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A NOVEL PHOTONIC CRYSTAL BAND-PASS FILTER USING DEGENERATE MODES OF A POINT-DEFECT MICROCAVITY FOR TERAHERTZ COMMUNICATION SYSTEMS

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ABSTRACT: Compact devices are important for the realization of terahertz communications systems. This article proposes a novel photonic crystal-based device for realizing microminiature, high-selectivity high Q band-pass filters (BPF) and the design of a dual-mode square lattice photonic crystal BPF that utilizes the degenerated modes of a point defect microcavity is presented. To design a high Q microcavity, the photonic band-gap is initially calculated using the plane wave expansion method. Second, the eigenfrequencies and modal fields of a point defect microcavity that generates localized states in the band-gap are calculated by a supercell method. Finally, the characteristics of mode splitting and the proposed dual-mode BPFs are numerically studied by a full-wave time-domain method. © 2014 Wiley Periodicals, Inc. Microwave Opt Technol Lett 56:792–797, 2014; View this article online at wileyonlinelibrary.com. DOI 10.1002/mop.28204

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1. INTRODUCTION

Devices operating at submillimeter wavelengths, or within the terahertz (THz) region of the electromagnetic spectrum (i.e., 0.1–10 THz), have allowed the development and realization of systems with new capabilities that span many fields of application; imaging, short-range and wideband secure communications, chemical and biological sensing, and material analysis to name but a few. In [1], a system comprised of electronic and photonic technologies has been demonstrated that is capable of relaying high-definition TV. Operating at a data-rate of 10 Gbit/s over a 120-GHz wireless system, this is a prime example of the utilization of submillimeter wave (sub-MMW) technologies. Compact and low-loss electromagnetic devices are key components for building future sub-MMW-integrated circuits operating at THz frequencies. Recently, a parallel plate metal waveguide in [2] has demonstrated excellent performance for guiding THz pulses with little distortion over a distance of the order of a few centimeters. However, there are some drawbacks with this structure; for example, it is not easy to control the propagation of the wave and the beam can only travel in one direction. To realize fundamental devices (e.g., filters, switches, and splitters), an integrated and compact silicon (Si)-based solid state platform for THz signal propagation, guidance, and control would be preferable. Fortunately, Si-based photonic crystals (PhC) are transparent in the THz range and they have shown promise in their ability to control the propagation of electromagnetic waves at these frequencies. However, problems will exist due to the discontinuities at the interfaces between the different circuit elements; therefore, care is needed when choosing and implementing specific computer-based simulation strategies during the design process.

In this article, we propose and simulate a novel PhC dual-mode band-pass filter (BPF), by integrating a high Q microcavity within a Si-based PhC platform. The resonant frequency splitting of a microcavity, which is important for the BPF design, is presented. Although two-dimensional (2D) PhCs lack a band gap in the direction perpendicular to the lattice plane, they offer substantial advantages in terms of compactness, stability, and fabrication, which make them attractive for THz devices [3, 4].

2. PROPERTIES OF THE 2D PHOTONIC CRYSTAL

2.1. Model of 2D Photonic Crystal in Air

In this article, we consider photonic crystals consisting of a 2D array of dielectric rods. These arrays form either a square or triangular lattice embedded within a parallel-plate metal waveguide. Figure 1 illustrates the case for a square lattice. A waveguide can then be created by introducing a line-defect within the crystal, this defect being surrounded by a finite number of rows, N, of periodically spaced dielectric rods. It is well known that the wave guided by this 2D PhC structure can be decomposed into transverse electric (TE: Ex, Ey, Hz) and transverse magnetic (TM: Hx, Hy, Ez) polarized modes which can also be designated as H-polarized and E-polarized modes, respectively. Various numerical methods have been employed to analyze the band structures and the transmission characteristics for PhC devices, and Figure 2 shows the computed values of the band gaps obtained by using the plane wave expansion method, [5]. To obtain accurate results, with an error of less than 1%, a significant number of component waves is required; 271 were used for those results shown in Figure 2. The band structure is dependent on the geometric and material parameters of the PhC, namely, the lattice parameters defined by the radius (r) and spacing of the rods (a), the refractive indices of the materials and corresponding refractive index contrast. A typical PhC material has a refractive index of n = 3.4 (relative dielectric constant of e = 11.56) which, at THz frequencies, corresponds to high-resistivity, high-purity silicon. With lattice parameters of r/a = 0.175, where a = 58.5 µm and r = 10.2375 µm, the PhC has a wide band-gap, for the Ez (TM) polarization in the frequency range of a/λ = 0.31–0.44, as illustrated in Figure 2 where λ = c/2πω, with c being the speed of light in a vacuum.
There is no corresponding band-gap for the Hz (TE) polarization.

2.2. Properties of PhC Straight Line Defect Waveguide

To obtain the transmission characteristics of PhC line-defect waveguides, a time-domain simulation was performed CST’s Microwave Studio [6]. The PhC was constructed on a mesh size of \( N_x = 919 \) by \( N_y = 219 \) with perfectly matched layers (PML) at the boundaries of the computational window. The line defect was created by removing one row of dielectric rods, as illustrated in Figure 3(a), [7, 8]. The waveguide was excited with a TM Gaussian modulated pulse with a center frequency of 0.35 \( \frac{a}{k} \). A key factor in designing a PhC waveguide is the propagation loss, \( S_{21} \), which is related to the confinement of the guided mode. Therefore, to validate our approach, simulations were initially performed on these straight waveguides and the convergence of transmission loss as a function of the number of rows, \( N \), used to represent the PhC lattice was examined [Fig. 3(a)]. We then obtained the transmission and reflection spectra for the 2D photonic crystal with three rows of dielectric rods, as shown in Figure 3(b). As can be seen from Figure 3(c), the waveguide
with $N = 3$ shows strong confinement for the TM mode over the frequency range of 1.7–2.3 THz. It should be noted that this single line-defect waveguide is single-moded. Figure 3(d) shows the corresponding dispersion relationship.

3. THE MICROCAVITY AND ITS APPLICATIONS

3.1. Model of the Microcavity and its Resonant Properties

In many emerging THz applications, BPFs play an important role. In particular, the demand for functional, high-performance components such as frequency selective filters is increasing in the field of short-range, high-speed THz communication systems. In this study, we focus our attention on the behavior of the first four resonant modes, that is TM$_{110}$-, TM$_{210}$-, TM$_{120}$-, and TM$_{220}$-like modes in a point defect microcavity, which are analogous to the resonant modes of a metal square-shaped microwave cavity. These resonant modes are computed by using a supercell approximation.

In the first example, a 2D $7 \times 7$ supercell containing 49 Si rods in air is considered; see Figure 1(b) with no perturbing rod. The radii of the regular rods are $r = 0.175a$ and the radius of the defect rod, $R_d$, is $0 < R_d < 2.5r$. The lattice constant, $a$, is 58.5 $\mu$m. The super-cell region is finely meshed, with the number of cells in the $x$ and $y$ dimensions being $N_x = 191$ and $N_y = 191$, respectively. Seven PML layers are used at the boundary of the problem structure to absorb all the outgoing energy. We consider the resonant modes of two types of microcavity coupled to a point-defect. The resonant frequencies and $E_z$-field distributions of the resonant modes for these cavities are presented in Figure 4. In Figure 4(a), the resonant modes of two microcavities are shown, presented for (left) $R_d = 0$ (a primitive point defect microcavity) and (right) for $R_d = 0.6r$. These modes correspond to the TM$_{110}$-like monopole modes of a square-shaped microwave cavity, that is, one half sine variation in the $x$ and $y$ directions. In Figure 4(b), $R_d = 1.6r$ which results in the doubly degenerate dipole modes that correspond to the TM$_{210}$ and TM$_{120}$ modes of a square-shaped microwave cavity. For these modes, the field distributions are antisymmetric and the modes disappear into the continuum below the band-gap when the radius of the rod becomes larger than $R_d = 2r$. 

Figure 4 Ez field distribution for four defect modes in the PhC point defect microcavity. (a) Monopole mode ($R_d$ less than $r$) shown for left $R_d = 0$ and right $R_d = 0.6r$ (b) doubly degenerate dipole mode, $R_d = 1.6r$, (c) coupled dipole mode, and (d) quadrupole mode. [Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com]

Figure 5 (a) Point defect narrow band microcavity filter without dielectric rod, (b) field distribution for $a = 58.5 \mu$m and $r = 0.175a$, (c) reflection (red) and transmission (black) characteristics as a function of frequency. [Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com]
A carefully designed PhC cavity can also be used as a high-Q narrowband filter in the THz band. The two degenerated dipole-like modes may exist independently of each other by perturbing the cavity through the introduction of an additional dielectric rod, see Figure 1(b). When no perturbation is present, only a single TM\(_{210}\)-or TM\(_{120}\)-like mode is excited by the dominant mode of the input/output waveguide. The addition of a small perturbation rod, of radius \(r_p\), causes the degenerate modes

![Diagram of PhC cavity with dielectric rod](image)

**Figure 6** (a) Point defect narrow band microcavity filter with an additional silicon dielectric rod \(R_d=1.6r\), refractive index \(n=3.4\) at its center, (b) field distribution for \(a=58.5\ \mu m\) and \(r=0.175a\), and (c) reflection (red) and transmission (black) characteristics as a function of frequency. [Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com]

![Graph of reflection and transmission](image)

**Figure 7** Structure of point defect microcavities with a dielectric rod \(R_d\) at their centers, and corresponding reflection (red) and transmission (black) characteristics as a function of frequency. (a) When excited from Port 1, the TM\(_{120}\)-like mode is not excited and there is little coupling to the orthogonal Port 2, (b) both Port 1 and Port 2 cannot couple to the quadrupole mode. [Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com]
to split, as shown in Figure 4(c), with the degree of splitting being a function of the radius of the perturbing rod. By increasing the radius $R_d$ of the defect rod, the quadrupole resonant mode (nondegenerate mode) can be excited in the bandgap, Figure 4(d). However, this quadrupole mode does not couple with the fundamental mode of the input/output ports.

Next, we considered the transmission characteristics of two types of microcavities coupled to straight- and right-angled line-defect waveguides. Schematics of the cavities (comprised of square lattices of Si rods in air) along with simulated results are shown in Figures 5–7. For the cavities coupled to straight waveguides shown in Figures 5 and 6, the transmission spectrum peaks at almost 0 dB at frequencies of 2.0 and 1.99 THz, for $R_d = 0$ and $R_d = 1.6r$, respectively. The field patterns in these cases illustrate the high $Q$ nature of the cavities where the field is observed to be strongly confined to a space of 2$a$ within the PhC. It is observed that these cavities have a relatively high-$Q$ resonance of at least $Q \sim 450$ and $Q \sim 940$ for the cases of $R_d = 0$ and $R_d = 1.6r$, respectively. Therefore, the $Q$ of dipole mode, which corresponds to the two degenerate TM$_{210}$ and TM$_{120}$ modes of a metal square-shaped microwave cavity, exceeds that of the fundamental monopole resonant mode. These modes are seen not to couple with the fundamental modes of the input and output ports in the right-angled case shown in Figure 7(a). The quadrupole resonant mode also does not couple with both the input and output ports, as indicated in Figure 7(b).

### 3.2. Transmission Properties of a Dual-Mode Band-Pass Filter using two Degenerate Modes

In the second example, we again consider a PhC point defect microcavity, $R_d = 1.6r$, but now with the inclusion of a small dielectric perturbation rod of radius $r_p$, Figure 8(a). With input and output ports in a right-angled configured, both the degenerate modes are excited and coupled to each other due to the addition of this small perturbation rod within the point defect microcavity [9]. The small dielectric perturbation rod, added at a point along a line that is 135° apart from both input and output ports, changes both the field and resonant frequency. This perturbation results in coupling between two orthogonal modes within the microwcavity, as shown in Figure 4(c). As a result, a shift in resonant frequency between two orthogonal modes occurs and the two degenerate dipole modes can couple with the dominant mode of input/output ports. The result is a realization of a dual-mode BPF utilizing the doubly degenerate dipole modes of the PhC point defect microcavity. An important issue in the design of this dual-mode filter is the precise control of the mode separation of the two degenerate modes at the working frequency. One approach is to change the radius ($R_d$) and dielectric constant ($\varepsilon$) of the dielectric rod at the center in the cavity, to realize the desired working frequency of the cavity illustrated in Figure 6(a). Two eigenfunctions describe the distribution of the electric field of the TM$_{210}$- or TM$_{120}$-like modes; the fields are depicted in Figure 4(c). The distribution of the electric field

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**Figure 8** (a) Structure of dual-mode bandpass filter using degenerate modes of photonic crystal point defect cavity showing the placed dielectric rod $R_d$ and small perturbation dielectric rod $r_p$, (b) transmission (red) and reflection (black) characteristics of dual-mode bandpass filter, (c) double-tuned characteristics of photonic crystal microcavity ($r = 10.2375$ $\mu$m, $a = 58.5$ $\mu$m, $R_d = 1.6a$, and $n = 3.4$ with, from left to right, undercoupled, critical coupling, and undercoupled conditions. [Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com]
in Figure 4(c) can be represented by the sum (= \(" TM_{210} + TM_{120} \)”) and difference (= \(" TM_{210} - TM_{120} \)”) of the modes in Figure 4(b). Figure 8(b) shows the optimized frequency characteristics of the dual-mode filter which is shown to have a stop-band with a rejection region located around 2 THz. The transmission spectra in Figure 8(c) show that the critical coupling is obtained for the perturbing cylindrical radius \( r_p = 0.6r \), overcoupled condition occurs for \( r_p = 0.7r \), and undercoupled condition for \( r_p = 0.55r \). The proposed dual-mode filters have the advantages of a high-unloaded \( Q \), small circuit size, and ease of interfacing with other functional circuits on a PhC platform.

4. CONCLUSION

The applicability of photonic crystal microcavities in the THz regime has been demonstrated through design and simulation. The results presented here indicate a new approach to designing a range of PhC-based devices for filter applications; dual-mode band-pass (or notch) filter, channel drop filter, planar crossing circuits, and so forth. By fine-tuning the lattice arrangement and the radius of the dielectric rods in the neighborhood of the junction or corner discontinuities, a Si/air PhC-based compact dual-mode BPF with a 2–3% rejection bandwidth at around 2.0 THz band has been designed and demonstrated through simulation. A high-Q microcavity has been achieved by modifying conventional point defect cavities through the addition of a dielectric rod in the defect location and the further addition of a perturbing rod into the PhC lattice. It is believed that a new dual-mode PhC point-defect microcavity is a very attractive structure from which to develop compact and high-performance THz band-pass or notch filters on a Si-based single platform.

Future work will extend the time-domain simulations demonstrated here to determine the transmission properties of new PhC planar circuits combining nonradiative dielectric H-guides, together with substrate-integrated waveguides, and PhC in operating in the THz regime.

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