Experimental Investigations of Polymer Hollow Fibre Heat Exchangers for Building Heat Recovery Application

Xiangjie Chen¹, Yuehong Su¹, Devrim Aydin¹, David Reay², Richard Law², Saffa Riffat¹

¹Department of Architecture and Built Environment, University of Nottingham, University Park, NG7 2JQ, Nottingham. United Kingdom
²David Reay & Associates, United Kingdom

Contact: Xiangjie Chen; Email:xiangjie.chen@nottingham.ac.uk

Abstract: Due to low cost, light weight and corrosion resistant features, polymer heat exchangers have been extensively studied by researchers with the aim to replace metallic heat exchangers in a wide range of applications. Although the thermal conductivity of polymer material is generally lower than the metallic counterparts, the large specific surface area provided by the polymer hollow fibre heat exchanger (PHFHE) offers the same or even better heat transfer performance with smaller volume and lighter weight compared with the metallic shell-and-tube heat exchangers. This paper presents the construction and experimental investigations of polypropylene based polymer hollow fibre heat exchangers in the form of shell-and-tube. The measured overall heat transfer coefficients of such PHFHEs are in the range of 258-1675W/m²K for water to water application. The effects of various parameters on the overall heat transfer coefficient including flow rates and numbers of fibres, the effectiveness of heat exchanger, the number of heat transfer unit (NTU), and the height of transfer unit (HTU) are also discussed in this paper. The results indicate that the PHFHEs could offer a conductance per unit volume of 4*10⁶W/m³K, which is 2~8 times higher than the conventional metal heat exchangers. This superior thermal performance together with its low cost, corrosive resistant and light weight features make PHFHEs potentially very good substitutes for metallic heat recovery system for building application.

Key words: Polymer hollow fibre, heat recovery, heat exchanger, heat transfer, experimental testing

Nomenclature

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
<th>Units</th>
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<tbody>
<tr>
<td>A</td>
<td>Heat transfer area (m²)</td>
<td></td>
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<tr>
<td>Cp</td>
<td>Specific heat (J/Kg K)</td>
<td></td>
</tr>
<tr>
<td>CUV</td>
<td>Conductance per unit volume (W/m³K)</td>
<td></td>
</tr>
<tr>
<td>D</td>
<td>Tube/shell diameter (m)</td>
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<tr>
<td>Gz</td>
<td>Graetz number</td>
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<tr>
<td>HTU</td>
<td>Height of transfer unit (m or cm)</td>
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</tr>
<tr>
<td>k</td>
<td>Thermal conductivity (W/mK)</td>
<td></td>
</tr>
<tr>
<td>L</td>
<td>Length (m)</td>
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</table>
36 $\dot{m}$ Mass flow rate (kg/s)
37 $N$ Number of fibres inside the heat exchanger
38 NTU Number of heat transfer unit
39 Nu Nusselt number
40 $\Delta P$ Pressure drop (Pa)
41 Pr Prandtle number
42 $Q$ Heat transfer rate (W)
43 $\dot{V}$ Volumetric flow rate ($m^3/s$)
44 $R$ Thermal resistance ($m^2/KW$)
45 Re Reynolds number
46 St Stanton number
47 $T$ Temperature (°C)
48 $U$ Overall heat transfer coefficient (W/m$^2$K)
49 $V$ Volume ($m^3$)

50 **Greek Letters/Subscripts**

51 $\alpha$ Surface to volume ratio ($m^2/m^3$)
52 c,i Cold side inlet
53 c,o Cold side outlet
54 $\varepsilon$ Heat exchanger effectiveness
55 i Inside
56 $\lambda$ Packing fraction of a PHFHE equals to $ND_0^2/D_S^2$
57 h,i Hot side inlet
58 h,o Hot side outlet
59 lm Logarithmic mean
60 o Outside
61 ov Overall
62 $\rho$ Density of the fluid (kg/m$^3$)
63 s Shell side
In the era of rapid global economic development, the growing world energy use has triggered problems such as primary energy supply difficulties and world-wide environmental concerns (carbon emission, global warming, air pollution, etc). In developed countries, the energy consumption of buildings account for 20-40% of the total final energy consumption [1]. Heat recovery systems in the form of air ventilation systems [2-5], membrane heat exchangers [6,7], metal heat exchanger [8,9] have been extensively studied by researchers with the aim to improve energy efficiency and reduce energy costs for building applications. Most of such heat recovery systems are made from metallic materials, which have the disadvantages in terms of weight and cost. In addition, specially treated metal heat exchanger is needed if the working fluids are corrosive. Moreover, the manufacturing process of metal materials consumes significant amount of primary energies, accompanied by carbon emissions. Given these considerations, it is desirable to find an alternative material for heat exchangers that can overcome these disadvantages and also acquire comparable heat exchange efficiency and be easily fabricated. This is where the use of polymer heat exchanger comes into place. With the advantages of greater fouling and corrosion resistance, greater geometric flexibility and ease of manufacturing, reduced energy of formation and fabrication, and the ability to handle liquids and gases (i.e, single and two-phase duties), polymer heat exchangers have been widely studied and applied in the field of evaporative cooling system [10,11], micro-electronic cooling devices [12,13], water desalination systems [14,15], solar water heating systems [16,17], liquid desiccant cooling systems [18,19], etc. The detailed research progresses and various applications of polymer hollow fibre heat exchanger can be found in the review paper [20]. Most importantly, polymer materials can offer substantial weight, space, and volume savings, which make them more competitive compared with heat exchangers manufactured from many metallic alloys. Moreover, the energy required to produce a unit mass of polymers is about two times lower than common metals, making them environmentally attractive [21].

One of the drawbacks of polymer materials are their relatively low thermal conductivities, typically in the range of 0.1 to 0.4 W/m²K, which is about 100-200 times lower than the metal materials. In order to overcome this obstacle and increase the thermal performance of polymer heat exchanger, researchers have studied the polymer heat exchangers with various configurations: gas to air heat exchanger with triangular channels [22], shell and tube or immersion coil fluoropolymer heat exchanger [23], air to water heat exchanger with rectangular channel plate [24], plastic falling-film evaporator [25]. But the overall heat transfer coefficients achieved were still very low, which were in the range of 341-567 W/m²K, with the fibre outside diameter between 2.54mm and 9.53mm.
The relatively low overall heat transfer coefficients can be improved and reach values comparable to metal heat exchangers, when the heat exchanger is made from polymer micro-hollow fibre with fibre wall thickness below 100µm. Several researches have been focused on the heat transfer mechanism of polymer micro-hollow fibre heat exchangers (PHFHE), with inside and outside diameter (ID and OD) less than 0.1mm. Bourouni et al. presented experimental data on a falling film evaporator and condenser made of 2.5 cm diameter circular PP tubes (wall thickness of 5 mm) used in an ‘aero-evapo-condensation process’ for desalination. The results showed that for the same thermal performance, such polymer heat exchanger was 2-3 times cheaper than its metal counterpart. Zarkadas and Sirkar reported polymeric hollow fibre heat exchangers (PHFHE) for low temperature (up to 150-200°C) applications. The overall heat transfer coefficients for the water-water, ethanol-water, and steam-water systems reached 647-1314, 414-642, and 2000 W/(m²K), respectively. An olefin/paraffin distillation system using hollow fibre structured packings (HFSP) was proposed by Yang et al. This group of researchers recently scaled up the experiment and long-term operational testing results were obtained and reported (Yang et al.). The results demonstrated that after long-term exposure to light hydrocarbon environments (≤70°C), the mechanical properties of the PP polymer did not degrade significantly. Astrouski I. et al. studied the fouling effect of polymeric heat exchanger made from PP (inner and out fibre diameter of 0.461mm and 0.523mm respectively) for the purpose of cooling TiO₂ suspension. The experimental test results showed a very high overall heat transfer coefficient, with up to 2100W/m²K for clean conditions and 1750W/m²K for dirty conditions at the flow velocity of 0.05m/s. Zhao et al. presented a numerical analysis of a novel PP hollow fibre heat exchanger for low temperature applications using FLUENT. The heat transfer coefficient of PP fibres was predicted to be achieved at 1109W/m²K with inside and outside fibre diameters of 0.6mm and 1mm respectively.

The lack of extensive experience and testing data for polymer hollow fibre plastic heat exchanger and the unwillingness of industry partners to depart from well established metal heat exchanger remain to be big barriers for the wide applications of this technology. With the aim to experimentally investigate the effects of various working flow rates and number of fibres on the overall heat transfer coefficients, and to validate the theoretical simulation model developed by the authors, three different modules of polymer hollow fibre heat exchanger (fibre ID of 450µm and OD of 550µm) were fabricated and tested in the laboratory testing conditions. The effects of various parameters on the overall heat transfer coefficient including flow rates, numbers of fibres, the effectiveness of heat exchanger, the number of heat transfer unit (NTU), and the height of transfer unit (HTU) are discussed in this paper. The experimental obtained overall heat transfer coefficient and overall conductance per unit volume for PHFHE are compared with these of metal heat exchangers. The experimental uncertainties occurred associated with the measurement of flow rates and working fluid temperatures, etc. are also analysed.

2. Theory
Assuming there is no heat loss to the surrounding, the overall heat transfer rate \( Q \), between the shell side and tube side fluids, is defined by the flow rates of the hot and cold fluids flow rates and their inlet and outlet temperatures, as shown in the following equation:

\[
Q = \dot{m}_t \, c_{p,t} \, (T_{c, o} - T_{c, i}) = \dot{m}_s \, c_s \, (T_{h, i} - T_{h, o})
\]

Eq. (1)

Where subscript \( t \) denotes tube side and \( s \) denotes shell side.

The overall heat transfer coefficient \( U \), can be given by:

\[
U = \frac{Q}{(A \Delta T_{lm})}
\]

Eq. (2)

Where \( Q \) is an average heat transfer rate value between two fluids;

\( A \) is the heat transfer area (for hollow fibre heat exchanger, \( A \) is the total inside surface area of the hollow fibres);

\( \Delta T_{lm} \) is the logarithmic mean temperature difference (LMTD), and is defined as:

\[
\Delta T_{lm} = \frac{\Delta T_1 - \Delta T_2}{\ln[\Delta T_1 / \Delta T_2]}
\]

Eq. (3)

Here \( \Delta T_1 \) and \( \Delta T_2 \) are the temperature differences between two fluids at each end of a heat exchanger. In our case, for counter-flow heat exchanger

\[
\Delta T_1 = T_{h, i} - T_{c, o} \quad \Delta T_2 = T_{h, o} - T_{c, i}
\]

Eq. (4)

The heat exchanger effectiveness \( \varepsilon \), number of transfer unit (NTU) and the height of transfer unit (HTU) can be calculated using the following equations:

\[
\varepsilon = \frac{U_i A_i}{C_{min}} \frac{\Delta T_{lm}}{T_{h,i} - T_{c,i}}
\]

Eq. (5)

\[
\text{NTU} = \frac{U_i A_i - U_o A_o}{C_{min}}
\]

Eq. (6)

\[
\text{HTU} = \frac{L}{\text{NTU}}
\]

Eq. (7)

Where \( L \) is the length of the heat exchanger and \( C_{min} \) is given by:

\[
C_{min} = \{\dot{m}_t C_t, \, \dot{m}_s C_s\}_{min}
\]

Eq. (8)

The performance comparison between PHFHEs and existing metal heat exchangers should be made on a volumetric basis, so the so-called overall conductance per unit volume\(^{14}\) (CUV) is defined, which is the product of the heat transfer coefficient and the surface to volume ratio \( \alpha \):

\[
\text{CUV} = \alpha U
\]

Eq.(9)
CUV in this case expresses the total amount of heat transferred per unit time and unit volume. A higher CUV value indicates a more compact heat exchanger which can offer the same thermal performance, or a heat exchanger that transfers more heat for the same heat exchanger volume.

The surface to volume ratio $\alpha$ of the PHFHE is the ratio between the fibre inside area to the volume of the heat exchanger, which can be calculated by:

$$\alpha = \frac{A_i}{V} = \frac{4ND_i}{D_s^2}$$  \hspace{1cm}  \text{Eq.(10)}

In fluid dynamics, the Graetz number ($Gz$) is a dimensionless number that characterizes laminar flow in a conduit. This number is useful in determining the thermally developing flow entrance length in ducts. As stated by Hewit et al.\textsuperscript{33}, small values of $Gz$ ($Gz < 20$) indicates that radial temperature profiles are fully developed inside the laminar flow tube. The $Gz$ number is defined as:

$$Gz = \frac{D_H}{L} Re \: Pr$$  \hspace{1cm}  \text{Eq.(11)}

Where

- $D_H$ is the diameter in round tubes or hydraulic diameter in arbitrary cross-section ducts (m);
- $L$ is the length;
- $Re$ is the Reynolds number and
- $Pr$ is the Prandtl number.

The theoretical tube side pressure drop for a PHFHE can be calculated based on Darcy-Weisban Equation as stated by\textsuperscript{34}:

$$\Delta P = fL \frac{\rho u^2}{2d_h}$$  \hspace{1cm}  \text{Eq.(12)}

Where $f$ is the flow resistance, also known as friction factor;

$\Delta P$ is the pressure drop of the tube side for PHFHE;

$\rho$ is the density of the water.

The shell side and tube side Reynolds number are calculated using following equation:

$$Re = \frac{D \cdot G}{\mu}$$  \hspace{1cm}  \text{Eq. (13)}

Where, $D$ is fiber inside/outside diameter for tube/shell side Reynolds number;

$\mu$ is dynamic viscosity of the tube/shell side fluid for tube/shell side Reynolds number;
\( G \) is fluid mass velocity at the center line of the heat exchanger, detailed calculations could be referred to Kern\textsuperscript{35}.

The relationship between the tube side Reynolds number and tube side linear velocity is described by Kern\textsuperscript{35} as following:

\[
Re_t = \frac{\rho^* D_t^* u_t}{\mu} \quad \text{Eq. (14)}
\]

The relationship between the shell side Reynolds number\textsuperscript{35} and shell side linear velocity can be found in\textsuperscript{35} as following:

\[
Re_s = \frac{\rho^* D_o^* u_s}{\mu} \quad \text{Eq. (15)}
\]

3. Apparatus and procedure

Polypropylene (PP) hollow fibres (manufactured by ZENA Ltd.) with outside diameter of 550\( \mu \)m and inside diameter of 450 \( \mu \)m were used for the fabrication of three modules, with their geometrical information listed in Table 1. The shell side tube diameter was 15mm for Module 1 and Module 2 and 22mm for Module 3. The three modules were fabricated in the following way: The two ends of the fibres in a bundle were glued together first using PTFE resin. The fibre bundle was then inserted into a plastic tubing which was connected by two tee fittings, as shown in Figure 1. The fibre bundle was sealed with the two ends of the plastic tubing and the excessive length of fibres was cut. The two ends of the plastic tubing can be connected with a water loop, so they serve as the inlet and outlet of one water flow. The tube side hot water and shell side cooling water are in the counter flow direction. The detailed images and testing rig of PHFHE modules could be found in Figure 1.

![Figure 1 - a PHFHE heat exchanger](image)

A: PHFHE heat exchanger (fibre number: 100 and 200)  
B: PHFHE heat exchanger cross section view (not to scale)
The schematic diagram of the experimental testing rig for the heat transfer measurement is shown in Figure 2. A 10 kW electric heater which could provide hot water up to 80°C, was used to provide hot water for the PHFHE module. Each time before starting the test, the heater was pre-setted to the required testing hot water condition. As soon as the hot water temperature reached the desired testing value, the test was ready to start. In order to remove any particulate matter and avoid blocking the hollow fibres, two micro filters (5 µm) for both shell and tube sides were introduced before hot water and cooling water entering into the PHFHE. The hot water feed was then introduced to the shell side of the PHFHE module from the electric heater by a centrifugal pump at a constant flow rate (0.1-0.6l/min) which was controlled by a ball valve. Tap water with the temperature around 14-16°C was used as the cooling water, which passed through the shell side of the PHFHE at constants flow rates (0.2-2.0l/min) controlled by a ball valve. In all runs, the hot water and cooling water went in counter flow directions. The inlet and outlet temperatures and pressures of two streams were measured by K type thermocouples and pressure sensors (Ge UNIK 5000) with the accuracy of ±0.2% and ±0.5% respectively.

The experimental procedures applied for the tests are as following: Firstly the hot water flow rate was maintained at a fixed value, while the cooling water flow rates were varied from 0.2-2.0l/min with 0.2l/min increments. Temperatures of the inlet and outlet of the two streams were recorded every 10 seconds by a DT800 data taker, until two to five subsequent readings did not differ by more than ±0.1°C. The hot water inlet temperature was varied between 38°C to 69°C, while the cooling water inlet temperature was kept between 14°C and 16°C.
4. Results and Discussion

In order to obtain the overall heat transfer coefficients, the heat transfer rate $Q$ should be determined by the mass flow rate and the temperature difference for the tube side or shell side. Figure 3 presents the experimentally obtained overall heat transfer coefficients under the conditions when the tube side flow rate was 0.5l/min, and the shell side flow rates were varied between 0.2l/min and 2.0l/min. It can be found that when the shell side flow rate is less than 0.8l/min, the overall heat transfer coefficient calculated from the thermal capacity change $Q_h$ of tube side is higher than that calculated from the thermal capacity change $Q_c$ of shell side. When the shell side flow rate is higher than 0.8l/min, the situation is reversed. The difference between the $U$ values calculated from the respective change of the thermal capacity of two streams tends to increase largely as the shell side flow rate increases. However, the difference of the $U$ values obtained by two streams is less than 10%, with the discrepancy being amplified by the fact that very low flow rate was applied in the tube side. As the shell side is well thermally insulated, heat loss may have a smaller effect on this discrepancy. So, in order to compensate and reduce the discrepancy, the average $Q$ values between the two streams are used for the following analysis and discussions, as presented in the rest of the paper.
Table 2 Representative experimental testing data for the heat transfer measurement of PHFHE

<table>
<thead>
<tr>
<th>Th,i (°C)</th>
<th>Th,o(°C)</th>
<th>Tc,i (°C)</th>
<th>Tc,o (°C)</th>
<th>(m_t) (l/min)</th>
<th>(m_s) (l/min)</th>
<th>(U_o) (W/m² K)</th>
<th>(\varepsilon)</th>
<th>NTU</th>
<th>HTU (cm)</th>
</tr>
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<tbody>
<tr>
<td>Module 1 N=100</td>
<td></td>
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<tr>
<td>49.4</td>
<td>23.9</td>
<td>14.9</td>
<td>19.0</td>
<td>0.3</td>
<td>2.0</td>
<td>1675</td>
<td>0.741</td>
<td>1.461</td>
<td>18.9</td>
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<td>42.3</td>
<td>26.8</td>
<td>13.5</td>
<td>18.9</td>
<td>0.5</td>
<td>1.6</td>
<td>1609</td>
<td>0.539</td>
<td>0.860</td>
<td>26.0</td>
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<td>51.9</td>
<td>41.6</td>
<td>15.6</td>
<td>35.3</td>
<td>0.4</td>
<td>0.2</td>
<td>767</td>
<td>0.711</td>
<td>1.235</td>
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<tr>
<td>69.8</td>
<td>43.8</td>
<td>15.6</td>
<td>39.4</td>
<td>0.55</td>
<td>0.6</td>
<td>857</td>
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<td>1010</td>
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<td>44.7</td>
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<tr>
<td>52.0</td>
<td>19.2</td>
<td>13.9</td>
<td>23.4</td>
<td>0.5</td>
<td>2.0</td>
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<td>16.6</td>
<td>0.1</td>
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<td>741</td>
<td>0.550</td>
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</table>

We select some typical testing data for the heat transfer measurement of PHFHE and summarize them in Table 2. These include the hot water and cooling water inlet and outlet temperature, the mass flow rate of the two streams, the calculated total heat transfer rate, and the overall heat transfer coefficient, the heat exchanger effectiveness, the number of transfer unit (NTU) and the height of transfer unit (HTU). We can see that the overall heat transfer coefficients for such PHFHE device could reach up to 1675 W/m² K for a piece of tubing with shell side diameter of 15mm and length of 14cm. In the literature, the designed value for tubular metal heat exchanger is around 1100-1400 W/m² K, which is even lower than the experimental testing results of such PHFHE device. Inspection of the data in Table 2 also shows that the high value of effectiveness and NTU, up to 0.991 and 5.065 respectively, could be achieved for such PHFHE device. These values correspond to a very small HTU of...
only 2.8 cm, which is in good agreement with HTU obtained in microporous fibre membrane-based separation process\textsuperscript{37}.

![Figure 4 Variations of experimental obtained overall heat transfer coefficients with respect to various tube side liner velocities (Module 1, hot water inlet temperature 48.5 °C)](image)

In order to understand the relationship between the overall heat transfer coefficient and the fluid velocity in both shell and tube side, we present the variations of $U$ value with tube side linear velocities when the shell side linear velocity changes from 2265 cm/min to 11323 cm/min. We can find from Figure 4 that higher tube side linear velocity will contribute to better overall heat transfer coefficient when the shell side linear velocity is at fixed value. For instance, for shell side linear velocity at 6794 cm/min, the overall heat transfer coefficient increases about 1.8% from 1405 W/m\textsuperscript{2}K to 1430 W/m\textsuperscript{2}K when the tube side linear velocity increases from 188 cm/min to 252 cm/min. Moreover, a common feature can be observed is that when the tube side linear velocity increases, the $U$ value reaches a plateau quickly. The plateau $U$ value is around 1600 W/m\textsuperscript{2}K for the shell side linear velocity of 11323 cm/min, and 1000 W/m\textsuperscript{2}K for the shell side linear velocity of 2265 cm/min. When the tube side linear velocity is below 150 cm/min, the heat transfer coefficient seems to follow a linear dependence with respect to tube side linear velocity. We can introduce Gz number to help us better understand the mechanism. According to Hewitt et al.\textsuperscript{33}, Gz is a non-dimensional group applicable mainly to transient heat conduction in laminar pipe flow. Gz represents the ratio of the time taken by heat to diffuse radially into the fluid by conduction to the time taken for the fluid to reach distance. By calculating the Gz number according to Equation (11), we can see that the Gz number is in the range of 10 to 53 when the tube side linear velocity increases from 63 cm/min to 315 cm/min (the same range as shown in Figure 4). As stated by Hewit et al.\textsuperscript{33}, small values of Gz (Gz < 20) indicates that radial temperature profiles are fully developed inside the laminar flow tube. This means that when Gz number and tube side linear...
velocity are at lower values, forced convection is not the only mechanism for heat transfer, heat transfer by natural convection in the radial direction becomes more dominant.

Figure 5 presents the variations of U value to the various shell side linear velocities for PHFHE module 1. We can find that the U value will increase as the shell side linear velocity improves from 1132cm/min to 11320cm/min. Similarly to Figure 4, after the shell side linear velocity reaches to 11000cm/min, the U value maintains at a stale value for most of the cases. For instance, when tube side linear velocity is fixed at 126cm/min and 63cm/min, the plateau value of U is around 1600W/m²K and 1250W/m²K respectively.

![Graph showing the variations of U value with respect to shell side linear velocity](image)

Figure 5 Variations of experimental obtained overall heat transfer coefficients with respect to various shell side linear velocities (Module 1, hot water inlet temperature 48.5 °C)

Figure 6-8 depict the variations of overall effectiveness, NTU and HTU of PHFHE with respect to various shell side Reynolds numbers. We can find from Figure 8 that higher shell side Reynolds number will lead to higher overall effectiveness when the tube side Reynold is at fixed value. For instance, at the tube side Reynolds number of 104, the overall effectiveness changes from 0.773 to 0.793 when the shell side Reynolds number increases from 863 to 1151. Figure 6 also reveals that at fixed shell side Reynolds number, the overall effectiveness will decrease as the tube side Reynolds number increases. For example, at shell side Reynolds number of 576, the overall effectiveness decreases from 0.597 to 0.5 when the tube side Reynolds number increases from 156 to 207. Figure 7 shows that for most of the cases (about 83%), the NTU is higher than 1. As the PHFHE device mainly operates in laminar flow regime, Figure 7 also reveals that high NTU can be obtained at low tube side Reynolds number, which is in good agreement with the heat transfer literature. Inspection of Figure 6 and 7 also shows that, the overall effectiveness first decreases and then increases as the shell side Re number improves. The reason is because that, according to Eq. (5), the effectiveness is proportional related to $C_{min}$, which is the minimum product of the flow rate
multiple by Cp for shell side and tube side. At lower shell side Re number (Re,s =144) and higher tube side Re number (Re,t>156), the effect of shell side flow rate on the effectiveness is more dominant. As the shell side Re number becomes higher than the tube side Re number, the effectiveness is more dependent on tube side Re number. That is why there is a small fluctuation at lower shell side Re number.

From Figure 6-8, we can see that high value of heat exchanger effectiveness and NTU, 0.932 and 0.822 respectively, could be achieved at the tube side Reynolds number of 52 and shell side Reynolds of 1439. However, inspection of Figure 6-8 further indicates that relatively low effectiveness and NTU values, accompanied by high HTU also exist. This means that the rating of the PHFHE device is rather important. In order to achieve higher effectiveness and better thermal performance, the rating of PHFHE device should be performed properly.

Figure 6 Variations of overall effectiveness with respect to various shell side Reynolds number (Module 1, hot water inlet temperature 48.5 °C)
Figure 7 Variations of NTU with respect to various shell side Reynolds number (Module 1, hot water inlet temperature 48.5 °C)

![Graph showing variations of NTU with respect to various shell side Reynolds number.]

Figure 8 Variations of HTU with respect to various shell side Reynolds number (Module 1, hot water inlet temperature 48.5 °C)

Figure 9-11 show the comparisons of overall heat transfer coefficients, heat transfer rate and LMTD for different fibre numbers under various shell side Reynolds numbers, at fixed tube side Reynolds number. It can be found that at the same shell and tube side Reynolds number, the module with smaller fibre number produces higher overall heat transfer coefficient. For instance, at shell side Reynolds number of 288, the overall heat transfer coefficient decreases from 817.6 W/m²K to 523.5 W/m²K, till 481.9 W/m²K as the fibre number changes from 100, 200 to 400. The reason can be referred to Equation (2), the U value is closely related to the total heat transfer rate Q, ΔT\text{lm}, and the heat transfer area A. As shown in Figure 10, at shell side Reynolds number of 288, when the fibre number increases from 100 to 200, the total heat transfer rate increases about 29.1% from 214.8W to 277.3W. Figure 11 indicates that at the same condition, ΔT\text{lm} decreases about 0.7% from 11.6 °C to 9.9°C, as the fibre number increases from 100 to 200. In the meantime, the total heat transfer area improves twice as the fibre number increase from 100 to 200. Compares the abovementioned percentage difference, we can see that the change of fibre numbers plays more dominant role on the overall heat transfer coefficients. Therefore, the increase of fibre number will lead to the decrease of overall U value. This is also the reason as U value deceases when the fibre number increases with the variations of tube side Reynolds number, as shown in Figure 12.

Inspection of Figure 9-11 further reveals an interesting phenomenon: at lower shell side flow rate, the heat transfer rate stays very close for N=200 and N=100, while there is a much bigger difference for N=400 and N=200. For instance, at shell side Re number of 288, the Q value increases about 29.1% from 214.8 W/m²K to 277.3W as the fibre number increases from 100 to 200, while it soars about 64.2% from 277.3W to 605.6W as the fibre number improves from 200 to 400. On the other hand, at lower shell side flow rate, the overall heat
transfer rate for N=200 and N=400 are approaching each other, while there is a big gap between N=100 and N=200. Hence, when we design the PHFHE device, the fibre numbers should be selected properly in order to maintain effective heat transfer while making full uses of the fibre materials.

Figure 9 Comparisons of overall heat transfer coefficients for Module 1-3 under various shell side flow rate and at fixed tube side Reynolds number

Figure 10 Comparisons of heat transfer rate for Module 1-3 under various shell side flow rate and at fixed tube side Reynolds number
Figure 11 Comparisons of $\Delta T_{lm}$ for Module 1-3 under various shell side flow rate and at fixed tube side Reynolds number

Figure 12 Comparisons of overall heat transfer coefficients for Module 1-3 under various tube side flow rate and at fixed shell side flow rate of 1.6l/min

Table 3 Percentage contribution of tube side, shell side and fibre wall resistance to the overall resistance

<table>
<thead>
<tr>
<th>Module</th>
<th>Fibre number</th>
<th>Rt/Rov(%)</th>
<th>Rs/Rov (%)</th>
<th>Rw/Rov (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>100</td>
<td>4-10</td>
<td>35-56</td>
<td>18-31</td>
</tr>
<tr>
<td>2</td>
<td>200</td>
<td>3-8</td>
<td>38-62</td>
<td>15-28</td>
</tr>
<tr>
<td>3</td>
<td>400</td>
<td>2-7</td>
<td>40-66</td>
<td>13-25</td>
</tr>
</tbody>
</table>

Table 3 presents the percentage contribution of the three major resistances to the overall resistance. The results indicate that tube side resistance are the smallest of the three, therefore by increasing the tube-side Reynolds number, little improvement will be achieved for the
By increasing the fibre numbers from 100, 200 to 400, the overall heat transfer coefficients tend to decrease accordingly, and the percentage contribution of shell side resistance will play more dominant role.

Figure 13 Shell side Nu numbers with respect to Re and Pr number using two different correlations (correlation 1)

Figure 14 Shell side Nu numbers with respect to Re and Pr number using two different correlations (correlation 2)

Figure 13 and Figure 14 present the relationships between shell side Nu numbers and Re, Pr number using two different correlations from the literature. Both suitable for laminar flow conditions and validated by various authors, Hausen’s correlation and Delaware’s correlation were applied respectively for calculating the tube side heat transfer coefficients. Then, the shell side heat transfer coefficients and the shell side Nu number could be derived from the experimental obtained overall heat transfer coefficients. The Nu-Re plot shown in
Figure 13 and Figure 14 indicated very good agreement of shell side Nu numbers using two different correlations. A well correlated equation showing shell side Nu number as the function of Re and Pr number is also presented respectively in Figure 13 and Figure 14. The difference between the correlation presented in Figure 13 and Figure 14 is the exponent of shell side Re number. Comparing the discrepancy of the correlated equation with results obtained from Hausen’s and Delaware correlations, it can be found that the derived correlation 1 with exponent of 0.35 (in Figure 13) is more suitable for shell side Re number less than 200 or larger than 1200, with the minimum difference of 0.3%. While the derived correlation 2 with exponent of 0.32 (in Figure 14) is more close to results obtained from Hausen’s and Delaware correlations (with the minimum difference of 0.14%), when the shell side Re number is in the range of 200-1200.

![Figure 15](image)

Figure 15 Variations of theoretical and experimental obtained tube side pressure drops under different tube side Re numbers. (Module 1)

Figure 15 shows the comparisons of theoretical and experimental obtained tube side pressure drops under different tube side Re numbers for fibre number N=100. The theoretical tube side pressure drop is calculated using Eq. (12). The experimental tube side pressures of PHFHE are monitored by pressured transducer sensors (GE UNIK 5000). We can see from the diagram that increasing the tube side Re number will result in higher tube side pressure drop. Moreover, a liner relationship could be derived between experimental obtained Re number and tube side pressure drop with $R^2=0.99$. We can also find that the experimental obtained pressure drops are quite close to the theoretical values, with the minimum percentage difference of 5.6%. As the tube side Re number increase, the difference between the theoretical and experimental results decreases.
Figure 16 Comparisons of overall conductance per unit volume between PHFHE with conventional heat exchangers

Figure 16 shows the comparisons of overall conductance per unit volume between PHFHEs with conventional metal and plastic heat exchangers. A compact metal heat exchanger with wall thickness of 0.4mm, a plate heat exchanger with 0.4mm thickness, and a PEEK plate heat exchanger are chosen for comparisons. We can see from Figure 15 that PHFHE modules generally demonstrate higher CUV values (about 2-8 times) compared with conventional metal and plastic heat exchangers. Despite the relatively low overall heat transfer coefficients, the large surface area to volume ratio of PHFHEs offers controlling factor of performance on a volumetric basis. For instance, for PHFHE module 3 (fibre number=400), the CUV values are about 7 times higher than the compact tube heat exchanger, and 1.5 times higher than the metal plate heat exchanger. However, the values in Figure 16 for the metal heat exchangers already represent the cutting edge of current technology. While the packing/manufacturing technology for the PHFHEs are currently only subjected to laboratory testing conditions. Hence, we could expect more area to be packed in the PHFHEs, and this will result in even better heat transfer performance and thermal capabilities, which exceeds greatly over the metal counterparts.
The uncertainty analysis of the experimental results shown in Figure 17 is performed using the methods proposed by Moffat. Considering all the measurement uncertainties for mass flow rates, temperatures, and fibre diameters, the experimental uncertainties for the overall heat transfer coefficients is between ±7.1% and ±9.8%. Based on the experimental inlet and outlet streams conditions, the simulation programme developed by the authors was applied and results are presented in Figure 15. We also plot two curves showing the deviations of ±5% from the experimental obtained results. We can find that, in general, the simulation results fall in good agreement with the experimental data, with differences less than 5%.

5. Conclusion

The PP based polymer hollow fibre heat exchangers were manufactured and tested under various shell (0.2-2.0l/min), tube side flow rate (0.1-0.6l/min) and tube side water temperatures (40-70°C). The maximum experimental obtained overall heat transfer coefficients were achieved in module 1 of PHFHE, with the U values between 1700-1800W/m²K. These values are higher than other results reported in literature for water to water applications in polymer hollow fibre heat exchanger.

Three different PHFHE modules with fibre numbers of 100, 200 and 400 were manufactured and the thermal performances were compared in the tests. The experimental obtained overall heat transfer coefficients were 758-1675W/m²K, 369-1453W/m²K and 296-1201W/m²K respectively for Module 1, 2 and 3. This indicates that module 1 offers higher U value compared with the other two modules.

By changing the tube and shell side flow rate, the effectiveness, NTU and HTU of PHFHE modules are also investigated. With the active length of 14cm, the module 1 of PHFHE could
attain high value of effectiveness and NTU, up to 0.991 and 5.065 respectively. The HTU achieved was as low as 2.8cm, about 35 times less than the lower limit for shell and tube heat exchangers and 20 times lower than typical values for plate heat exchangers. Such results demonstrate that if PHFHE devices could be rated and designed properly, they could achieve relatively high NTU in a single module.

Since the surface area per unit volume in such PHFHEs is quite high, in the range of 880-3600 m²/m³, their volumetric rate of heat transfer is very high. Comparisons of CUV between PHFHEs and metal heat exchangers reveals that the CUV values of PHFHEs are approximately 2-7 times higher than the metal counterparts. This superior performance can result in potentially more compact designs based on PHFHE devices, for water desalination, solar water heating system, and automotive applications. Therefore, the superior thermal performance, and large heat transfer areas, and the advantages of low price and light weight of polymer materials, make PHFHEs a promising substitute over conventional metal heat recovery system for building application.

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Reference


