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Foreword and Colophon

This paper reports on work performed in 2005–6 by my grad. student Benji Kelly, which eventually formed a major part of his Masters (M.Phil) thesis here at the University of Nottingham. He then went on to do a PhD at Cornell University.

Benji’s work began with an interest in Golomb coding but he soon extended the scope of his researches to take in adaptive binary arithmetic coding. The paper presented here was submitted to the annual Data Compression Conference in 2006 (DCC 2006). These conferences are held in Snowbird, Utah and are very well regarded in the DCC field. Although our paper was accepted only as a poster, we felt rather pleased to have had success of some sort at our first attempt.

The version here is the original, unabbreviated, submission to DCC.

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David F. Brailsford. February 2015.
The B-coder: An improved binary arithmetic coder and probability estimator

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Abstract

In this paper we present the B-coder, an efficient binary arithmetic coder that performs extremely well on a wide range of data. The B-coder should be classed as an ‘approximate’ arithmetic coder, because of its use of an approximation to multiplication. We show that the approximation used in the B-coder has an efficiency cost of 0.003 compared to Shannon entropy. At the heart of the B-coder is an efficient state machine that adapts rapidly to the data to be coded. The adaptation is achieved by allowing a fixed table of transitions and probabilities to change within a given tolerance. The combination of the two techniques gives a coder that outperforms the current state-of-the-art binary arithmetic coders.

1 Background

Arithmetic coding (AC) is a technique for data compression that theoretically allows us to code data at Shannon entropy. The idea was first developed by Pasco[1], who was inspired by a proof of Shannon’s theorem, and shortly after by Rissanen[2]. The first practical implementation was by Langdon and Rissanen[3]. The basic idea in AC is to represent a series of choices between events as a selection of intervals (or regions) on the real line. Each choice can be viewed as a selection of a letter from an alphabet, \( \alpha \), and arithmetic coding as a way of representing strings from \( \alpha^* \). For each letter in \( \alpha \), an initial interval is allocated whose length is proportional to its probability. When the first letter is known, its region is selected and re-divided according to suitable probabilities. Langdon and Rissanen were the first to show that the issues of determining probabilities and performing the coding can be dealt with separately[4]. Their suggestion is to use a modelling unit to partition the data into conditioning classes or contexts, such that the members of a particular context share similar characteristics and therefore similar probabilities. An arithmetic coder can then exploit the similarity by coding the members of each class together. In this paper we make contributions to both practical arithmetic coding and probability estimation.

Traditionally, implementations of arithmetic coding track two variables: \( C \), the start of the interval and \( A \), the size of the interval, so at any point \([C, C + A]\) represents the current interval (alternative approaches exist, e.g. in[5] where the authors track \( L \) and \( H \), the endpoints of the coding interval.) Initially we have \( C_0 = 0 \) and \( A_0 = 1 \). For an \( n \)-ary
alphabet, where letter \( i \in 0...n - 1 \), has probability \( P(i) \), coding the event \( j \) proceeds as follows. Let \( W(j) \) be the alphabetic index of the \( j \)th character of the string to be encoded, then \( C \) and \( A \) become: \( A_j = A_{j-1} \times P(W(j)) \) and \( C_j = C_{j-1} + S(W(j)) \), where \( S(0) = 0 \) and \( S(k) = \sum_{l=0}^{k-1} P(l) \).

Binary arithmetic coding (BAC) is a special case of AC that allows for decisions between two events to be encoded. Conventionally we designate the two events MPS and LPS, for more-probable and less-probable symbol, and let \( \alpha = \{0, 1\} \). The initial region is the semi-open interval \([0, 1)\), which is first divided into two regions \( L \) (for the less-probable letter, assumed to be 1 in the equations below) and \( M \) (for the more-probable letter, assumed to be 0 in the equations below), such that \( L + M = 1 \) covers the entire region. For each event to be coded, the region corresponding to the event to be encoded is selected, and that new region is again divided in to \( L' \) and \( M' \). Note that the division of the region at each coding decision need not be the same, that is, it is not necessary for \( \frac{L}{L+M} = \frac{L'}{L'+M'} \). This allows a modelling unit to provide a BAC with a different estimate for LPS for each symbol, which coupled with the interval subdivision allows a BAC to achieve optimal compression without alphabet extension. In terms of the coding variables described above, binary arithmetic coding has a particularly simple implementation. Redefining \( A \) be a function from strings of \( \alpha \) i.e. \((0, 1)^*\) to interval size and \( C \) to be a function from strings of \( \alpha \) to interval start points, \( C \) and \( A \) can be defined using the following double recursion:

\[
\begin{align*}
A(s0) &= A(s) - A(s1) \\
A(s1) &= A(s) \times P(1) \\
C(s0) &= C(s) \\
C(s1) &= C(s) + A(s0)
\end{align*}
\]

In [3], Langdon and Rissanen developed a binary arithmetic coder, which we refer to as the Skew Coder[1]. Their motivation was to find a simple implementation of binary arithmetic coding that did not involve multiplication. (In the early days of arithmetic coding, the time taken to perform multiplication in hardware was very high compared to other machine operations.) In the skew coder, fixed-point arithmetic is carried out in \( n \)-bit registers. When the left-most bit of \( A \) is a zero, both \( A \) and \( C \) are shifted to the left until the left-most bit of \( A \) is a one, this overcomes the “growing precision” problem caused by the continual multiplication in step 2. The simplification in the skew coder is accomplished by approximating the multiplication in equation 2 with a right-logical-shift (\( \gg \)). If \( P(\text{LPS}) = 2^{-Q} \), equation 2 then becomes \( A(s1) = A(S) \gg Q \). The parameter \( Q \) is known as the skew value, and is supplied to the arithmetic coder in lieu of the probability estimate for the event to be coded. The skew coder performs surprisingly well on real data, given the crudeness of the approximation.

In search of further speed improvements, the skew coder was refined in [6], where the multiplication is replaced by assignment (and a corresponding shift of \( C \)). In this refinement

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1In recent literature there is some confusion about which of Langdon and Rissanen’s coders is the ‘skew coder’. Some authors refer to [3] and others (including IBM staff and some relevant US patents) cite [6]. However, [3] includes the first occurrence of the phrase ‘skew values’.
can be seen the beginning of the Q-coder \cite{7} and its variants (Q, QM, MQ). In each of these coders multiplication is replaced by assignment, which is possible when \( A \) is kept close to one. This approximation comes with some cost to coding efficiency, but at the time it was considered a worthwhile price to pay to avoid the costly multiplication. The secret weapon of the Q-coder and its descendants lies in their probability estimation; rather than relying on a modeller to supply the probability of each event to be coded, these coders estimate probabilities internally via an efficient state machine.

In this work we describe a new coder, the B-coder, which is based on the skew coder and in its simplest form has a worst case inefficiency of around 0.3\% above entropy. The B-coder incorporates an efficient state machine based loosely around the idea of ‘fast-attack’, as used in JPEG \cite{8}. However, unlike previous coders, our state machine allows the probabilities and transitions to fluctuate within a given tolerance, which further improves performance by between 0.1\% and 4\% depending on the statistics of the data being coded.

In section 2 we give the derivation of the B-coder. Its probability estimation is described in section 3. Results are presented in section 4 by comparing the B-coder to two other state-of-the-art coders. Finally, section 5 presents the conclusion.

## 2 Motivation and description of our code

Figure 1 shows a plot of entropy versus code length for the skew coder \cite{3}. The main peaks occur where the skew value does a poor job of approximating the true probability. Ideally, what we seek is a low-cost improvement to the probability approximation. The skew coder uses what is in effect a ‘one significant figure’ approximation to the actual LPS probability. If we allow a two-bit approximation, \( P(l) = 2^{-Q} + 2^{-R}, R > Q \) the approximation gets
slightly better, but this new approximation still has a noticeable peak near \( P(l) = 0.437 \) (see +Skew in figure [1]) Instead, we approximate using \( P(l) = 2Q \pm 2^{-R} \), \( R > Q \) and achieve a much tighter approximation. In terms of coding variables, this new approximation requires a minor modification: equation [2] becomes \( A(s1) = A(s0) \gg Q \pm A(s0) \gg R \); and the modelling unit now needs to supply two variables, \( Q \) and \( R \), to the coding unit. For simplicity, we allow the sign of \( R \) to determine whether \( A(s0) \gg R \) should be added or subtracted from \( A(s0) \gg Q \). In the description of the algorithm below, we use the \textit{signum} function, where \( \text{signum}(x) = 1 \) if \( x > 0 \), \( -1 \) if \( x < 0 \), 0 otherwise.

**Encoding Algorithm**

The inputs to the encoding are the bit, \( b \), to be encoded, plus \( Q \) and \( R \) supplied by the modeller.

1. (Initialise) Set \( C \) to 0 and \( A \) to all 1s.
2. Compute \( a1 := A \gg Q + \text{signum}(R) \times (A \gg |R|) \)
3. Compute \( a0 := A - a1 \)
4. If \( b = 0 \) set \( A := a1 \), else if \( b = 1 \) set \( A := a1 \) and \( C := C + a0 \).
5. (Renormalise) While the left-most bit of \( A \) is zero, set \( A := A \ll 1 \) and \( C := C \ll 1 \).

Note, in carrying out the addition of step 4 the quantity \( C + a0 \) may overflow the \( n \)-bit register, so the output shifted from the left end of \( C \) in the renormalisation step should be buffered, and if carry occurs, the carry should be propagated into the buffer. Additionally, as observed in [3] this carry may propagate through the entire buffer, so a method to block the carry must be used (e.g. bit-stuffing.)

**Decoding Algorithm**

The inputs to the algorithm are the code string plus skew parameters \( Q \) and \( R \), supplied by the modeller. The output is the decoded bit, \( b \).

1. (Initialise) Fill register \( C \) with the first \( n \) bits of the code string and fill \( A \) with 1s.
2. Compute \( a1 := A \gg Q + \text{signum}(R) \times (A \gg |R|) \)
3. Compute \( a0 := A - a1 \)
4. If \( a0 > C \) then set \( b := 0 \) and \( A := a0 \). Go to 6.
5. Otherwise \( a0 \leq C \), set \( b := 1 \), \( C := C - a1 \) and \( A := a0 \).
6. (Renormalise) While the left-most bit of \( A \) is zero, set \( A := A \ll 1 \) and \( C := C \ll 1 \).

Figure [1] shows the efficiency of the B-coder versus the binary entropy function. The B-coder’s worst-case efficiency is 0.3%, which occurs near \( P(\text{LPS})=0.346 \).
3 Probability estimation

In the previous section we described the B-coder without giving any consideration to probability estimation. For efficient compression a coder needs to have an accurate estimate of the probability of each symbol as it is compressed. A computationally ‘cheap’ approach is to use renormalisation-driven probability estimation, first used in the Q-coder (see [9] for a detailed analysis.) The basic idea is that the renormalisation step in the encoding algorithm can be used as a criterion to decide when to perform adaptation. When an LPS event causes a renormalisation (‘LPS-renorm’) we should increase the LPS probability estimate and for an MPS invoked renormalisation (‘MPS-renorm’) we should decrease it.

In the Q-coder and its descendants, the probability estimates are used directly when dividing the intervals during the coding process. The B-coder takes a similar approach. In the B-coder, we have constructed a set of $Q$ and $R$ values that can be used to estimate a range of LPS probabilities. Our table is arranged in a similar fashion to the ‘fast-attack’ (FA) tables of JBIG/JPEG. A table is ‘fast-attack’ when an uninterrupted sequence of MPS-renorms rapidly decreases the LPS probability, faster than would be warranted by the equations in [9]. In our tables, an early LPS-renorm moves the coder into a less confident state and two LPS-renorms move the coder into the steady-state mode, where the analysis from [9] is valid.

One characteristic shared by many table-driven probability estimators is that they are inherently static in nature. The estimated probabilities and transitions are drawn from the table and are always used. In the B-coder we break this paradigm and allow the table entries to fluctuate. The coder keeps track of the quantity MPS-renorms − LPS-renorms for each entry in the probability table and uses this figure as a confidence estimate about that probability. If a table entry has a positive confidence estimate, we can be sure that $P(\text{LPS})$ is lower than the table suggests (because we have had a net-positive number of MPS-renorms at this entry before), so we should compensate in some way. One method is to decrease $P(\text{LPS})$ by a small amount. The necessary adjustments can be achieved by letting the skew values change in some controlled manner.

<table>
<thead>
<tr>
<th>Effective Probability</th>
<th>Occupancy</th>
<th>Confidence Estimate</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.503 (1,-8)</td>
<td>183484</td>
<td>1358</td>
</tr>
<tr>
<td>0.492 (1,-7)</td>
<td>183722</td>
<td>-2515</td>
</tr>
<tr>
<td>0.484 (1,-6)</td>
<td>178534</td>
<td>-4026</td>
</tr>
<tr>
<td>0.375 (2,3)</td>
<td>170421</td>
<td>-16069</td>
</tr>
<tr>
<td>0.313 (2,4)</td>
<td>138650</td>
<td>-22321</td>
</tr>
<tr>
<td>0.266 (2,6)</td>
<td>93217</td>
<td>-22460</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Effective Probability</th>
<th>Occupancy</th>
<th>Confidence Estimate</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.109 (3,-6)</td>
<td>103682</td>
<td>9917</td>
</tr>
<tr>
<td>0.094 (3,-5)</td>
<td>151080</td>
<td>7556</td>
</tr>
<tr>
<td>0.064 (4,10)</td>
<td>155777</td>
<td>5982</td>
</tr>
<tr>
<td>0.059 (4,-8)</td>
<td>147105</td>
<td>3360</td>
</tr>
<tr>
<td>0.047 (4,-6)</td>
<td>122792</td>
<td>-321</td>
</tr>
<tr>
<td>0.030 (5,-10)</td>
<td>92726</td>
<td>-2389</td>
</tr>
</tbody>
</table>

Table 1: An sub-section of the effective probabilities used during the single-context coding of a pseudo-random distribution of binary events $P(\text{LPS})$=$P(\text{MPS})$=0.5 (left) and $P(\text{LPS})$=0.05 (right)
In the B-coder we use the following approach. Compare the confidence estimate with the number of times the context has been used (context occupancy), if the magnitude of the confidence estimate is at least 5% of context occupancy then suitably adjust both Q and R. This technique was motivated by observing the distribution of the probability states that were used during single-context coding (see table [1]). For data distributed with \( P(\text{LPS}) = 0.5 \), the probabilities used (effective probability) ranged from \( 2^{-1} \) to \( 2^{-3} \). A similar phenomenon was observed during single-context coding of any fixed-probability file, as expected according to the analysis in [9]. In this method, the confidence estimate allows the coder to detect when it is using an inappropriate effective probability and compensate proportionally. We found that letting Q and R assume the values from the entry \( \Delta \) states away in the ‘right’ direction worked best. (The ‘right’ direction is forward if the confidence estimate is positive and backwards if the confidence estimate is negative.) We used the update schedule shown in equation [5] (arrived at experimentally), where confidence level (cl) is confidence estimate/context occupancy.

\[
\Delta = \begin{cases} 
0, & \text{cl} < 5 \\
1, & 5 \leq \text{cl} < 15 \\
2, & 15 \leq \text{cl} < 35 \\
3, & 35 \leq \text{cl} < 55 \\
4, & 55 \leq \text{cl} 
\end{cases}
\] (5)

Even though this schedule and method were derived from single-context coding, we show in the next section that it improves performance even in mixed-context coding.

4 Coding Results and Analysis

To assess the performance of the coder we performed a number of tests on real world data ranging from single context coding through to multi-context bi-level image coding. We present the results in this section. Additionally, for comparison purposes, we include in each test results from the Augmented-ELS coder [10] and the Z-Coder [11]. In the tables of results that follow the entry labelled “B-coder + dynamic state” gives the performance of the coder with the probability model as from section 3. The entry labelled “B-coder + static state” gives the performance of the B-coder with the adaptation disabled, i.e. using only the probabilities and transitions defined by the initial state machine. In each table the best result in each row is underlined.

4.1 Single context coding

To test the efficacy of the coder, we compressed a million ‘random’ bits generated according to a fixed probability distribution. The results are presented in table [2]. Overall, the Z-coder fares well in these tests, which is to be expected. The Z-coder is developed from Golomb’s run-length code [12], and these files follow precisely the geometric distribution that Golomb’s code was designed for. In all but two tests, the B-coder outperforms the Augmented ELS coder. In the first four tests, the B-coder outperforms the Z-coder.
Table 2: A comparison of the B-coder against the ELS- and Z-coder for single context with fixed less probably symbol probabilities. Entropy column is number of bits, coder performance figures are percentage over entropy.

<table>
<thead>
<tr>
<th>P(LPS)</th>
<th>Entropy</th>
<th>B-coder + static state</th>
<th>B-coder + dynamic state</th>
<th>ELS Coder</th>
<th>Z-Coder</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.50</td>
<td>1000000</td>
<td>2.79</td>
<td>1.32</td>
<td>8.38</td>
<td>2.99</td>
</tr>
<tr>
<td>0.40</td>
<td>970951</td>
<td>3.04</td>
<td>2.32</td>
<td>8.12</td>
<td>2.52</td>
</tr>
<tr>
<td>0.30</td>
<td>881291</td>
<td>2.80</td>
<td>1.77</td>
<td>7.07</td>
<td>2.54</td>
</tr>
<tr>
<td>0.20</td>
<td>722656</td>
<td>3.12</td>
<td>1.14</td>
<td>5.13</td>
<td>2.23</td>
</tr>
<tr>
<td>0.10</td>
<td>468996</td>
<td>4.85</td>
<td>3.42</td>
<td>3.22</td>
<td>2.17</td>
</tr>
<tr>
<td>0.01</td>
<td>80794</td>
<td>4.42</td>
<td>4.28</td>
<td>5.67</td>
<td>3.14</td>
</tr>
</tbody>
</table>

4.2 Bi-level image coding

Bi-level images are a natural source of data for BAC. We developed a simple test suite that modelled images using the JBIG 10-pixel context. Each pixel was assigned a context according to the values of the pixels “underneath” the template, giving rise to 1024 possible contexts. For the B-coder, each context was allowed its own $Q$ and $R$ values, and maintained its own set of confidence estimates of the probabilities in the state-machine. Four collections of document images were used:

1. The eight ITU test images (known previously as the “CCITT suite”);
3. 155 pages selected at random from journals available on the JSTOR archive [14];
4. 210 pages selected at random from theses recently completed in the author’s department.

With the exception of collection 4, the images were all from scanned sources and contained varying levels of noise. The results are presented in table [3].

The B-coder performs best on the first three collections. On the ‘perfect’ images, generated from the theses, the ELS coder does best. For these very clean images, the B-coder isn’t able to adapt to the data as well as the ELS coder; one possible reason for this lies in the results from the previous section. In table [2] we see the ELS coder is able to out-perform the B-coder for LPS probabilities near to 0.10. The context statistics for the clean images involve LPS probabilities near to this value. Overall, the Z-coder is the worst performer.

4.3 Audio residual coding

For the final measurement of efficacy of the B-coder, we turned to a non-typical source: integers generated by coding residuals in audio coding. Following the approach used in
Figure 2: An example decision tree, suitable for coding 7-bit integers.

Table 3: A comparison of the B-coder against the ELS- and Z-coder coder for bi-level images. File sizes are in bits.

<table>
<thead>
<tr>
<th>Test Set</th>
<th>B-coder + static state</th>
<th>B-coder + dynamic state</th>
<th>ELS</th>
<th>Z-Coder</th>
</tr>
</thead>
<tbody>
<tr>
<td>CCITT</td>
<td>1672944</td>
<td>1670960</td>
<td>1678944</td>
<td>1688856</td>
</tr>
<tr>
<td>BBC</td>
<td>234551072</td>
<td>233959512</td>
<td>235396960</td>
<td>238096048</td>
</tr>
<tr>
<td>JSTOR</td>
<td>34025504</td>
<td>33998744</td>
<td>34146880</td>
<td>34459920</td>
</tr>
<tr>
<td>Theses</td>
<td>28562992</td>
<td>28522296</td>
<td>27845664</td>
<td>29558608</td>
</tr>
</tbody>
</table>

[IS], we developed a coder for monaural audio files. The audio data were split into frames, each 1192 samples long, and 4 finite impulse response predictors were used to predict the contents of each frame. Next, for each frame, the predictor that minimised the difference between the actual frame and the predicted frame was selected and the “residual” values (the difference between a predicted sample and its corresponding actual value) were coded using a BAC. The residuals follow approximately a Laplacian distribution and in the case of 16-bit sampling range from $-32768$ to $+32767$ (the range of signed 16-bit integers.) Efficiently coding the residuals using a BAC involved exploiting the distribution of residuals.

To encode the values, we used a tree structure similar to that shown in figure 2. Notice that the leaves of the tree are sets, $S$. The BAC was used to encode the decisions (at each $c.n$) that select the set and a $\log_2(\#(S))$ number was used to encode the position within $S$, where $\#(S)$ denotes the number of elements in $S$. The signs of the residuals were passed-through the encoder as a 1-bit number. Each of the arithmetic coders was incorporated into this scheme and was used to code audio files from six different genres. The results are presented in table 4.

The results show that the B-coder fares best over the different types of music, although in each case the performance of the Z-coder is very close. Interestingly, in this set of tests, the Z-coder and the ELS-coder have traded places for worst performer. One possible reason for this is that the Z-coder performs better than the ELS coder in range of $P(LPS) \geq 0.1;
Table 4: A comparison of the B-coder against the ELS- and Z-coder for audio residual coding. File sizes are in bytes.

<table>
<thead>
<tr>
<th>Audio File</th>
<th>B-coder + static state</th>
<th>B-coder + dynamic state</th>
<th>ELS</th>
<th>Z-Coder</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rock</td>
<td>13057278</td>
<td>13052245</td>
<td>14149493</td>
<td>13046911</td>
</tr>
<tr>
<td>Pop</td>
<td>23080175</td>
<td>23068182</td>
<td>25852924</td>
<td>23073038</td>
</tr>
<tr>
<td>Jazz</td>
<td>12198492</td>
<td>12186563</td>
<td>13150655</td>
<td>12190307</td>
</tr>
<tr>
<td>Spoken</td>
<td>19888302</td>
<td>19861438</td>
<td>21033058</td>
<td>19888255</td>
</tr>
<tr>
<td>Electronic</td>
<td>14166508</td>
<td>14159275</td>
<td>15507239</td>
<td>14163875</td>
</tr>
<tr>
<td>Classical</td>
<td>21949666</td>
<td>21927481</td>
<td>23258411</td>
<td>21924458</td>
</tr>
</tbody>
</table>

the decision tree structure used to code the residuals results in the context nodes dealing with probabilities in this range.

5 Conclusion and Further work

We have presented the B-coder, an approximate binary arithmetic coder that out-performs other comparable coders on a range of data. Additionally we have demonstrated an improvement of table-based probability estimation, which allows a probability estimator to better track the source probabilities.

The improvement made in the B-coder’s probability estimation makes a considerable difference in single-context coding (see table 2); where previous coders’ effective probability fluctuated over a large range, the B-coder is able to keep the effective probability under much tighter control. There are in effect two methods of improving the estimators performance, both using the confidence estimate: (1) allow the probabilities themselves to fluctuate; (2) allow the transitions between the states to fluctuate. In the B-coder, for speed we use technique (1) to achieve technique (2).

The B-coder has reasonable time performance, but our initial implementation was not totally optimised for speed. Our tests show it to be a little faster than the ELS coder, but somewhat slower than the Z-Coder. Possible speed improvements include taking advantage of word size by shifting out blocks of 32-bits at a time. We feel it is necessary to add the following caveat to our work. Recent advances in CPU technology mean that multiplication no longer has the massive cost disadvantage compared with shifts and additions (e.g. for a Pentium-4: IMUL 15µops, ADD+SHIFT 6 µops.) However, in a dedicated hardware device, i.e. when not using a general-purpose CPU, we believe our coder would be an excellent choice. For example, even at the micro-code level, because \( R \) is always greater than \( Q \), the shift of \( R \) includes the shift of \( Q \) and this can be exploited.

Further research might include investigating the update schedule (equation 5) Although our schedule works well over a range of applications, we found that for each file there was a different set of thresholds that gave much better results. This poses the question of whether it is possible to learn suitable thresholds from the data.
References


