their references, while balancing the DC-link voltage for both qZS-CHB inverter modules. Grid-tie current injection with low THD and unity power factor has been achieved. The feasibility of this strategy has been validated in simulation using Matlab/Simulink environment.

ACKNOWLEDGMENT

This publication was made possible by the NPRP-EP award [X-033-2-007] from the Qatar National Research Fund (a member of Qatar Foundation). The statements made herein are solely the responsibility of the authors.